



266-15367

CON

NASA CR-54738

A COMPUTER PROGRAM FOR ELECTRON OR ION GUN ANALYSIS:

OPERATIONS MANUAL

by

V. Hamza

M. L. Report No. 1369

September 1965

Microwave Laboratory

W. W. HANSEN LABORATORIES OF PHYSICS

STANFORD UNIVERSITY . STANFORD, CALIFORNIA



Interim Report

Prepared for

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

Contract NAS 3-4100

NOTICE

This report was prepared as an account of Government sponsored work. Neither the United States, nor the National Aeronautics and Space Administration (NASA), nor any person acting on behalf of NASA:

- A.) Makes any warranty or representation, expressed or implied, with respect to the accuracy, completeness, or usefulness of the information contained in this report, or that the use of any information, apparatus, method, or process disclosed in this report may not infringe privately owned rights; or
- B.) Assumes any liabilities with respect to the use of, or for damages resulting from the use of any information, apparatus, method or process disclosed in this report.

As used above, "person acting on behalf of NASA" includes any employee or contractor of NASA, or employee of such contractor, to the extent that such employee or contractor of NASA, or employee of such contractor prepares, disseminates, or provides access to, any information pursuant to his employment or contract with NASA, or his employment with such contractor.

Requests for copies of this report should be referred to
National Aeronautics and Space Administration
Office of Scientific and Technical Information
Attention: AFSS-A
Washington, D. C. 20546

NASA CR-54738

A COMPUTER PROGRAM FOR ELECTRON OR ION GUN ANALYSIS:
OPERATIONS MANUAL

By

V. Hamza

M. L. Report No. 1369
September 1965

Interim Report
Prepared for
NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
Contract NAS 3-4100

Microwave Laboratory
W. W. Hansen Laboratories of Physics
Stanford University
Stanford, California

TABLE OF CONTENTS

	<u>Page</u>
I. Introduction	1
II. Computer program for beam analysis	3
A. Data input	5
B. Fortran coding form	13
C. Data output.	13
III. Computer program for spectral radius calculation - XR - calculation.	46
A. Data input	46
B. Data output.	47
Appendices	
A. Flow chart and Fortran II. Statements for beam analysis	52
B. Flow chart and Fortran II. Statements for XR-calcula- tion	80
C. Detailed flow charts	89
References	102

I. INTRODUCTION

This report describes a computer program, shown at the end of the report, which is used to analyze the space-charge flow in an electron or ion gun. It determines the nature of the beam profiles for practically any specified two-dimensional or axially symmetric gun electrode system. The basic process that is followed is to initially assume that the space-charge density is zero, solve LaPlace's equation by finite-difference methods, and find the potential variation in the region of interest shown in Fig. 1.. With a knowledge of this potential variation, the motion of charged particles from the emitter source is determined, and the current density emitted is found by the Child-Langmuir law in the neighborhood of the emitter. The whole process is then repeated through several iterative cycles (solving Poisson's equation instead of LaPlace's equation), until the final solution converges to a self-consistent solution. The use of the program will be illustrated by an example of an ion propulsion gun design.

It is beyond the scope of this report to explain the mathematical method used; the reader is referred to the references for this.

The computer program has been written in the IBM 7090 Fortran II programming language, which requires at least a 32,000 word core for execution.

Subroutines of the computer program will be now listed with a brief explanation of their function.

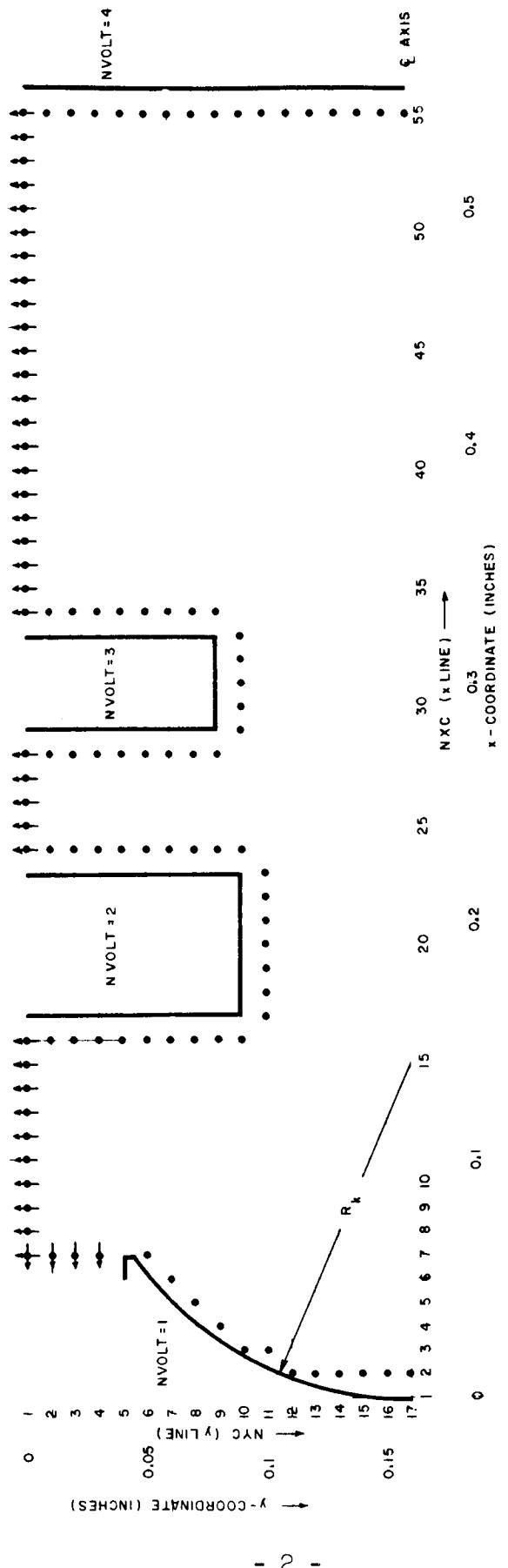


FIG. 1--Layout of electrode system for beam analysis.

II. COMPUTER PROGRAM FOR BEAM ANALYSIS

It is to be emphasized that all Fortran statements referring to plotting may have to be changed in accordance with the particular installations where the program is being used. The statements herein refer specifically to the plotting routines at the Stanford Computation Center, and may not be accurate elsewhere.

Subroutines Required:

1. MAIN ØNE*

Starts the program, brings in all the data input, calculates the matrix coefficients, plots the electrode boundary points and calls UCAL for LaPlace's solution and then MNTRI.

2. ARC

Calculates the emitter length, determines the width of the current tubes (ARCL) and establishes the beginning trajectory coordinates (ETX, ETY). ARC is called by MNTRI.

3. CALR

Calculates the right hand side (RHS) of the matrix equation (space-charge density). CALR is called by MNTRI.

4. CØRRCT

Checks on trajectories intercepted by the electrode system.
CØRRCT is called by TRCU.

5. EQLINE

Calculates the equipotential line coordinates throughout the region of interest, starting with the potential VAT, and continues by increment of SIZE until the potential of VBT is reached for each cycle if KCY(J) > 0 , (where J represents cycle number), otherwise, no calculation (if SIZE = 0 no equipotential line coordinates calculation). EQLINE is called by UCAL.

* Ø Represents OU to distinguish from O as zero.

6. MATRIX

Solves the matrix equation for each line, e.g., matrix equation

$$A\underline{w} = \underline{k}$$

$$\underline{w} = A^{-1}\underline{k} .$$

MATRIX is called by UCAL.

7. MNTRI

Governs the whole solution once the initial (LaPlace's) potential distribution is known. MNTRI is called by MAIN.

8. PEQ

Calculates the equipotential line coordinates through a given point $N\phi_{PT}$ ($N\phi_{PTX}$, $N\phi_{PTY}$) for current density calculation. PEQ is called by MNTRI.

9. TRAJ

Calculates the trajectory coordinates through the region of interest once the trajectories were initialized. TRAJ is called by TRCU.

10. TRCU

Initializes trajectories and calculates current density distribution along the emitter. TRCU is called by MNTRI.

11. TR ϕ UT

Prints out the RHS distribution through the region of interest for each cycle if $IX\phi > 0$ and $KCY(J) > 0$. Otherwise, no print-out. TR ϕ UT is called by MNTRI.

12. TW ϕ UT

Prints out the potential distribution through the region of interest for each cycle, if $KCY(J) > 0$. The final solution is printed automatically. TW ϕ UT is called by UCAL.

13. UCAL

Solves for potential distribution inside the region of interest. UCAL is called by MAIN for LaPlace's solution, then by MNTRI for the space-charge-flow solution.

14. 7090 PLOTTING ROUTINES (Fortran II) for the CalComp Plotter (Stanford University Computation Center Library Program No. 157).

A. DATA INPUT

It is recommended that a scaled graph of the configuration to be analyzed be drawn as shown in Fig. 1. Attention is given to two different sets of coordinates, e.g., x-y line coordinate and x,y coordinate in inches (dimension in inches is not essential).

The first data card is the number of heading cards (NH) which will follow (e.g., identification of run by serial number, date, description, etc.). It is particularly useful to differentiate repeated machine deck executions of the program.

The second data card is as follows:

NXF	total number of x-lines
NYF	total number of y-lines
NEM	number of x,y coordinates specifying emitter surface (a minimum of two are required, namely, the end points).

NTJ	number of trajectories
NDIM	two-dimensional geometry ≤ 2 , axially symmetric geometry > 2
NRL	number of cycles (e.g., NRL = 2; LaPlace's solution is considered as zeroth cycle, then 2 cycles plus last cycle; altogether 4 cycles); must be greater than 0
NUL	number of iterations for LaPlace's solution
NURL	number of iterations for Poisson's solution (after last cycle NURL used as a switch to terminate the problem)
NC ϕ R	positive, emitter coordinates are beginning trajectory coordinates; negative or zero, beginning trajectory coordinates are calculated
IDEC	negative, emitter is concave (for flat emitter use IDEC < 0 with XEMIT $\rightarrow \infty$); zero and positive, emitter is convex
NFUL	0 for the case of axial symmetry or for the case of two-dimensional geometry when symmetry about the axis is used to eliminate the lower half plane from the computation; 1 for the case of two-dimensional geometry when the full problem is considered in the calculation.
NC ϕ	number of lines in x-direction for which noncalculated points (outside the region of interest, e.g., electrode) will be set to a potential of the emitter (VA); in most cases this can be taken to be the number of x-mesh lines up to the face of the first electrode beyond the emitter
KRHX	x-line coordinate of the test point for RHS
KRHY	y-line coordinate of the test point for RHS

The third data card is as follows:

IX ϕ	positive, RHS prints out-condition to KCY > 0; negative or zero, RHS will not print out
NSPAN	number of x-lines to traverse to obtain equipotential line for current density calculation; this is used for conserving time

in the scan for the equipotential used in the calculation
 used in the calculation of emitter current density
 NP ϕ TX { x- and y-line coordinate of a point whose potential will be
 NP ϕ TY } used for determining the coordinates of the equipotential line
 for current density calculation.
 YAXS y-coordinate of the axis of symmetry

The fourth data card shows:

KRTN number of test points (test point determines whether its
 potential is lower than the emitter potential; if so, the
 calculation proceeds; if not, EXIT is called

KRTX { x- and y-line coordinate of a test point.
 KRTY

The fifth data card gives this information:

VAT upper potential in equipotential calculation (see definition
 of subroutine EQLINE)

VBT lower potential in equipotential calculation

SIZE step size in equipotential calculation

VA emitter potential

VB highest negative potential, otherwise zero

VC y-distance in inches for y-positioning of the output plot
 [VC = 10.0 (maximum width of the graph paper is 10") moves the
 pen to point (0.0, 10.0) and makes that the reference point].

The sixth data card is:

HGH the largest y-coordinate (in inches) of the second elec-
 trode chosen for checking on trajectories for possible
 interception

$XL\phi W$	the largest y-coordinate (in inches) of the first electrode chosen for checking on trajectories for possible interception (e.g., in example given, only the second accelerator electrode was chosen to check on trajectories)
HSL	not used
XSL	slope of a line to which normal derivative should be zero, (see sketch below)
	Note: the first calculated point of each line should be taken directly above or on the line of symmetry and must be identified by $ND(3) > 0$ in addition to $NS = 1$
VD	scaling factor for plotting purposes; H times VD gives actual inches on plot.
	The seventh data card gives:
AXX	the x-coordinate in inches where subroutine CORRCT starts to check on $XL\phi W$ for possible trajectory interception
BXX	the x-coordinate in inches where subroutine CORRCT stops to check on $XL\phi W$ and starts to check on HGH for possible trajectory interception

CXX the x-coordinate in inches where subroutine CORRCT stops
 to check on HGH for possible trajectory interception

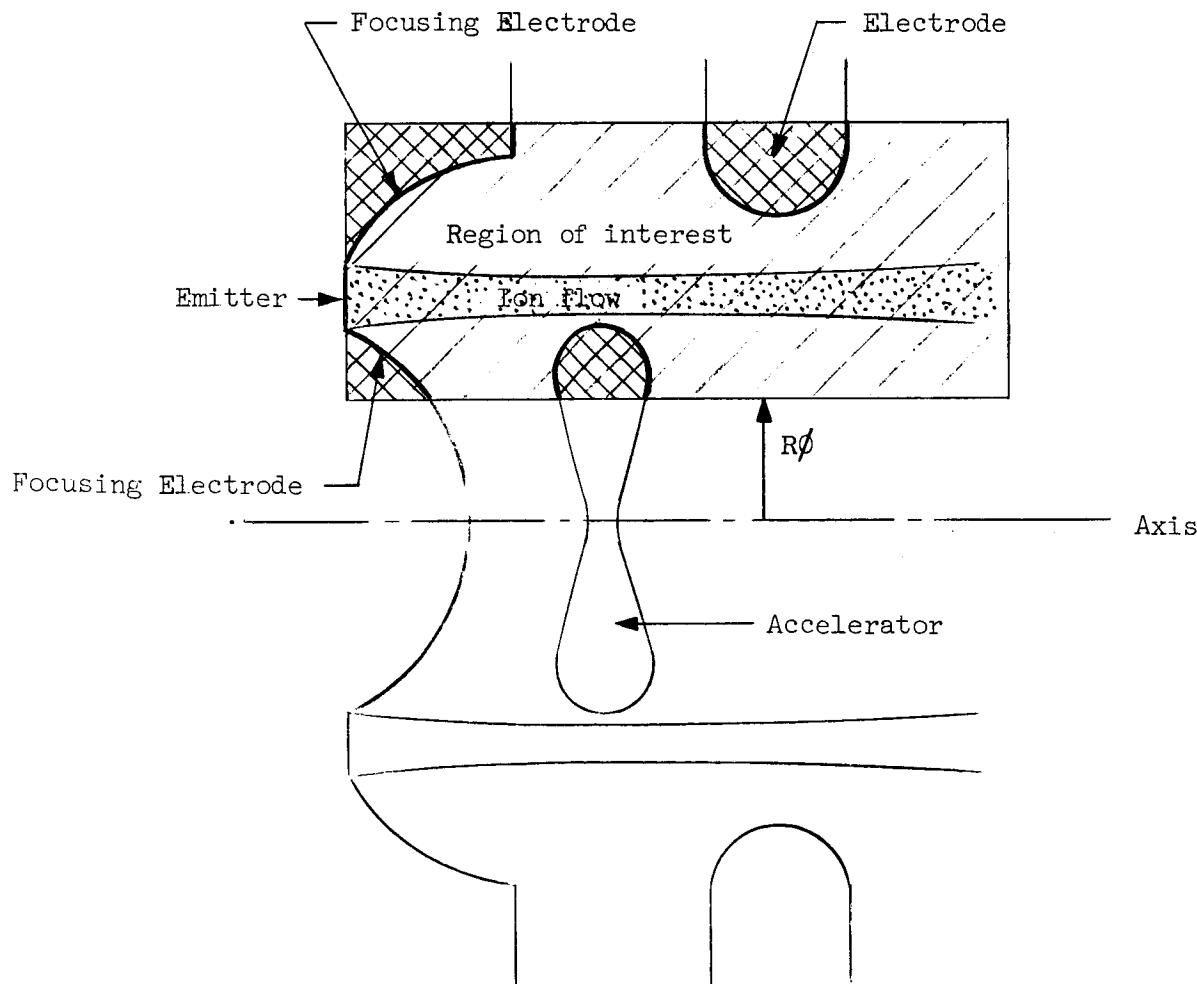
DXX a constant - not used

XR the spectral radius of the matrix (the largest eigenvalue)
 obtained by a separate program using essentially the same
 data input (see Spectral Radius Calculation).

The eighth data card consists of:

$R\phi$ the distance in inches from the axis (for axially geometry
 only) when the axis is not part of the region of interest.

See sketch below



EPS convergence test for matrix equation. (Data output prints EPSIL ϕ N)

XEMIT x-coordinate in inches of the emitter radius (XEMIT is equal to the emitter radius only if the emitter x-coordinate passes through zero) and must be a very large number for a flat emitter.

H mesh size in inches. (Data output prints MESH SIZE-H)

The ninth data card shows:

YEP permittivity of free space (Data output prints EPSN ϕ T)

XQ ϕ M specific charge-to-mass ratio for proton (or electron)

AT ϕ M atomic weight number of ion flow (for electron flow, AT ϕ M = 1.0)

VTH transverse thermal velocity of emission

VTHX } not used.

VTHY }

The tenth data card is as follows:

ATX } x- and y-corrdinates (in inches) of the emitter shape
(three (x,y) coordinates per card). Total number of x,y
ATY } coordinates must equal NEM, and they must follow in order
of increasing y-coordinate.

The eleventh data card gives:

KCY positive, all print-outs occur (condition to IX ϕ > 0 and
SIZE > 0) ; negative or zero, no print-outs.

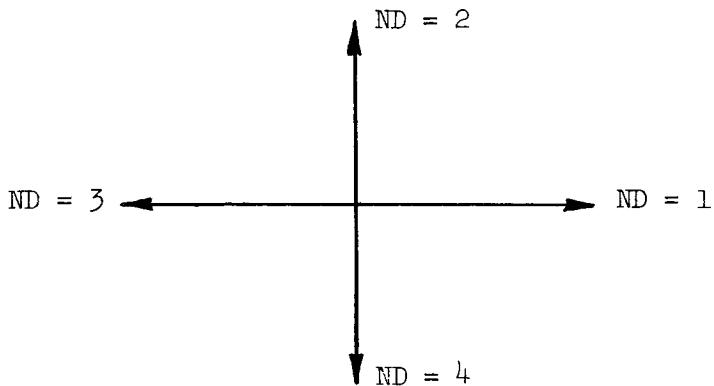
Note: Last cycle (final solution) is automatically
printed out.

The twelfth data card consists of electrode voltage register (7 voltages per card, 4 cards needed). Twenty-eight voltages available, labeled from NV ϕ LT (or NV ϕ LT1) = 1 to NV ϕ LT (or NV ϕ LT1) = 28.

The thirteenth data card consists of the boundary points of an electrode system. The calculation is broken up into a series of lines consisting of simply connected interim points. There may be more than one of these lines for each x-line. The boundary points are specified by proceeding from the top to the bottom and left to right, one boundary point per card.

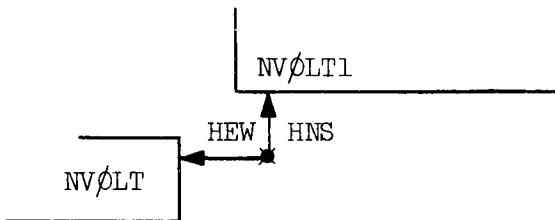
NS = 1 the first and uppermost calculated point inside the region of interest for each set of simply connected interim points
= 2 the last and lowermost calculated point inside the region of interest for each simply connected set of interior points. In case the axis of symmetry constitutes the boundary of the electrode system as shown in Fig. 1, the whole card specifying the last calculated point for that x-line is not necessary for any point
= 0 inside the region of interest containing any information about the boundary of the electrode system (excluding the two cases above for which NS = 1 and 2).

ND(1)
ND(2) } specify the zero normal derivative of the potential of that point according to the direction as shown:



There is a possibility that two normal derivatives may be zero at one point but not more. It is also possible to set one derivative equal to zero and specify a potential on the same boundary card.

$ND(3) > 0$ indicates that the boundary point faces two different potentials, as shown below:



or that the normal derivative is zero to some prescribed line given by the slope of $XLSL \neq 0$, otherwise zero

NXC x-line coordinate of the boundary point

NYC y-line coordinate of the boundary point

HEW represents the distance left or right from the boundary point to the solid boundary (electrode) in percent of mesh size (maximum = 1.0 \equiv one whole mesh). The distance to the right (East) is positive, whereas the distance to the left (West) is negative)

HNS same as HEW for up and down boundary. The distance up (North) is positive, whereas the distance down (South) is negative

NV ϕ LT is the index number of the voltage register specifying the voltage of the boundary point to the left or right

NV ϕ LT1 same as NV ϕ LT for the boundary point up or down with ND(3) > 0 . Note: In the case (NV ϕ LT = NV ϕ LT1) or when the boundary point (up or down) is the only boundary potential, it is not necessary to specify NV ϕ LT1 with ND(3) > 0 . In this case, it is sufficient to specify NV ϕ LT only.

NCHECK = 1 for the last boundary point. (This is important because check is made on the last data card if NCHECK = 1 in case of no, the EXIT is called). For this card one must put NXC = NXF and NYC = NYF even if this requires a dummy card.

B. FORTRAN CODING FORM

The format of the Data Input Deck is shown on the next three pages.

C. DATA OUTPUT

The output consists of a plot shown in Fig. 2. The trajectories and electrode boundaries are given to scale.

The Data Output print-out starts on page 23. The first three pages consist of Data Input for the record. Every "read in" data card is automatically printed-out with identification. Page 26 shows the information on zeroth cycle - No space-charge-LaPlace solution. Iteration No. = 45, indicating that 45 iterations were completed for calculating the potential distribution, with point 731 (or x-line = 43, y-line = 17)

EXAMPLE SHOWN ON FIGURE 1

Punching Instructions							Page 1 of 3
Graphic			Card Form #			*	Identification
Program	TON THRUSTOR ANALYSIS	Date 9/31/65	Punch				73
Programmer	V. HAMZA						80
C FOR COMMENT							

STATEMENT NUMBER	5	6	7	10	15	20	25	30	35	40	45	50	55	60	65	70	72
1																	

114

2

DEFLECTING PLATES FOR TON ENGINE №. 1
NASA-LEWIS FOR F. KAVANAGH / S. JONES

NXF NYF NEM NTJ NDIN NPL NURLNCΦΦR IDEC NFUL NCΦ KRHK KRHY

55 17 8 10 3 2 45 45 0 -1 0 14 2 17

IΧΦ NΣΡΑΗ ΗΡΦΤΞΝΡΦΤΥ
1 13 5 17

KRTN KRTX KRTY
1 2 17

VAT VBT SIZE VA VB
2000. 500. 500. 2100. 0.

HGH XLΦW HSL XLSL VD
0. 0.08 0. 0. 0. 20.

AXX BX_X CXX DXX XR
0.28 0.32 0.54 0.54 0.9804

RΦ EPSILAN XEMIT MESH SIZE - H
0. 0.01 0.14 0.01

EPSILAN XQM ATΦA VT_H
8.854E-12 9.579E+07 1.329E+02

VT_H VT_H VT_H VT_H

IBM

FORTRAN CODING FORM

Program ION THRUSTOR ANALYSIS		Punching Instructions		Page 2 of 3
Programmer R. HAMZA	Date 7/31/65	Graphic	Punch	Card Form # *
C FOR COMMENT				Identification 73 60

FORTRAN STATEMENT									
STATEMENT NUMBER	5	6	7	10	15	20	25	30	35
ATX	ATY	ATX	ATY	ATX	ATY				
0.06	0.044	0.05	0.052	0.04	0.04				
0.025	0.08	0.014	0.10	0.006	0.12				
0.002	0.14	0.0	0.16						
PRINT-OUT OF CYCLE NO.									
KEY(3) KEY(8)	KEY(8) KEY(4)	...							
0	0								
ELECTRODE VOLTAGE									
NVOLT-1	NVOLT-2	NVOLT-3	NVOLT-4	NVOLT-5	NVOLT-6	NVOLT-7			
2100.	0.	0.	500.	2000.	1800.	1600.			
1400.	1200.	1000.	800.	600.	400.	200.			
100.	50.	0.	0.	0.	0.	0.			
0.	0.	0.	0.	0.	0.	0.			
BOUNDARY POINTS OF ELECTRODE SHAPE									
SUM	NC	NYC	NEW	HNS	NVOLT	NNVOLT	CHECK		
1	2	12	-100	200	1				
2	13	-400			1				
2	14	-650			1				
2	15	-800			1				
2	16	-950			1				

IBM

FORTRAN CODING FORM

Program	TON THRUSTOR ANALYSIS		Punching Instructions	Page: 3 of 3
Programmer	V. HAMZA		Card Form # *	Identification
Date	7/31/65		Punch	73 74 75 76 77 78 79 80

C FOR COMMENT

FORTRAN STATEMENT		50	55	60	65	70	72
STATEMENT NUMBER	C FOR COMMENT	30	35	40	45		
1							
2	2 17-1.	1					
1	3 10 -150 300	1					
1	3 11 -700	1					
	:	:					
2	55 17 1.	4	1				

THIS IS THE LAST DATA CARD

NOTE: THE ALPHANUMERICAL DATA CARDS SHOWN HERE ARE FOR IDENTIFICATION ONLY. THEY WILL NOT APPEAR IN THE DATA DECK. THE ASSEMBLED DATA DECK CONTAINS NUMERICAL DATA ONLY WITH THE EXCEPTION OF THE FIRST CARDS IDENTIFYING THE PROBLEM AS NOTED ABOVE. HOWEVER, THE DATA OUTPUT WILL HAVE THESE ALPHANUMERICAL DATA PRINTED AUTOMATICALLY.

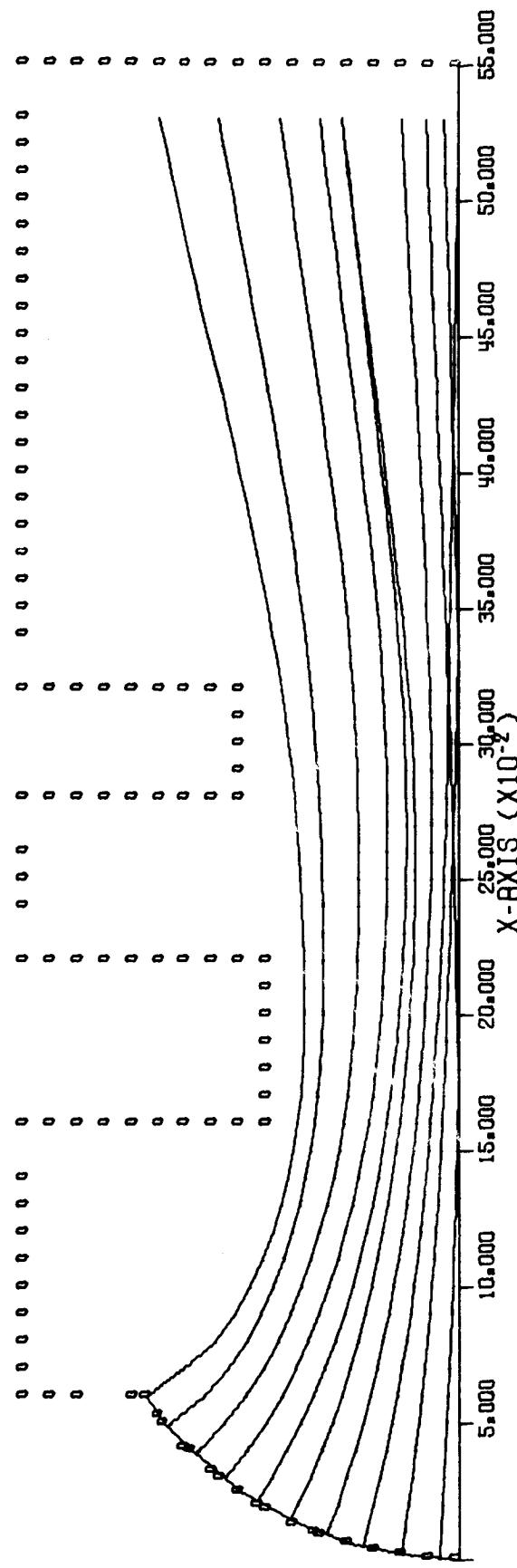


FIG. 2--Plot of the final solution.

displaying the largest error of $\underline{\epsilon} = 25.78$. [Note:

$$\underline{\epsilon} \triangleq \frac{2(\Delta U_{\max})}{\frac{1}{\left(\frac{NXF}{2}\right)^2} + \frac{1}{\left(\frac{NYF}{2}\right)^2}}$$

where

$$\Delta U_{\max} = \max_{1 \leq i \leq N} (U^{m+1} - U^m)$$

and $m + 1$ is the last iteration number ($N \equiv$ total No. of points). It is not, therefore, the difference in the potential of the last two iterations.] $\text{EPSILON} = 0.01$ is the given error in the Data Input to compare with $\underline{\epsilon}$. The total length of the emitter circular arc in inches is $\text{ARC} = 0.13524$. $\text{DELTA ARC LENGTH} = 0.01424$ is the arc increment of each current tube (or the spacing between two adjacent trajectories). The $X, Y - \text{EMITTER}$ prints-out coordinates of the emitter given in the Data Input, and $X, Y - \text{BEGIN TRAJ.}$ gives the calculated beginning trajectory coordinates. (Note: No. 1 is always the first pair of coordinates given in Data Input ($X, Y - \text{EMITTER}$ discussed above), likewise the last one located along the axis.

The expression $X, Y - \text{EQUIPOTENTIAL}$ represents the (x, y) coordinates in inches of the equipotential line through the given point $\text{NPOT}(NPOTX, NPOTY)$ specified by the Data Input, for the current density calculation.

The intercepts of two normals to the emitter on the equipotential line for the current density calculation of the seventh current tube (number shown in the last column) are X1, Y1 and X2, Y2. The normals are drawn from the points of the seventh and the eighth beginning trajectory coordinates. The arithmetic mean distance between the emitter surface and the equipotential line used in the Child-Langmuir formula for calculating the current density of the seventh current tube is represented by DX.

The current density in amp/in² (or amp/unit area in the case of different dimensions used for unit length) is CD. The last-but-one column displaying -1 indicates that the first x-line closest to the emitter for the seventh or for both the seventh and the eighth trajectories is less than one half of the mesh width away, thus the trajectories have not yet been initialized. (Here 0 indicates that the trajectories have been initialized and from that point on the coordinates of the trajectories are calculated from the potential distribution. This point will be more apparent when the last cycle is discussed where the x-coordinates are also shown.) The order of current tubes printed, given by the last column, is given in order of machine calculation.

EMITTER CURRENT IN TUBES shows the total current in amps., (in two-dimensional cases amp/in of emitter length out of paper) for each tube. TOTAL EMITTER CURRENT \approx 0.0023 amps (for two-dimensional cases amp/in of emitter length out of paper).

Page 27 gives similar information on CYCLE No. 1. The only difference from the previous page is RTEST = 0.01825 and UTEST = 2034.5567. Here RTEST is the value of the RHS (right hand side of the matrix equation, containing information on space-charge density) at the point KRH(KRHX,KRHY)

specified in the Data Input, and UTEST is the value of the potential at the point KRH. The information on the emitter coordinates and the beginning trajectory coordinates shown for the previous cycle are not given because they are identical. The rest of the page contains information discussed in the previous cycle. Page 28 shows similar information for CYCLE No. 2. Page 29 starts the information for the final solution. The print-out of the previous cycles is given primarily for checking purposes. Namely, RTEST must increase from cycle to cycle and must approach an asymptotic value if the number of cycles has been allowed to increase indefinitely (in other words, the difference between two following cycles must be decreasing). Likewise, the indicated ERROR must be decreasing from cycle to cycle.

Next, the information on pages 29-31 is the U-FIELD of LAST CYCLE ≡ (discrete potential value for each point through the region of interest given in Fig. 1). The first column indicates the x-line number, the next 8 columns represent the y-line number, thus defining every point in the region of interest. Columns 10 to 17 correspond to the respective potential values for each point given by x-line, y-line (e.g., the potential of the point given by x-line = 8 and y-line = 6 is 1759.447 volts.) The X,Y COORDINATES OF EQUIPOTENTIAL LINES shown on pages 31-32 are the (x,y) coordinates in inches for a given equipotential, starting with the potential specified by the Data Input VAT = 2000.0 and continued by an increment given by SIZE = 500.0 until final potential given by VBT = 500.0 is reached. The order of print-out of the coordinates is in order of machine calculation.

The next information given on page 32 is the coordinates of the equipotential line for the current density (X,Y-EQUIPOTENTIAL) calculation. Then the current density for the current tubes (7, 8, 9, and 10) are printed; this could be calculated at the station shown by $X = 0.01$ (for the rest of the beginning trajectory, x-coordinates are greater than $X = 0.01$ and thus they could not yet be initialized). Then for each x-line (e.g., $X = 0.01$) the y-coordinate of the initialized trajectories No. 9 and No. 10 are given. (Notice 0 above the statement $X = 0.01$ in the last-but-one column for the current density calculation for the current tube 9 and 10 and -1 for the tube 7 and 8; indicating that trajectories 7 and 8 will be initialized again on the next x-line because the distance from the emitter to the x-line was less than one half of a mesh size.)

The columns VX and VY correspond to the x- and y-velocities of the ions. Pages 33 to 42 show the rest of the (x,y) coordinates of the trajectories and their respective x- and y-velocities. The right hand side (RHS) of the matrix equation is shown on pages 42 to 45 for each point. This print-out occurs because of the $IX\phi > 0$ specification given in Data Input. From this RHS distribution, the current density profile in the beam can be obtained for any desired x-line location. For axially symmetric geometries we have

$$RHS = rh^2 \frac{J}{VX} .$$

Thus, knowing RHS, r, h, and VX it is easy to calculate J . Similarly, for two-dimensional geometries we have

$$\text{RHS} = h^2 \frac{J}{VX}$$

The last information on page 45 contains the total current distribution in each current tube at the emitter and finally the total emitter current.

DATA OUTPUT PRINT-OUT BY THE COMPUTER

DEFLECTING PLATES FOR ION ENGINE NO.1
NASA-LEWIS FOR F.KAVANAGH/S.JONES

08/02/65

VXF	VYF	NEM	NTJ	NDIM	NRL	NUL	NURLNCOOR	IDEC	NFVL	VCD	KRHX	KRHY
55	17	8	10	3	2	45	45	0	-1 0	14	2	17

IXONSPANNPOTXNPOTY YAXS
1 13 5 17 0.0

KRTN KRTX KRTY KRTX KRTY KRTX KRTY

1	2	17	VAT	VBT	SIZE	VA	VB	VC
2000.0000	500.0000	500.0000	2100.0000	-0.	8.0000			
HGH	XLOW	HSL	XSL	VD				
-0.	0.0800	-0.	-0.	20.0000				
AXX	BXX	CXX	DXX	XR				
0.2800	0.3200	0.5400	0.5400	0.9804				
RD	EPSILON	XEMIT	MESH SIZE - H					
0.	0.01000000	0.13999999	0.01000000					
EPSNOT	XQM	ATOM	VTH	VTHX	VTHY			
.88540E-11.95790E	08.13290E	03.	.	.	.			

CATHODE COORDINATES

0.0600	0.0440	0.0500	0.0520	0.0400	0.0520
0.0250	0.0800	0.0140	0.1000	0.0060	0.1200
0.0020	0.1400	-0.	0.1500		

PRINT-OUT OF CYCLE NO.

-0	-0	-0	-0	-0	-0	-0	-0	-0
----	----	----	----	----	----	----	----	----

VOLT-1	-2	-3	-4	-5	-6	-7
2100.0000	0.	0.	500.0000	2000.0000	1800.0000	1600.0000
1400.0000	1200.0000	1000.0000	800.0000	600.0000	400.0000	200.0000
100.0000	50.0000	-0.	-0.	-0.	-0.	-0.
-0.	-0.	-0.	-0.	-0.	-0.	-0.

BOUNDARY POINTS OF ELECTRODE SHAPE

1000	2	12-0.100 0.200	1	-0	-0
0000	2	13-0.400-0.	1	-0	-0
0000	2	14-0.650-0.	1	-0	-0
0000	2	15-0.800-0.	1	-0	-0
0000	2	16-0.950-0.	1	-0	-0
2000	2	17-1.000-0.	1	-0	-0
1000	3	10-0.150 0.300	1	-0	-0
0000	3	11-0.700-0.	1	-0	-0
1000	4	9-0.500 0.700	1	-0	-0
1000	5	8-0.750 0.800	1	-0	-0
1000	6	7-0.900 0.800	1	-0	-0
1230	7	1-0. -0.	1	-0	-0
0300	7	2-0. -0.	1	-0	-0
0300	7	3-0. -0.	1	-0	-0
2300	7	4-0. -1.000	1	-0	-0
1000	7	6-0.700 0.500	1	-0	-0
1200	8	1-0. -0.	1	-0	-0
1200	9	1-0. -0.	1	-0	-0
1200	10	1-0. -0.	7	-0	-0
1200	11	1-0. -0.	9	-0	-0
1200	12	1-0. -0.	11	-0	-0
1200	13	1-0. -0.	13	-0	-0

1200	14	1-0.	-0.	2	-0	-0
1200	15	1-0.	-0.	2	-0	-0
1200	16	1	1.000-0.	2	-0	-0
0000	16	2	1.000-0.	2	-0	-0
0000	16	3	1.000-0.	2	-0	-0
0000	16	4	1.000-0.	2	-0	-0
0000	16	5	1.000-0.	2	-0	-0
0000	16	6	1.000-0.	2	-0	-0
0000	16	7	1.000-0.	2	-0	-0
0000	16	8	1.000-0.	2	-0	-0
0000	16	9	1.000-0.	2	-0	-0
0000	16	10	1.000-0.	2	-0	-0
1000	17	11-0.	1.000	2	-0	-0
1000	18	11-0.	1.000	2	-0	-0
1000	19	11-0.	1.000	2	-0	-0
1000	20	11-0.	1.000	2	-0	-0
1000	21	11-0.	1.000	2	-0	-0
1000	22	11-0.	1.000	2	-0	-0
1000	23	11-0.	1.000	2	-0	-0
1200	24	1-1.000-0.		2	-0	-0
0000	24	2-1.000-0.		2	-0	-0
0000	24	3-1.000-0.		2	-0	-0
0000	24	4-1.000-0.		2	-0	-0
0000	24	5-1.000-0.		2	-0	-0
0000	24	6-1.000-0.		2	-0	-0
0000	24	7-1.000-0.		2	-0	-0
0000	24	8-1.000-0.		2	-0	-0
0000	24	9-1.000-0.		2	-0	-0
0000	24	10-1.000-0.		2	-0	-0
1200	25	1-0.	-0.	2	-0	-0
1200	26	1-0.	-0.	2	-0	-0
1200	27	1-0.	-0.	3	-0	-0
1200	28	1	1.000-0.	3	-0	-0
0000	28	2	1.000-0.	3	-0	-0
0000	28	3	1.000-0.	3	-0	-0
0000	28	4	1.000-0.	3	-0	-0
0000	28	5	1.000-0.	3	-0	-0
0000	28	6	1.000-0.	3	-0	-0
0000	28	7	1.000-0.	3	-0	-0
0000	28	8	1.000-0.	3	-0	-0
0000	28	9	1.000-0.	3	-0	-0
1000	29	10-0.	1.000	3	-0	-0
1000	30	10-0.	1.000	3	-0	-0
1000	31	10-0.	1.000	3	-0	-0
1000	32	10-0.	1.000	3	-0	-0
1000	33	10-0.	1.000	3	-0	-0
1200	34	1-1.000-0.		3	-0	-0
0000	34	2-1.000-0.		3	-0	-0
0000	34	3-1.000-0.		3	-0	-0
0000	34	4-1.000-0.		3	-0	-0
0000	34	5-1.000-0.		3	-0	-0
0000	34	6-1.000-0.		3	-0	-0
0000	34	7-1.000-0.		3	-0	-0
0000	34	8-1.000-0.		3	-0	-0
0000	34	9-1.000-0.		3	-0	-0
1200	35	1-0.	-0.	3	-0	-0
1200	36	1-0.	-0.	3	-0	-0
1200	37	1-0.	-0.	3	-0	-0
1200	38	1-0.	-0.	3	-0	-0

1200	39	1-0.	-0.	3	-0	-0
1200	40	1-0.	-0.	3	-0	-0
1200	41	1-0.	-0.	3	-0	-0
1200	42	1-0.	-0.	3	-0	-0
1200	43	1-0.	-0.	3	-0	-0
1200	44	1-0.	-0.	3	-0	-0
1200	45	1-0.	-0.	3	-0	-0
1200	46	1-0.	-0.	3	-0	-0
1200	47	1-0.	-0.	3	-0	-0
1200	48	1-0.	-0.	3	-0	-0
1200	49	1-0.	-0.	3	-0	-0
1200	50	1-0.	-0.	3	-0	-0
1200	51	1-0.	-0.	3	-0	-0
1200	52	1-0.	-0.	3	-0	-0
1200	53	1-0.	-0.	3	-0	-0
1200	54	1-0.	-0.	3	-0	-0
1200	55	1 1.000-0.		4	-0	-0
0000	55	2 1.000-0.		4	-0	-0
0000	55	3 1.000-0.		4	-0	-0
0000	55	4 1.000-0.		4	-0	-0
0000	55	5 1.000-0.		4	-0	-0
0000	55	6 1.000-0.		4	-0	-0
0000	55	7 1.000-0.		4	-0	-0
0000	55	8 1.000-0.		4	-0	-0
0000	55	9 1.000-0.		4	-0	-0
0000	55	10 1.000-0.		4	-0	-0
0000	55	11 1.000-0.		4	-0	-0
0000	55	12 1.000-0.		4	-0	-0
0000	55	13 1.000-0.		4	-0	-0
0000	55	14 1.000-0.		4	-0	-0
0000	55	15 1.000-0.		4	-0	-0
0000	55	16 1.000-0.		4	-0	-0
2000	55	17 1.000-0.		4	-0	1

THIS ENDS DATA CARDS

NO SPACE-CHARGE - LAPLACE SOLUTION

ITERATION NO./POINT/ERROR/EPSILON 45 731 25.775817 0.310000

ARC,DELTA ARC LENGTH 0.13524 0.01424

X,Y-EMITTER	1 (0.060,0.044)	2 (0.050,0.052)	3 (0.040,0.062)	4 (0.030,0.074)	5 (0.014,0.100)	6 (0.005,0.120)	7 (-0.009,0.140)
	8 (0.,0.160)						
X,Y-BEGIN TRAJ.	1 (0.060,0.044)	2 (0.049,0.053)	3 (0.039,0.063)	4 (0.030,0.074)	5 (0.022,0.086)	6 (0.015,0.093)	7 (-0.009,0.111)
	8 (0.005,0.125)	9 (0.002,0.139)	10 (0.001,0.153)	11 (0.,0.160)			

```

X,Y-EQUIPOTENTIAL
1 (0.054,0.) 2 (0.054,0.010) 3 (0.055,0.020) 4 (0.056,0.030) 5 (0.067,0.040) 6 (0.067,0.050) 7 (0.063,0.060)
8 (0.060,0.070) 9 (0.055,0.080) 10 (0.052,0.090) 11 (0.049,0.100) 12 (0.046,0.110) 13 (0.044,0.120) 14 (0.042,0.130)
15 (0.041,0.140) 16 (0.040,0.150) 17 (0.040,0.160) 18 (0.,0.170)
X1=.431E-01 X2=.416E-01 Y1=.124E-03 Y2=.134E-03 DX=.368E-01 CD=C.1602E-01 -1 7
X1=.416E-01 X2=.405E-01 Y1=.134E-03 Y2=.145E-03 DX=.382E-01 CD=C.1183E-01 -1 8
X1=.406E-01 X2=.401E-01 Y1=.145E-03 Y2=.155E-03 DX=.391E-01 CD=C.1120E-01 0 9
X1=.401E-01 X2=.400E-01 Y1=.155E-03 Y2=.160E-03 DX=.397E-01 CD=C.1076E-01 0 10
X1=.452E-01 X2=.431E-01 Y1=.113E-03 Y2=.124E-03 DX=.347E-01 CD=C.1494E-01 0 6
X1=.431E-01 X2=.416E-01 Y1=.124E-03 Y2=.134E-03 DX=.369E-01 CD=C.1202E-01 0 7
X1=.416E-01 X2=.405E-01 Y1=.134E-03 Y2=.145E-03 DX=.382E-01 CD=C.1183E-01 0 8
X1=.480E-01 X2=.452E-01 Y1=.102E-03 Y2=.113E-03 DX=.3223E-01 CD=C.1783E-01 0 5
X1=.557E-01 X2=.515E-01 Y1=.792E-03 Y2=.910E-03 DX=.2533E-01 CD=C.2179E-01 -1 3
X1=.515E-01 X2=.480E-01 Y1=.910E-03 Y2=.102E-03 DX=.291E-01 CD=C.2275E-01 0 4
X1=.608E-01 X2=.557E-01 Y1=.669E-01 Y2=.792E-01 DX=.207E-01 CD=C.5922E-01 -1 2
X1=.557E-01 X2=.515E-01 Y1=.792E-01 Y2=.910E-01 DX=.2533E-01 CD=C.179E-01 0 3
X1=.608E-01 X2=.557E-01 Y1=.669E-01 Y2=.792E-01 DX=.207E-01 CD=C.5222E-01 0 2
X1=.659E-01 X2=.608E-01 Y1=.526E-01 Y2=.669E-01 DX=.143E-01 CD=C.1134E-00 0 1

```

```

EMITTER CURRENT IN TUBES
1 0.113116E-02 2 0.4577765E-03 3 0.259828E-03 4 0.162916E-03 5 0.138455E-03 6 0.737875E-04 7 0.468289E-04
8 0.298514E-04 9 0.141851E-04 10 0.169591E-05
TOTAL EMMITTER CURRENT 0.228848E-02

```

C Y C L E NO. 1
 RHTEST= 0.01825 UTEST= 2034.5567

ITERATION NO./POINT/ERROR/EPSILON 45 731 22.747585 0.010600

X, Y-EQUIPOTENTIAL	1	2	3	4	5	6	7
X1 = 0.052, 0.	0.052, 0.010	(0.052, 0.020)	(0.054, 0.030)	(0.064, 0.040)	(0.063, 0.050)	(0.063, 0.060)	
X1 = 0.057, 0.070	0.054, 0.080	(0.051, 0.090)	(0.048, 0.100)	(0.046, 0.110)	(0.044, 0.120)	(0.044, 0.130)	
X1 = 0.041, 0.140	0.040, 0.150	(0.040, 0.160)	(0.040, 0.170)	(0.040, 0.180)	(0.040, 0.190)	(0.040, 0.200)	
X1 = .430E-01 X2 = .416E-01 Y1 = .124E-01 Y2 = .134E-01	DX = .368E-01 CD = .473E-02	DX = .368E-01 CD = .427E-02	DX = .383E-01 CD = .427E-02	DX = .392E-01 CD = C 4551E-02	DX = .397E-01 CD = C .3907E-02	DX = .346E-01 CD = C .5485E-02	
X1 = .416E-01 X2 = .407E-01 Y1 = .134E-01 Y2 = .145E-01	DX = .145E-01 DX = .155E-01	DX = .145E-01 DX = .155E-01	DX = .145E-01 DX = .155E-01				
X1 = .407E-01 X2 = .402E-01 Y1 = .145E-01 Y2 = .155E-01	DX = .155E-01 DX = .165E-01	DX = .155E-01 DX = .165E-01	DX = .155E-01 DX = .165E-01				
X1 = .402E-01 X2 = .400E-01 Y1 = .155E-01 Y2 = .165E-01	DX = .165E-01 DX = .175E-01	DX = .165E-01 DX = .175E-01	DX = .165E-01 DX = .175E-01				
X1 = .450E-01 X2 = .430E-01 Y1 = .113E-01 Y2 = .124E-01	DX = .124E-01 DX = .134E-01	DX = .124E-01 DX = .134E-01	DX = .124E-01 DX = .134E-01				
X1 = .430E-01 X2 = .416E-01 Y1 = .124E-01 Y2 = .134E-01	DX = .134E-01 DX = .145E-01	DX = .134E-01 DX = .145E-01	DX = .134E-01 DX = .145E-01				
X1 = .416E-01 X2 = .407E-01 Y1 = .134E-01 Y2 = .145E-01	DX = .145E-01 DX = .155E-01	DX = .145E-01 DX = .155E-01	DX = .145E-01 DX = .155E-01				
X1 = .407E-01 X2 = .400E-01 Y1 = .145E-01 Y2 = .155E-01	DX = .155E-01 DX = .165E-01	DX = .155E-01 DX = .165E-01	DX = .155E-01 DX = .165E-01				
X1 = .400E-01 X2 = .400E-01 Y1 = .155E-01 Y2 = .165E-01	DX = .165E-01 DX = .175E-01	DX = .165E-01 DX = .175E-01	DX = .165E-01 DX = .175E-01				
X1 = .510E-01 X2 = .477E-01 Y1 = .905E-01 Y2 = .102E-01	DX = .905E-01 DX = .102E-01	DX = .905E-01 DX = .102E-01	DX = .905E-01 DX = .102E-01				
X1 = .585E-01 X2 = .545E-01 Y1 = .642E-01 Y2 = .780E-01	DX = .642E-01 DX = .780E-01	DX = .642E-01 DX = .780E-01	DX = .642E-01 DX = .780E-01				
X1 = .545E-01 X2 = .510E-01 Y1 = .780E-01 Y2 = .905E-01	DX = .905E-01 DX = .102E-01	DX = .905E-01 DX = .102E-01	DX = .905E-01 DX = .102E-01				
X1 = .585E-01 X2 = .545E-01 Y1 = .642E-01 Y2 = .780E-01	DX = .642E-01 DX = .780E-01	DX = .642E-01 DX = .780E-01	DX = .642E-01 DX = .780E-01				
X1 = .630E-01 X2 = .585E-01 Y1 = .484E-01 Y2 = .642E-01	DX = .484E-01 DX = .642E-01	DX = .484E-01 DX = .642E-01	DX = .484E-01 DX = .642E-01				

EMITTER CURRENT IN TUBES

I 1 0.890361E-03 2 0.225737E-03 3 0.105797E-03 4 0.621034E-04 5 0.403966E-04 6 0.270904E-04 7 0.177497E-04
I 8 0.107913E-04 9 0.512949E-05 10 0.615666E-05 11 0.344E-02 12 0.046E-01 13 0.044E-01 14 0.044E-01
TOTAL EMMITTER CURRENT 0.138577E-02

CYCLE NO. 2

RHTEST= 0.C2004 UTEST= 2075.3603

ITERATION NO./POINT/ERROR/EPSILON 45 731 2.723059 0.010000

x,y-EQUIPOTENTIAL

x1=.052,0.	x2=.052,0.010)	y1=.052,0.323)	y2=.054,0.030)	5	(0.054,0.040)		
x1=(0.058,0.070)	x2=(0.055,0.080)	y1=(0.052,0.390)	y2=(0.049,0.100)	11	(0.049,0.110)		
x1=(0.041,0.140)	x2=(0.040,0.150)	y1=(0.040,0.160)	y2=(0.040,0.170)	17	(0.040,0.180)		
x1=.433E-01	x2=.418E-01	y1=.124E-00	y2=.134E-00	DX=.370E-01	CD=C.4542E-02	-1	7
x1=.418E-01	x2=.408E-01	y1=.134E-C0	y2=.145E-00	DX=.384E-01	CD=C.4138E-02	-1	8
x1=.408E-01	x2=.402E-01	y1=.145E-C0	y2=.155E-00	DX=.392E-01	CD=C.3936E-02	0	9
x1=.402E-01	x2=.400E-01	y1=.155E-00	y2=.160E-00	DX=.398E-01	CD=0.3802E-02	0	10
x1=.455E-01	x2=.433E-01	y1=.113E-00	y2=.124E-00	DX=.350E-01	CD=0.5190E-02	0	6
x1=.433E-01	x2=.418E-01	y1=.124E-00	y2=.134E-00	DX=.370E-01	CD=0.4542E-02	0	7
x1=.418E-01	x2=.408E-01	y1=.134E-00	y2=.145E-00	DX=.384E-01	CD=0.4138E-02	0	8
x1=.484E-C1	x2=.455E-01	y1=.102E-00	y2=.113E-00	DX=.327E-01	CD=0.6139E-02	0	5
x1=.556E-01	x2=.518E-01	y1=.791E-01	y2=.912E-01	DX=.253E-01	CD=C.1119E-01	-1	3
x1=.518E-01	x2=.484E-01	y1=.912E-01	y2=.102E-00	DX=.295E-01	CD=G.7804E-02	0	4
x1=.593E-01	x2=.555E-01	y1=.652E-01	y2=.791E-01	DX=.194E-01	CD=0.2546E-01	-1	2
x1=.556E-01	x2=.518E-01	y1=.791E-01	y2=.912E-01	DX=.253E-01	CD=0.1119E-01	0	3
x1=.593E-01	x2=.556E-01	y1=.652E-01	y2=.791E-01	DX=.194E-01	CD=C.2646E-01	0	2
x1=.631E-01	x2=.593E-01	y1=.485E-01	y2=.652E-01	DX=.107E-01	CD=0.7465E-01	0	1

EMITTER CURRENT IN TUBES

1 0.744461E-03 2 0.186523E-03 3 0.914853E-04 4 0.558937E-04 5 0.373450E-04
 8 0.104400E-C4 9 0.498402E-C5 10 0.599153E-06
 TOTAL Emitter Current 0.117439E-02

EMITTER CURRENT IN TUBES
 1 0.744461E-03 2 0.186523E-03 3 0.914853E-04 4 0.558937E-04 5 0.373450E-04
 8 0.104400E-C4 9 0.498402E-C5 10 0.599153E-06
 TOTAL Emitter Current 0.117439E-02

LAST CYCLE
RHTEST= 0.02101 UTEST= 2076.5208

ITERATION NO./POINT/ERROR/EPSILON 45 731 1.158253 0.010006

U-FIELD OF LAST CYCLE.

U-FIELD OF THIS CYCLE											
1	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
1	9	10	11	12	13	14	15	16	2100.000	2100.000	2100.000
1	17	0	0	0	0	0	0	0	0.0	0.0	0.0
1	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
2	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
2	17	0	0	0	0	0	0	0	0.0	0.0	0.0
3	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
3	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
3	17	0	0	0	0	0	0	0	0.0	0.0	0.0
4	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
4	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
4	17	0	0	0	0	0	0	0	0.0	0.0	0.0
5	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
5	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
5	17	0	0	0	0	0	0	0	0.0	0.0	0.0
6	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
6	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
6	17	0	0	0	0	0	0	0	0.0	0.0	0.0
7	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
7	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
7	17	0	0	0	0	0	0	0	0.0	0.0	0.0
8	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
8	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
8	17	0	0	0	0	0	0	0	0.0	0.0	0.0
9	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
9	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
9	17	0	0	0	0	0	0	0	0.0	0.0	0.0
10	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
10	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
10	17	0	0	0	0	0	0	0	0.0	0.0	0.0
11	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
11	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
11	17	0	0	0	0	0	0	0	0.0	0.0	0.0
12	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
12	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
12	17	0	0	0	0	0	0	0	0.0	0.0	0.0
13	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
13	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
13	17	0	0	0	0	0	0	0	0.0	0.0	0.0
14	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
14	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
14	17	0	0	0	0	0	0	0	0.0	0.0	0.0
15	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
15	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
15	17	0	0	0	0	0	0	0	0.0	0.0	0.0
16	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
16	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
16	17	0	0	0	0	0	0	0	0.0	0.0	0.0
17	1	2	3	4	5	6	7	8	2100.000	2100.000	2100.000
17	9	16	11	12	13	14	15	16	2100.000	2100.000	2100.000
17	17	0	0	0	0	0	0	0	0.0	0.0	0.0

EQUIPOT 2000.0 (0.03301, 0.12000)(0.23114, 0.13000)(0.04000, 0.09800)(0.04000, 0.09800)(0.04000, 0.09800)(0.04000, 0.09800)(0.04000, 0.09800)
 EQUIPOT 2000.0 (0.05128, 0.) (0.05133, 0.05100)(0.05152, 0.02600)(0.05219, 0.05219, 0.05219, 0.05219, 0.05219, 0.05219)
 EQUIPOT 2000.0 (0.05000, 0.03781)(0.06000, 0.05191)(0.06258, 0.04000)(0.06258, 0.04000)(0.06258, 0.04000)
 EQUIPOT 1500.0 (0.05771, 0.) (0.05798, 0.01000)(0.05911, 0.02000)(0.05911, 0.02000)(0.05911, 0.02000)
 EQUIPOT 1500.0 (0.0586, 0.04000)(0.08203, 0.04452)(0.08163, 0.05000)(0.08163, 0.05000)
 EQUIPOT 1500.0 (0.08464, 0.09000)(0.08837, 0.10000)(0.08793, 0.11000)(0.08793, 0.11000)
 EQUIPOT 1500.0 (0.0863, 0.15000)(0.08647, 0.16000)(0.08647, 0.16000)
 EQUIPOT 1000.0 (0.08879, 0.) (0.09942, 0.01000)(0.10000, 0.01331)(0.10111, 0.01331)
 EQUIPOT 1000.0 (0.10742, 0.05000)(0.11095, 0.02600)(0.11095, 0.02600)
 EQUIPOT 1000.0 (0.11959, 0.10000)(0.12000, 0.12244)(0.12132, 0.11600)(0.12132, 0.11600)
 EQUIPOT 1000.0 (0.12563, 0.15000)(0.12572, 0.16000)(0.12572, 0.16000)
 EQUIPOT 500.0 (0.11299, 0.15000)(0.11314, 0.01200)(0.11314, 0.01200)
 EQUIPOT 500.0 (0.1531, 0.05000)(0.1531, 0.05000)
 EQUIPOT 500.0 (0.1700, 0.10791)(0.15138, 0.11000)(0.15138, 0.11000)
 EQUIPOT 500.0 (0.1780, 0.14307)(0.17249, 0.15000)(0.17249, 0.16000)
 EQUIPOT 500.0 (0.4545, 0.09000)(0.45135, 0.10000)(0.45135, 0.10000)
 EQUIPOT 500.0 (0.42649, 0.04000)(0.42033, 0.05000)(0.42033, 0.05000)
 EQUIPOT 500.0 (0.43173, 0.03000)(0. , 0.)
 X,Y-EQUIPOTENTIAL
 1 (0.052, 0.) 2 (0.052, 0.010) 3 (0.052, 0.020) 4 (0.054, 0.030) 5 (0.064, 0.040) 6 (0.063, 0.050) 7 (0.061, 0.060)
 8 (0.059, 0.070) 9 (0.056, 0.080) 10 (0.052, 0.090) 11 (0.049, 0.100) 12 (0.046, 0.110) 13 (0.044, 0.120) 14 (0.042, 0.130)
 15 (0.041, 0.140) 16 (0.040, 0.150) 17 (0.040, 0.160) 18 (0.040, 0.170)
 X1=.433E-01 X2=.418E-01 Y1=.124E-00 Y2=.134E-00 DX=.373E-01 CD=.479E-02 -1 7
 X1=.433E-01 X2=.408E-01 Y1=.134E-00 Y2=.145E-00 DX=.384E-01 CD=.437E-02 -1 8
 X1=.408E-01 X2=.402E-01 Y1=.145E-00 Y2=.159E-00 DX=.392E-01 CD=.416E-02 0 9
 X1=.402E-01 X2=.400E-01 Y1=.159E-00 Y2=.165E-00 DX=.398E-01 CD=.432E-02 0 10
 X= 0.01000 NO. Y= VX VY
 X= 0.02000 NO. Y= VX VY
 X,Y-EQUIPOTENTIAL
 1 0. 1.00000E-04 0.
 2 0. 1.00000E-04 0.
 3 0. 1.00000E-04 0.
 4 0. 1.00000E-04 0.
 5 0. 1.00000E-04 0.
 6 0. 1.00000E-04 0.
 7 0. 1.00000E-04 0.
 8 0. 1.00000E-04 0.
 9 0. 1.00000E-04 0.
 10 0. 1.00000E-04 0.
 X1=.456E-01 X2=.433E-01 Y1=.113E-00 Y2=.124E-00 DX=.351E-01 CD=.545E-02 5
 X1=.433E-01 X2=.418E-01 Y1=.113E-00 Y2=.124E-00 DX=.351E-01 CD=.545E-02 5
 X1=.418E-01 X2=.418E-01 Y1=.124E-00 Y2=.145E-00 DX=.384E-01 CD=.437E-02 0 7
 X1=.418E-01 X2=.418E-01 Y1=.134E-00 Y2=.159E-00 DX=.394E-01 CD=.437E-02 0 8
 X1=.486E-01 X2=.456E-01 Y1=.103E-00 Y2=.113E-00 DX=.384E-01 CD=.437E-02 0 5
 X= 0.03000 NO. Y= VX VY
 1 0. 1.00000E-04 0.
 2 0. 1.00000E-04 0.
 3 0. 1.00000E-04 0.
 4 0. 1.00000E-04 0.
 5 0. 1.00000E-04 0.
 6 0. 1.00708E-05 0. 471565E-04 0. 233560E-04
 7 0. 1.15265E-06 0. 657917E-04 0. 26267E-04
 8 0. 1.28712E-06 0. 791215E-04 0. 23296E-04
 9 0. 141437E-06 0. 878511E-04 0. 122690E-04
 10 0. 153950E-06 0. 921179E-04 0. 555218E-03

5	0.908814E-01	0.631387E 04	0.396732E 04
6	0.105282E-00	0.870459E 04	0.380850E 04
7	0.118741E-00	0.102586E 05	0.340038E 04
8	0.131176E-00	0.113439E 05	0.258181E 04
9	0.142816E-00	0.120555E 05	0.151778E 04
10	0.154537E-00	0.124044E 05	0.724668E 03
X1=.559E-01 X2=.520E-01 Y1=.793E-01 Y2=.913E-01 DX=.256E-01 CD=0.1151E-01 -1 3			
X1=.520E-01 X2=.486E-01 Y1=.913E-01 Y2=.103E-00 DX=.297E-01 CD=0.8132E-02 0 4			
X = 0.04000	NO.	Y	VX
1	0.	1.000000E-04	0.
2	0.	1.000000E-04	0.
3	0.641055E-01	0.260289E 04	0.249603E 04
4	0.819782E-01	0.724445E 04	0.555226E 04
5	0.967159E-01	0.103477E 05	0.575376E 04
6	0.109439E-00	0.123603E 05	0.494791E 04
7	0.121900E-00	0.136814E 05	0.416133E 04
8	0.133435E-00	0.145942E 05	0.317650E 04
9	0.144111E-00	0.151921E 05	0.191169E 04
10	0.155106E-00	0.154868E 05	0.850775E 03
X1=.597E-01 X2=.559E-01 Y1=.656E-01 Y2=.793E-01 DX=.199E-01 CD=0.2048E-01 -1 2			
X1=.559E-01 X2=.520E-01 Y1=.793E-01 Y2=.913E-01 DX=.256E-01 CD=0.1151E-01 0 3			
X = 0.05000	NO.	Y	VX
1	0.	1.000000E-04	0.
2	0.541993E-01	0.322701E 04	0.379355E 04
3	0.736950E-01	0.838487E 04	0.804063E 04
4	0.889451E-01	0.120776E 05	0.780924E 04
5	0.101916E-00	0.143158E 05	0.707212E 04
6	0.113256E-00	0.159155E 05	0.584438E 04
7	0.124808E-00	0.170094E 05	0.476416E 04
8	0.135519E-00	0.177713E 05	0.356873E 04
9	0.145325E-00	0.182733E 05	0.214941E 04
10	0.155642E-00	0.185225E 05	0.954749E 03
X1=.597E-01 X2=.559E-01 Y1=.656E-01 Y2=.793E-01 DX=.199E-01 CD=0.2048E-01 0 2			
X = 0.06000	NO.	Y	VX
1	0.	1.000000E-04	0.
2	0.659549E-01	0.101424E 05	0.119230E 05
3	0.816731E-01	0.143271E 05	0.100793E 05
4	0.948744E-01	0.165126E 05	0.914295E 04
5	0.106558E-00	0.181445E 05	0.799633E 04
6	0.116755E-00	0.193960E 05	0.631262E 04
7	0.127486E-00	0.202802E 05	0.522155E 04
8	0.137442E-00	0.209070E 05	0.386914E 04
9	0.146458E-00	0.213243E 05	0.233556E 04
10	0.156144E-00	0.215331E 05	0.104274E 04
X1=.633E-01 X2=.597E-01 Y1=.488E-01 Y2=.656E-01 DX=.112E-01 CD=0.7223E-01 0 1			
X = 0.07000	NO.	Y	VX
1	0.585000E-01	0.122137E 05	0.177099E 05
2	0.751146E-01	0.171116E 05	0.130408E 05
3	0.879915E-01	0.191970E 05	0.111025E 05
4	0.100019E-00	0.206202E 05	0.996212E 04
5	0.110714E-00	0.218189E 05	0.861267E 04
6	0.119953E-00	0.227927E 05	0.697977E 04
7	0.129946E-00	0.234954E 05	0.554874E 04
8	0.139213E-00	0.240029E 05	0.408662E 04
9	0.147511E-00	0.243460E 05	0.247399E 04
10	0.156609E-00	0.245190E 05	0.109987E 04
X = 0.08000	NO.	Y	VX
1	0.697770E-01	0.187982E 05	0.172622E 05
2	0.817708E-01	0.225195E 05	0.133383E 05

		3	0.933111E-01	0.235417E 05	0.116329E 05
		4	0.104543E-00	0.244697E 05	0.104335E 05
		5	0.114447E-00	0.253449E 05	0.898992E 04
		6	0.122869E-00	0.260964E 05	0.727714E 04
		7	0.132201E-00	0.266440E 05	0.575972E 04
		8	0.140842E-00	0.270459E 05	0.422853E 04
		9	0.148487E-00	0.273257E 05	0.256876E 04
		10	0.157040E-00	0.274677E 05	0.113983E 04
X =	0.09000	NO.	Y	VX	VY
		1	0.774085E-01	0.249515E 05	0.151254E 05
		2	0.871033E-01	0.271582E 05	0.131526E 05
		3	0.979078E-01	0.275197E 05	0.118381E 05
		4	0.108554E-00	0.280930E 05	0.106529E 05
		5	0.117807E-00	0.287187E 05	0.917689E 04
		6	0.125525E-00	0.292947E 05	0.743302E 04
		7	0.134265E-00	0.297092E 05	0.536823E 04
		8	0.142337E-00	0.300210E 05	0.430259E 04
		9	0.149389E-00	0.302431E 05	0.252443E 04
		10	0.157438E-00	0.303594E 05	0.116577E 04
X =	0.10000	NO.	Y	VX	VY
		1	0.830877E-01	0.298761E 05	0.150126E 05
		2	0.915359E-01	0.312385E 05	0.127324E 05
		3	0.101934E-00	0.312082E 05	0.118069E 05
		4	0.112133E-00	0.315133E 05	0.106763E 05
		5	0.120838E-00	0.319381E 05	0.920860E 04
		6	0.127941E-00	0.323595E 05	0.746512E 04
		7	0.136149E-00	0.325691E 05	0.588797E 04
		8	0.143707E-00	0.329029E 05	0.431614E 04
		9	0.150221E-00	0.330740E 05	0.264563E 04
		10	0.157808E-00	0.331693E 05	0.118049E 04
X =	0.11000	NO.	Y	VX	VY
		1	0.876128E-01	0.340898E 05	0.139324E 05
		2	0.952948E-01	0.350414E 05	0.121814E 05
		3	0.105486E-00	0.346704E 05	0.115903E 05
		4	0.115334E-00	0.347414E 05	0.105359E 05
		5	0.123574E-00	0.349924E 05	0.910587E 04
		6	0.130136E-00	0.352982E 05	0.738593E 04
		7	0.137868E-00	0.354998E 05	0.582951E 04
		8	0.144960E-00	0.356658E 05	0.427503E 04
		9	0.150988E-00	0.357922E 05	0.263643E 04
		10	0.158151E-00	0.358691E 05	0.118636E 04
X =	0.12000	NO.	Y	VX	VY
		1	0.913367E-01	0.379531E 05	0.128955E 05
		2	0.985101E-01	0.385556E 05	0.114820E 05
		3	0.108625E-00	0.379017E 05	0.111947E 05
		4	0.118201E-00	0.3777625E 05	0.102493E 05
		5	0.126043E-00	0.378532E 05	0.888057E 04
		6	0.132125E-00	0.380581E 05	0.720732E 04
		7	0.139433E-00	0.381709E 05	0.559906E 04
		8	0.146104E-00	0.382783E 05	0.418597E 04
		9	0.151694E-00	0.383657E 05	0.250024E 04
		10	0.158470E-00	0.384262E 05	0.118546E 04
X =	0.13000	NO.	Y	VX	VY
		1	0.944397E-01	0.415164E 05	0.117642E 05
		2	0.101258E-00	0.418174E 05	0.106329E 05
		3	0.111392E-00	0.409201E 05	0.106174E 05
		4	0.120763E-00	0.405677E 05	0.981618E 04
		5	0.128265E-00	0.405230E 05	0.853808E 04
		6	0.133923E-00	0.406213E 05	0.693575E 04

		7	0.140854E-00	0.406472E 05	0.550021E 04
		8	0.147147E-00	0.407031E 05	0.405520E 04
		9	0.152344E-00	0.407596E 05	0.254009E 04
		10	0.158768E-00	0.408027E 05	0.117976E 04
X=	0.14000	NO.	Y	VX	VY
		1	0.970124E-01	0.448398E 05	0.104526E 05
		2	0.103584E-00	0.449075E 05	0.957238E 04
		3	0.113807E-00	0.437374E 05	0.982768E 04
		4	0.123038E-00	0.431154E 05	0.922168E 04
		5	0.130257E-00	0.429247E 05	0.808049E 04
		6	0.135540E-00	0.429410E 05	0.657505E 04
		7	0.142140E-00	0.428872E 05	0.523731E 04
		8	0.148097E-00	0.428965E 05	0.388766E 04
		9	0.152941E-00	0.429279E 05	0.245953E 04
		10	0.159049E-00	0.429563E 05	0.117124E 04
X=	0.15000	NO.	Y	VX	VY
		1	0.990967E-01	0.479869E 05	0.889575E 04
		2	0.105514E-00	0.477426E 05	0.831038E 04
		3	0.115876E-00	0.462145E 05	0.877794E 04
		4	0.125039E-00	0.453394E 05	0.847716E 04
		5	0.132030E-00	0.450122E 05	0.751757E 04
		6	0.136985E-00	0.449610E 05	0.613282E 04
		7	0.143297E-00	0.448427E 05	0.492101E 04
		8	0.148961E-00	0.448129E 05	0.359155E 04
		9	0.153491E-00	0.448272E 05	0.236414E 04
		10	0.159315E-00	0.448436E 05	0.116207E 04
X=	0.16000	NO.	Y	VX	VY
		1	0.100681E-00	0.507042E 05	0.674019E 04
		2	0.107049E-00	0.500669E 05	0.659739E 04
		3	0.117603E-00	0.482192E 05	0.752850E 04
		4	0.126778E-00	0.471647E 05	0.750780E 04
		5	0.133600E-00	0.467302E 05	0.687850E 04
		6	0.138270E-00	0.455292E 05	0.553110E 04
		7	0.144337E-00	0.464707E 05	0.457246E 04
		8	0.149748E-00	0.464144E 05	0.348041E 04
		9	0.153998E-00	0.464205E 05	0.226254E 04
		10	0.159569E-00	0.464292E 05	0.115433E 04
X=	0.17000	NO.	Y	VX	VY
		1	0.101781E-00	0.518139E 05	0.453477E 04
		2	0.108205E-00	0.513350E 05	0.503087E 04
		3	0.119011E-00	0.496398E 05	0.625250E 04
		4	0.128269E-00	0.485085E 05	0.666310E 04
		5	0.134983E-00	0.480324E 05	0.623077E 04
		6	0.139407E-00	0.479188E 05	0.511676E 04
		7	0.145271E-00	0.477515E 05	0.422252E 04
		8	0.150465E-00	0.476870E 05	0.327265E 04
		9	0.154468E-00	0.476911E 05	0.216546E 04
		10	0.159813E-00	0.476974E 05	0.114964E 04
X=	0.18000	NO.	Y	VX	VY
		1	0.102493E-00	0.523983E 05	0.288636E 04
		2	0.109043E-00	0.520987E 05	0.363463E 04
		3	0.120141E-00	0.505977E 05	0.507802E 04
		4	0.129534E-00	0.495175E 05	0.573874E 04
		5	0.136202E-00	0.490264E 05	0.550223E 04
		6	0.140412E-00	0.488945E 05	0.451474E 04
		7	0.146111E-00	0.487214E 05	0.388884E 04
		8	0.151125E-00	0.486522E 05	0.307969E 04
		9	0.154909E-00	0.486552E 05	0.208019E 04
		10	0.159948E-00	0.486624E 05	-0.114861E 04

X=	0.19000	NO.	Y	VX	VY
X= 0.19000	NO.	1	0.102916E-00	0.527391E 05	0.156341E 04
		2	0.109626E-00	0.525816E 05	0.247109E 04
		3	0.121036E-00	0.512560E 05	0.403189E 04
		4	0.130598E-00	0.502626E 05	0.487841E 04
		5	0.137272E-00	0.497363E 05	0.496747E 04
		6	0.141298E-00	0.495828E 05	0.411752E 04
		7	0.145872E-00	0.494064E 05	0.357252E 04
		8	0.151735E-00	0.493351E 05	0.290426E 04
		9	0.155326E-00	0.493405E 05	0.200782E 04
		10	0.159714E-00	0.493486E 05	-0.115104E 04
X=	0.20000	NO.	Y	VX	VY
X= 0.20000	NO.	1	0.103107E-00	0.529386E 05	0.449992E 03
		2	0.110001E-00	0.528886E 05	0.148304E 04
		3	0.121730E-00	0.517123E 05	0.311339E 04
		4	0.131480E-00	0.508105E 05	0.403658E 04
		5	0.138200E-00	0.501972E 05	0.429871E 04
		6	0.142075E-00	0.500141E 05	0.361826E 04
		7	0.147562E-00	0.498409E 05	0.327884E 04
		8	0.152306E-00	0.497730E 05	0.275119E 04
		9	0.155725E-00	0.497818E 05	0.194886E 04
		10	0.159481E-00	0.497938E 05	-0.115622E 04
X=	0.21000	NO.	Y	VX	VY
X= 0.21000	NO.	1	0.103099E-00	0.530311E 05	-0.527079E 03
		2	0.110200E-00	0.530619E 05	0.624550E 03
		3	0.122252E-00	0.519975E 05	0.230240E 04
		4	0.132190E-00	0.511655E 05	0.320271E 04
		5	0.138984E-00	0.505617E 05	0.350629E 04
		6	0.142744E-00	0.503555E 05	0.309449E 04
		7	0.143187E-00	0.501259E 05	0.297259E 04
		8	0.152843E-00	0.500357E 05	0.250735E 04
		9	0.156111E-00	0.500440E 05	0.189906E 04
		10	0.159248E-00	0.500555E 05	-0.116399E 04
X=	0.22000	NO.	Y	VX	VY
X= 0.22000	NO.	1	0.102916E-00	0.530081E 05	-0.142300E 04
		2	0.110247E-00	0.531073E 05	-0.130681E 03
		3	0.122625E-00	0.521644E 05	0.158187E 04
		4	0.132739E-00	0.514200E 05	0.242575E 04
		5	0.139625E-00	0.508737E 05	0.289194E 04
		6	0.143294E-00	0.505940E 05	0.245746E 04
		7	0.148740E-00	0.502193E 05	0.257427E 04
		8	0.153349E-00	0.500993E 05	0.246323E 04
		9	0.156487E-00	0.501194E 05	0.186652E 04
		10	0.159015E-00	0.501413E 05	-0.117102E 04
X=	0.23000	NO.	Y	VX	VY
X= 0.23000	NO.	1	0.102576E-00	0.527755E 05	-0.216598E 04
		2	0.110163E-00	0.530321E 05	-0.754301E 03
		3	0.122868E-00	0.522395E 05	0.959324E 03
		4	0.133143E-00	0.515927E 05	0.173730E 04
		5	0.140117E-00	0.511092E 05	0.213201E 04
		6	0.143700E-00	0.507714E 05	0.155935E 04
		7	0.149203E-00	0.502997E 05	0.207918E 04
		8	0.153828E-00	0.501694E 05	0.233865E 04
		9	0.156858E-00	0.501953E 05	0.185720E 04
		10	0.158782E-00	0.502231E 05	-0.117371E 04
X=	0.24000	NO.	Y	VX	VY
X= 0.24000	NO.	1	0.102112E-00	0.525895E 05	-0.272836E 04
		2	0.109975E-00	0.529462E 05	-0.123872E 04
		3	0.123001E-00	0.522751E 05	0.431592E 03

		4	0.133421E-00	0.517134E 05	0.113202E 04
		5	0.140460E-00	0.512350E 05	0.137900E 04
		6	0.143943E-00	0.509641E 05	0.815035E 03
		7	0.149566E-00	0.505194E 05	0.157542E 04
		8	0.154283E-00	0.503787E 05	0.223700E 04
		9	0.157226E-00	0.503955E 05	0.134651E 04
		10	0.158548E-00	0.504168E 05	-0.117921E 04
X =	0.25000	NO.	Y	VX	VY
		1	0.101546E-00	0.524908E 05	-0.321973E 04
		2	0.109704E-00	0.528945E 05	-0.153760E 04
		3	0.123040E-00	0.523027E 05	-0.208384E 02
		4	0.133590E-00	0.518214E 05	0.611741E 03
		5	0.140666E-00	0.514693E 05	0.735698E 03
		6	0.144033E-00	0.512257E 05	0.998833E 02
		7	0.149831E-00	0.509109E 05	0.111990E 04
		8	0.154710E-00	0.506955E 05	0.207357E 04
		9	0.157585E-00	0.505586E 05	0.178337E 04
		10	0.158310E-00	0.506609E 05	-0.122163E 04
X =	0.26000	NO.	Y	VX	VY
		1	0.100886E-00	0.524828E 05	-0.370433E 04
		2	0.109359E-00	0.528880E 05	-0.200254E 04
		3	0.122998E-00	0.523234E 05	-0.425127E 03
		4	0.133665E-00	0.518940E 05	0.171932E 03
		5	0.140762E-00	0.516050E 05	0.251782E 03
		6	0.144003E-00	0.514327E 05	-0.408118E 03
		7	0.150010E-00	0.512459E 05	0.703766E 03
		8	0.155087E-00	0.509447E 05	0.176131E 04
		9	0.157923E-00	0.508561E 05	0.154699E 04
		10	0.158058E-00	0.508506E 05	-0.133667E 04
X =	0.27000	NO.	Y	VX	VY
		1	0.100131E-00	0.525433E 05	-0.422774E 04
		2	0.108945E-00	0.529119E 05	-0.237934E 04
		3	0.122879E-00	0.523204E 05	-0.818151E 03
		4	0.133659E-00	0.518884E 05	-0.231533E 03
		5	0.140772E-00	0.516036E 05	-0.150814E 03
		6	0.143884E-00	0.514347E 05	-0.809903E 03
		7	0.150138E-00	0.512544E 05	0.303120E 03
		8	0.155395E-00	0.509523E 05	0.137922E 04
		9	0.158232E-00	0.508632E 05	0.149251E 04
		10	0.157779E-00	0.508577E 05	-0.150398E 04
X =	0.28000	NO.	Y	VX	VY
		1	0.992695E-01	0.526365E 05	-0.483189E 04
		2	0.108455E-00	0.529375E 05	-0.280525E 04
		3	0.122682E-00	0.522760E 05	-0.123758E 04
		4	0.133573E-00	0.517922E 05	-0.651818E 03
		5	0.140698E-00	0.514562E 05	-0.611814E 03
		6	0.143680E-00	0.512339E 05	-0.128672E 04
		7	0.150128E-00	0.509459E 05	-0.101208E 03
		8	0.155637E-00	0.507222E 05	0.108233E 04
		9	0.158515E-00	0.506751E 05	0.138324E 04
		10	0.157468E-00	0.505584E 05	-0.155831E 04
X =	0.29000	NO.	Y	VX	VY
		1	0.982884E-01	0.525697E 05	-0.549979E 04
		2	0.107879E-00	0.529188E 05	-0.329739E 04
		3	0.122401E-00	0.521758E 05	-0.170626E 04
		4	0.133397E-00	0.515233E 05	-0.115844E 04
		5	0.140520E-00	0.512228E 05	-0.120850E 04
		6	0.143365E-00	0.509409E 05	-0.193420E 04
		7	0.150067E-00	0.505220E 05	-0.517127E 03

			8	0.155837E-00	0.504015E 05	0.941509E 03
			9	0.158784E-00	0.504083E 05	0.133653E 04
			10	0.157131E-00	0.503664E 05	-0.174365E 04
X =	0.30000	NO.		Y	VX	VY
		1	0.971780E-01	0.526118E 05	-0.619067E 04	
		2	0.107203E-00	0.528215E 05	-0.385300E 04	
		3	0.122023E-00	0.520057E 05	-0.222622E 04	
		4	0.133118E-00	0.513975E 05	-0.172111E 04	
		5	0.140217E-00	0.509554E 05	-0.139588E 04	
		6	0.142910E-00	0.506663E 05	-0.268340E 04	
		7	0.149923E-00	0.502312E 05	-0.936187E 03	
		8	0.156021E-00	0.501439E 05	0.905853E 03	
		9	0.159049E-00	0.501680E 05	0.132656E 04	
		10	0.156781E-00	0.501146E 05	-0.176856E 04	
X =	0.31000	NO.		Y	VX	VY
		1	0.959300E-01	0.524456E 05	-0.692083E 04	
		2	0.106414E-00	0.526153E 05	-0.446056E 04	
		3	0.121540E-00	0.517538E 05	-0.278443E 04	
		4	0.132722E-00	0.511087E 05	-0.233095E 04	
		5	0.139777E-00	0.506379E 05	-0.257374E 04	
		6	0.142309E-00	0.503841E 05	-0.339083E 04	
		7	0.149697E-00	0.500552E 05	-0.132191E 04	
		8	0.156201E-00	0.499719E 05	0.896017E 03	
		9	0.159314E-00	0.499968E 05	0.132446E 04	
		10	0.155427E-00	0.499425E 05	-0.177709E 04	
X =	0.32000	NO.		Y	VX	VY
		1	0.945290E-01	0.521043E 05	-0.772702E 04	
		2	0.105503E-00	0.522604E 05	-0.509124E 04	
		3	0.120945E-00	0.514055E 05	-0.335639E 04	
		4	0.132203E-00	0.507613E 05	-0.295692E 04	
		5	0.139206E-00	0.502924E 05	-0.318546E 04	
		6	0.141575E-00	0.500734E 05	-0.398468E 04	
		7	0.149402E-00	0.498852E 05	-0.153558E 04	
		8	0.156379E-00	0.498073E 05	0.885903E 03	
		9	0.159579E-00	0.498309E 05	0.132301E 04	
		10	0.156070E-00	0.497779E 05	-0.178744E 04	
X =	0.33000	NO.		Y	VX	VY
		1	0.929637E-01	0.513418E 05	-0.846457E 04	
		2	0.104468E-00	0.517142E 05	-0.567437E 04	
		3	0.120235E-00	0.509603E 05	-0.391134E 04	
		4	0.131560E-00	0.503483E 05	-0.355079E 04	
		5	0.138518E-00	0.499306E 05	-0.370946E 04	
		6	0.140729E-00	0.497397E 05	-0.445900E 04	
		7	0.149050E-00	0.496952E 05	-0.136509E 04	
		8	0.156556E-00	0.496250E 05	0.871504E 03	
		9	0.159845E-00	0.496457E 05	0.132195E 04	
		10	0.155708E-00	0.495960E 05	-0.180447E 04	
X =	0.34000	NO.		Y	VX	VY
		1	0.912496E-01	0.505293E 05	-0.899716E 04	
		2	0.103317E-00	0.510817E 05	-0.615612E 04	
		3	0.119413E-00	0.504472E 05	-0.442378E 04	
		4	0.130799E-00	0.493905E 05	-0.407138E 04	
		5	0.137729E-00	0.495574E 05	-0.413792E 04	
		6	0.139792E-00	0.493912E 05	-0.483220E 04	
		7	0.148658E-00	0.494314E 05	-0.202530E 04	
		8	0.155731E-00	0.493759E 05	0.856489E 03	
		9	0.159888E-00	0.493985E 05	-0.132177E 04	
		10	0.155341E-00	0.493461E 05	-0.182433E 04	
X =	0.35000	NO.		Y	VX	VY

		1	0.894172E-01	0.497598E 05	-0.937983E 04
		2	0.102066E-00	0.504341E 05	-0.654588E 04
		3	0.118486E-00	0.499014E 05	-0.487985E 04
		4	0.129935E-00	0.494145E 05	-0.450661E 04
		5	0.136857E-00	0.491638E 05	-0.447609E 04
		6	0.138780E-00	0.490211E 05	-0.512719E 04
		7	0.148235E-00	0.491215E 05	-0.214165E 04
		8	0.156904E-00	0.49303E 05	0.846385E 03
		9	0.159620E-00	0.491053E 05	-0.132245E 04
		10	0.154969E-00	0.490491E 05	-0.183964E 04
X =	0.36000	NO.	Y	VX	VY
		1	0.874901E-01	0.490277E 05	-0.955750E 04
		2	0.100728E-00	0.497996E 05	-0.686614E 04
		3	0.117462E-00	0.493425E 05	-0.527789E 04
		4	0.128983E-00	0.489504E 05	-0.485758E 04
		5	0.135917E-00	0.487728E 05	-0.472949E 04
		6	0.137707E-00	0.486494E 05	-0.535281E 04
		7	0.147788E-00	0.487959E 05	-0.223139E 04
		8	0.157076E-00	0.487643E 05	0.840557E 03
		9	0.159350E-00	0.487907E 05	-0.132337E 04
		10	0.154591E-00	0.487318E 05	-0.185153E 04
X =	0.37000	NO.	Y	VX	VY
		1	0.854857E-01	0.483527E 05	-0.986186E 04
		2	0.993138E-01	0.491982E 05	-0.713304E 04
		3	0.116352E-00	0.488069E 05	-0.552534E 04
		4	0.127959E-00	0.485056E 05	-0.512945E 04
		5	0.134925E-00	0.483824E 05	-0.491039E 04
		6	0.136585E-00	0.482711E 05	-0.551766E 04
		7	0.147322E-00	0.484641E 05	-0.230219E 04
		8	0.157249E-00	0.484427E 05	0.837523E 03
		9	0.159077E-00	0.484701E 05	-0.132415E 04
		10	0.154209E-00	0.484089E 05	-0.186187E 04
X =	0.38000	NO.	Y	VX	VY
		1	0.834155E-01	0.477534E 05	-0.100342E 05
		2	0.978324E-01	0.486421E 05	-0.736122E 04
		3	0.115162E-00	0.483110E 05	-0.592492E 04
		4	0.126875E-00	0.480910E 05	-0.533619E 04
		5	0.133892E-00	0.480091E 05	-0.503970E 04
		6	0.135426E-00	0.479050E 05	-0.553517E 04
		7	0.146840E-00	0.481385E 05	-0.235382E 04
		8	0.157422E-00	0.481271E 05	0.836429E 03
		9	0.158803E-00	0.481551E 05	-0.132454E 04
		10	0.153822E-00	0.480921E 05	-0.186985E 04
X =	0.39000	NO.	Y	VX	VY
		1	0.812856E-01	0.472231E 05	-0.101947E 05
		2	0.962903E-01	0.481365E 05	-0.756306E 04
		3	0.113905E-00	0.478575E 05	-0.616751E 04
		4	0.125745E-00	0.477155E 05	-0.548876E 04
		5	0.132829E-00	0.476678E 05	-0.513606E 04
		6	0.134236E-00	0.475675E 05	-0.572089E 04
		7	0.146346E-00	0.478295E 05	-0.239031E 04
		8	0.157596E-00	0.478256E 05	0.836851E 03
		9	0.158527E-00	0.478542E 05	-0.132425E 04
		10	0.153432E-00	0.477893E 05	-0.187496E 04
X =	0.40000	NO.	Y	VX	VY
		1	0.791011E-01	0.467315E 05	-0.103292E 05
		2	0.946928E-01	0.476795E 05	-0.774337E 04
		3	0.112591E-00	0.474527E 05	-0.635433E 04
		4	0.124580E-00	0.473785E 05	-0.559445E 04

		5	0.131740E-00	0.473602E 05	-0.520656E 04
		6	0.133023E-00	0.472622E 05	-0.578488E 04
		7	0.145842E-00	0.475466E 05	-0.241694E 04
		8	0.157772E-00	0.475488E 05	0.838472E 03
		9	0.158250E-00	0.475776E 05	-0.132308E 04
		10	0.153038E-00	0.475112E 05	-0.187734E 04
X =	0.41000	NO.	Y	VX	VY
		1	0.768691E-01	0.462924E 05	-0.104343E 05
		2	0.930447E-01	0.472705E 05	-0.790524E 04
		3	0.111232E-00	0.471097E 05	-0.649728E 04
		4	0.123388E-00	0.470863E 05	-0.556484E 04
		5	0.130633E-00	0.470902E 05	-0.525509E 04
		6	0.131791E-00	0.469937E 05	-0.583036E 04
		7	0.145330E-00	0.472968E 05	-0.243596E 04
		8	0.157949E-00	0.473040E 05	0.840755E 03
		9	0.157971E-00	0.473330E 05	-0.132104E 04
		10	0.152642E-00	0.472655E 05	-0.187751E 04
X =	0.42000	NO.	Y	VX	VY
		1	0.745963E-01	0.459205E 05	-0.105238E 05
		2	0.913507E-01	0.469176E 05	-0.805089E 04
		3	0.109837E-00	0.468212E 05	-0.650166E 04
		4	0.122177E-00	0.468418E 05	-0.571109E 04
		5	0.129511E-00	0.468620E 05	-0.528590E 04
		6	0.130544E-00	0.467665E 05	-0.585996E 04
		7	0.144812E-00	0.470845E 05	-0.244907E 04
		8	0.158128E-00	0.470955E 05	0.843364E 03
		9	0.157692E-00	0.471246E 05	-0.131813E 04
		10	0.152244E-00	0.470562E 05	-0.187592E 04
X =	0.43000	NO.	Y	VX	VY
		1	0.722876E-01	0.456047E 05	-0.106065E 05
		2	0.895157E-01	0.465181E 05	-0.817686E 04
		3	0.108416E-00	0.465858E 05	-0.657154E 04
		4	0.120952E-00	0.466455E 05	-0.573805E 04
		5	0.128379E-00	0.466770E 05	-0.530251E 04
		6	0.129287E-00	0.465825E 05	-0.537628E 04
		7	0.144290E-00	0.469136E 05	-0.245782E 04
		8	0.158307E-00	0.469274E 05	0.846078E 03
		9	0.157412E-00	0.469566E 05	-0.131438E 04
		10	0.151845E-00	0.468875E 05	-0.187304E 04
X =	0.44000	NO.	Y	VX	VY
		1	0.699476E-01	0.453344E 05	-0.106735E 05
		2	0.878457E-01	0.463684E 05	-0.828172E 04
		3	0.106977E-00	0.464078E 05	-0.671513E 04
		4	0.119719E-00	0.464960E 05	-0.574893E 04
		5	0.127241E-00	0.465362E 05	-0.530746E 04
		6	0.128023E-00	0.464424E 05	-0.588129E 04
		7	0.143765E-00	0.467859E 05	-0.246303E 04
		8	0.158488E-00	0.468015E 05	0.848695E 03
		9	0.157132E-00	0.468308E 05	-0.130992E 04
		10	0.151445E-00	0.467614E 05	-0.186935E 04
X =	0.45000	NO.	Y	VX	VY
		1	0.675823E-01	0.451279E 05	-0.107236E 05
		2	0.860465E-01	0.461837E 05	-0.837102E 04
		3	0.105526E-00	0.462815E 05	-0.673702E 04
		4	0.118481E-00	0.463945E 05	-0.574671E 04
		5	0.126099E-00	0.464415E 05	-0.530304E 04
		6	0.126755E-00	0.463480E 05	-0.587704E 04
		7	0.143238E-00	0.467018E 05	-0.246524E 04
		8	0.158670E-00	0.467189E 05	0.851090E 03

		9	0.156853E-00	0.467481E 05	-0.130485E 04
		10	0.151046E-00	0.466785E 05	-0.138522E 04
X =	0.46000	NO.	Y	VX	VY
		1	0.651975E-01	0.449814E 05	-0.107657E 05
		2	0.842239E-01	0.460596E 05	-0.844103E 04
		3	0.104069E-00	0.462088E 05	-0.673908E 04
		4	0.117243E-00	0.463410E 05	-0.573388E 04
		5	0.124958E-00	0.463931E 05	-0.529181E 04
		6	0.125488E-00	0.462999E 05	-0.586598E 04
		7	0.142710E-00	0.466608E 05	-0.246470E 04
		8	0.158852E-00	0.466790E 05	0.853210E 03
		9	0.156574E-00	0.467083E 05	-0.129923E 04
		10	0.150646E-00	0.466386E 05	-0.186078E 04
X =	0.47000	NO.	Y	VX	VY
		1	0.627979E-01	0.448861E 05	-0.107982E 05
		2	0.823854E-01	0.459908E 05	-0.848220E 04
		3	0.102611E-00	0.461890E 05	-0.672642E 04
		4	0.116008E-00	0.463348E 05	-0.571299E 04
		5	0.123819E-00	0.463908E 05	-0.527552E 04
		6	0.124223E-00	0.462977E 05	-0.584991E 04
		7	0.142182E-00	0.466631E 05	-0.246189E 04
		8	0.159035E-00	0.466820E 05	0.855021E 03
		9	0.156297E-00	0.467113E 05	-0.129312E 04
		10	0.150248E-00	0.466416E 05	-0.185613E 04
X =	0.48000	NO.	Y	VX	VY
		1	0.603890E-01	0.448539E 05	-0.108187E 05
		2	0.805389E-01	0.459832E 05	-0.850056E 04
		3	0.101158E-00	0.462197E 05	-0.670340E 04
		4	0.114779E-00	0.463746E 05	-0.568620E 04
		5	0.122685E-00	0.464332E 05	-0.525529E 04
		6	0.122962E-00	0.463403E 05	-0.582992E 04
		7	0.141655E-00	0.467077E 05	-0.245747E 04
		8	0.159219E-00	0.467268E 05	0.856499E 03
		9	0.156021E-00	0.467551E 05	-0.128664E 04
		10	0.149851E-00	0.466866E 05	-0.185153E 04
X =	0.49000	NO.	Y	VX	VY
		1	0.579761E-01	0.448778E 05	-0.108324E 05
		2	0.785912E-01	0.460384E 05	-0.850290E 04
		3	0.997121E-01	0.462999E 05	-0.657283E 04
		4	0.113557E-00	0.464596E 05	-0.565581E 04
		5	0.121556E-00	0.465191E 05	-0.523232E 04
		6	0.121707E-00	0.4654254E 05	-0.530712E 04
		7	0.141130E-00	0.467935E 05	-0.245218E 04
		8	0.159432E-00	0.468121E 05	0.857627E 03
		9	0.155747E-00	0.468415E 05	-0.127993E 04
		10	0.149455E-00	0.467724E 05	-0.184731E 04
X =	0.50000	NO.	Y	VX	VY
		1	0.555636E-01	0.449628E 05	-0.108411E 05
		2	0.768480E-01	0.461470E 05	-0.848854E 04
		3	0.982767E-01	0.464266E 05	-0.653734E 04
		4	0.112345E-00	0.465871E 05	-0.552438E 04
		5	0.120436E-00	0.466457E 05	-0.520804E 04
		6	0.120461E-00	0.4655532E 05	-0.578287E 04
		7	0.140607E-00	0.469182E 05	-0.244678E 04
		8	0.159585E-00	0.469356E 05	0.858414E 03
		9	0.155474E-00	0.469651E 05	-0.127317E 04
		10	0.149061E-00	0.468955E 05	-0.134382E 04
X =	0.51000	NO.	Y	VX	VY
		1	0.531559E-01	0.451059E 05	-0.108449E 05

RH-FIELD OF LAST CYCLE											
RHS OF MATRIX EQUATION - SPACE-CHARGE DENSITY											
1	1	2	3	4	5	6	7	8	0*	0*	0*
1	9	10	11	12	13	14	15	16	0*	0*	0*
1	17	0	0	0	0	0	0	0	0*	0*	0*
2	1	2	3	4	5	6	7	8	0*	0*	0*
2	9	10	11	12	13	14	15	16	0*	0*	0*
2	17	0	0	0	0	0	0	0	0*	0*	0*
3	1	2	3	4	5	6	7	8	0*	0*	0*
3	9	10	11	12	13	14	15	16	0*	0*	0*
3	17	0	0	0	0	0	0	0	0*	0*	0*
4	1	2	3	4	5	6	7	8	0*	0*	0*
4	9	10	11	12	13	14	15	16	0*	0*	0*
4	17	0	0	0	0	0	0	0	0*	0*	0*
5	1	2	3	4	5	6	7	8	0*	0*	0*
5	9	10	11	12	13	14	15	16	0*	0*	0*
5	17	0	0	0	0	0	0	0	0*	0*	0*
6	1	2	3	4	5	6	7	8	0*	0*	0*
6	9	10	11	12	13	14	15	16	0*	0*	0*
6	17	0	0	0	0	0	0	0	0*	0*	0*
7	1	2	3	4	5	6	7	8	0*	0*	0*
7	9	10	11	12	13	14	15	16	0*	0*	0*
7	17	0	0	0	0	0	0	0	0*	0*	0*
8	1	2	3	4	5	6	7	8	0*	0*	0*
8	9	10	11	12	13	14	15	16	0*	0*	0*
8	17	0	0	0	0	0	0	0	0*	0*	0*

49	1	2	3	4	5	6	7	8	9.	0.342	0.628	0.637	0.664	1.041	1.762
49	9	10	11	12	13	14	15	16	0.	1.487	0.663	0.528	0.386	0.461	0.391
49	17	0	0	0	0	0	0	0	0.	0.355	0.	0.	0.	0.	0.
50	1	2	3	4	5	6	7	8	0.	0.367	0.476	0.531	0.232	0.475	1.283
50	9	10	11	12	13	14	15	16	0.	1.126	0.609	0.475	0.365	0.421	1.910
50	17	0	0	0	0	0	0	0	0.	0.254	0.	0.	0.	0.	0.
51	1	2	3	4	5	6	7	8	0.	0.328	0.532	0.745	0.002	1.657	1.947
51	9	10	11	12	13	14	15	16	0.	0.831	0.559	0.426	0.346	0.389	0.577
51	17	0	0	0	0	0	0	0	0.	0.053	0.	0.	0.	0.	0.
52	1	2	3	4	5	6	7	8	0.	0.343	0.482	0.516	0.364	0.492	1.780
52	9	10	11	12	13	14	15	16	0.	0.628	0.516	0.395	0.333	0.360	0.574
52	17	0	0	0	0	0	0	0	0.	0.252	0.	0.	0.	0.	0.
53	1	2	3	4	5	6	7	8	0.	0.259	0.259	0.557	0.130	0.632	0.817
53	9	10	11	12	13	14	15	16	0.	0.580	0.457	0.366	0.322	0.331	0.080
53	17	0	0	0	0	0	0	0	0.	0.349	0.	0.	0.	0.	0.
54	1	2	3	4	5	6	7	8	0.	0.523	0.757	0.166	1.598	0.251	1.121
54	9	10	11	12	13	14	15	16	0.	0.546	0.425	0.340	0.312	0.303	0.382
54	17	0	0	0	0	0	0	0	0.	0.045	0.	0.	0.	0.	0.
55	1	2	3	4	5	6	7	8	0.	0.	0.	0.	0.	0.	0.
55	9	10	11	12	13	14	15	16	0.	0.	0.	0.	0.	0.	0.
55	17	0	0	0	0	0	0	0	0.	0.	0.	0.	0.	0.	0.

EMITTER CURRENT IN TUBES
 1 0.722298E-03 2 0.186652E-03 3 0.940203E-04 4 0.582407E-04 5 0.391668E-04 6 0.27023E-04 7 0.179885E-04
 1 0.722298E-03 2 0.186652E-03 3 0.940203E-04 4 0.582407E-04 5 0.391668E-04 6 0.27023E-04 7 0.179885E-04
 8 0.110625E-04 9 0.527475E-05 10 0.634128E-06
 TOTAL Emitter Current 0.116032E-02
 END OF PROBLEM

III. COMPUTER PROGRAM FOR SPECTRAL RADIUS CALCULATION (XR-CALCULATION)

The subroutines used for these calculations are:

1. MAIN ONE

Same as before, but it calls MATIN only.

2. MATIN

Calculates the largest eigenvalue.

3. MATRIX

Same as before.

4. 7090 PLOTTING ROUTINES (Fortran II) for the CalComp Plotter (Stanford University Computation Center Library Program No. 157).

A. DATA INPUT

The Data Input for this calculation is the same as for the beam analysis program with an additional card at the end shown on page 50 of Data Output by arrow. This card indicates how many iterations (MIT = 100) to perform and whether the print-out for each iteration is required (KWR > 0).

B. DATA OUTPUT

The print-out of Data Output consists of the Data Input (pages 48 to 50) and then the ~~LOW~~ and HIGH eigenvalues for the first two iterations. The last two columns show the point numbers where the lowest and the highest eigenvalue, respectively, were found. At the end the square root mean value of XR is given (page 51).

DEFLECTING PLATES FOR ION ENGINE NO.1
NASA-LEWIS FOR F.KAVANAGH/S.JONES

08/02/65

NXF	NYF	NEM	NTJ	NDIM	NRL	NUL	NURLNCOOR	IDEC	NFUL	NCO	KRHX	KRHY
55	17	8	10	3	2	45	45	0	-1	14	2	17
0												

IXONSPANNPOTXNPOTY YAXS
 1 13 5 17 0.0

KRTN KRTX KRTY KRTX KRTY KRTX KRTY

1	2	17	VAT	VBT	SIZE	VA	VB	VC
2000.0000	500.0000	500.0000	2100.0000	-0.			8.0000	
HGH	XLOW	HSL	XLSL			VD		
-C.	C.08C0	-0.	-C.			20.0000		
AXX	BXX	CXX	DXX			XR		
C.28C0	C.3200	0.5400	0.5400			0.9804		
RC	EPSILON		XEMIT		MESH SIZE - H			
0.	0.01000000		0.13999999		0.01000000			
EPSNOT	XQM	ATOM	VTH		VTHX		VTHY	
.88540E-11	.95790E 08.13290E	03.

CATHODE COORDINATES

0.0600	0.0440	0.0500	0.0520	0.0400	0.0620
0.0250	0.0800	0.0140	0.1000	0.0060	0.1200
0.0020	0.1400	-0.	0.1600		

PRINT-OUT OF CYCLE NO.

-0	-0	-0	-0	-0	-0	-0	-0	-0	-0
----	----	----	----	----	----	----	----	----	----

VOLT-1	-2	-3	-4	-5	-6	-7
2100.0000	0.	0.	500.0000	2000.0000	1800.0000	1600.0000
1400.0000	1200.0000	1000.0000	800.0000	600.0000	400.0000	200.0000
100.0000	50.0000	-0.	-0.	-0.	-0.	-0.
-0.	-0.	-0.	-0.	-0.	-0.	-0.

BOUNDARY POINTS OF ELECTRODE SHAPE

1000	2	12-0.100 0.200	1	-0	-0
0000	2	13-0.400-0.	1	-0	-0
0000	2	14-0.650-0.	1	-0	-0
0000	2	15-0.800-0.	1	-0	-0
0000	2	16-0.950-0.	1	-0	-0
2000	2	17-1.000-0.	1	-0	-0
1000	3	10-C.150 0.300	1	-0	-0
0000	3	11-0.700-0.	1	-0	-0
1000	4	9-0.500 0.700	1	-0	-0
1000	5	8-C.750 0.800	1	-0	-0
1000	6	7-0.900 0.800	1	-0	-0
1230	7	1-C. -0.	1	-0	-0
0300	7	2-C. -0.	1	-0	-0
0300	7	3-C. -0.	1	-0	-0
2300	7	4-0. -1.000	1	-0	-0
1000	7	6-C.700 0.500	1	-0	-0
1200	8	1-C. -0.	1	-0	-0
1200	9	1-C. -C.	1	-0	-0
1200	10	1-C. -0.	7	-0	-0
1200	11	1-C. -0.	9	-0	-0
1200	12	1-C. -0.	11	-0	-0
1200	13	1-C. -0.	13	-0	-0
1200	14	1-C. -0.	2	-0	-0

1200	15	1-0.	-0.	2	-0	-0
1200	16	1	1.000-0.	2	-0	-0
0000	16	2	1.000-0.	2	-0	-0
0000	16	3	1.000-0.	2	-0	-0
0000	16	4	1.000-0.	2	-0	-0
0000	16	5	1.000-0.	2	-0	-0
0000	16	6	1.000-0.	2	-0	-0
0000	16	7	1.000-0.	2	-0	-0
0000	16	8	1.000-0.	2	-0	-0
0000	16	9	1.000-0.	2	-0	-0
0000	16	10	1.000-0.	2	-0	-0
1000	17	11-0.	1.000	2	-0	-0
1000	18	11-0.	1.000	2	-0	-0
1000	19	11-0.	1.000	2	-0	-0
1000	20	11-0.	1.000	2	-0	-0
1000	21	11-0.	1.000	2	-0	-0
1000	22	11-0.	1.000	2	-0	-0
1000	23	11-0.	1.000	2	-0	-0
1200	24	1-1.000-0.		2	-0	-0
0000	24	2-1.000-0.		2	-0	-0
0000	24	3-1.000-0.		2	-0	-0
0000	24	4-1.000-0.		2	-0	-0
0000	24	5-1.000-0.		2	-0	-0
0000	24	6-1.000-0.		2	-0	-0
0000	24	7-1.000-0.		2	-0	-0
0000	24	8-1.000-0.		2	-0	-0
0000	24	9-1.000-0.		2	-0	-0
0000	24	10-1.000-0.		2	-0	-0
1200	25	1-0.	-0.	2	-0	-0
1200	26	1-0.	-0.	2	-0	-0
1200	27	1-0.	-0.	3	-0	-0
1200	28	1	1.000-0.	3	-0	-0
0000	28	2	1.000-0.	3	-0	-0
0000	28	3	1.000-0.	3	-0	-0
0000	28	4	1.000-0.	3	-0	-0
0000	28	5	1.000-0.	3	-0	-0
0000	28	6	1.000-0.	3	-0	-0
0000	28	7	1.000-0.	3	-0	-0
0000	28	8	1.000-0.	3	-0	-0
0000	28	9	1.000-0.	3	-0	-0
1000	29	10-C.	1.000	3	-0	-0
1000	30	10-C.	1.000	3	-0	-0
1000	31	10-C.	1.000	3	-0	-0
1000	32	10-C.	1.000	3	-0	-0
1000	33	10-0.	1.000	3	-0	-0
1200	34	1-1.000-0.		3	-0	-0
0000	34	2-1.000-0.		3	-0	-0
0000	34	3-1.000-0.		3	-0	-0
0000	34	4-1.000-0.		3	-0	-0
0000	34	5-1.000-0.		3	-0	-0
0000	34	6-1.000-0.		3	-0	-0
0000	34	7-1.000-0.		3	-0	-0
0000	34	8-1.000-0.		3	-0	-0
0000	34	9-1.000-0.		3	-0	-0
1200	35	1-0.	-0.	3	-0	-0
1200	36	1-0.	-0.	3	-0	-0
1200	37	1-0.	-0.	3	-0	-0
1200	38	1-0.	-0.	3	-0	-0
1200	39	1-0.	-0.	3	-0	-0
1200	40	1-C.	-0.	3	-0	-0

1200	41	1-C.	-C.	3	-C	-0
1200	42	1-C.	-0.	3	-0	-0
1200	43	1-C.	-0.	3	-0	-0
1200	44	1-C.	-0.	3	-0	-0
1200	45	1-C.	-0.	3	-0	-0
1200	46	1-C.	-0.	3	-0	-0
1200	47	1-C.	-0.	3	-0	-0
1200	48	1-C.	-0.	3	-0	-0
1200	49	1-C.	-0.	3	-0	-0
1200	50	1-C.	-0.	3	-0	-0
1200	51	1-C.	-0.	3	-0	-0
1200	52	1-C.	-0.	3	-0	-0
1200	53	1-C.	-0.	3	-0	-0
1200	54	1-C.	-0.	3	-0	-0
1200	55	1 1.000-C.		4	-0	-0
0000	55	2 1.000-C.		4	-0	-0
0000	55	3 1.000-C.		4	-0	-0
0000	55	4 1.000-C.		4	-0	-0
0000	55	5 1.000-C.		4	-0	-0
0000	55	6 1.000-C.		4	-0	-0
0000	55	7 1.000-C.		4	-0	-0
0000	55	8 1.000-C.		4	-0	-0
0000	55	9 1.000-C.		4	-0	-0
0000	55	10 1.000-C.		4	-0	-0
0000	55	11 1.000-C.		4	-0	-0
0000	55	12 1.000-C.		4	-0	-0
0000	55	13 1.000-C.		4	-0	-0
0000	55	14 1.000-C.		4	-0	-0
0000	55	15 1.000-C.		4	-0	-0
0000	55	16 1.000-C.		4	-0	-0
2000	55	17 1.000-C.		4	-0	1

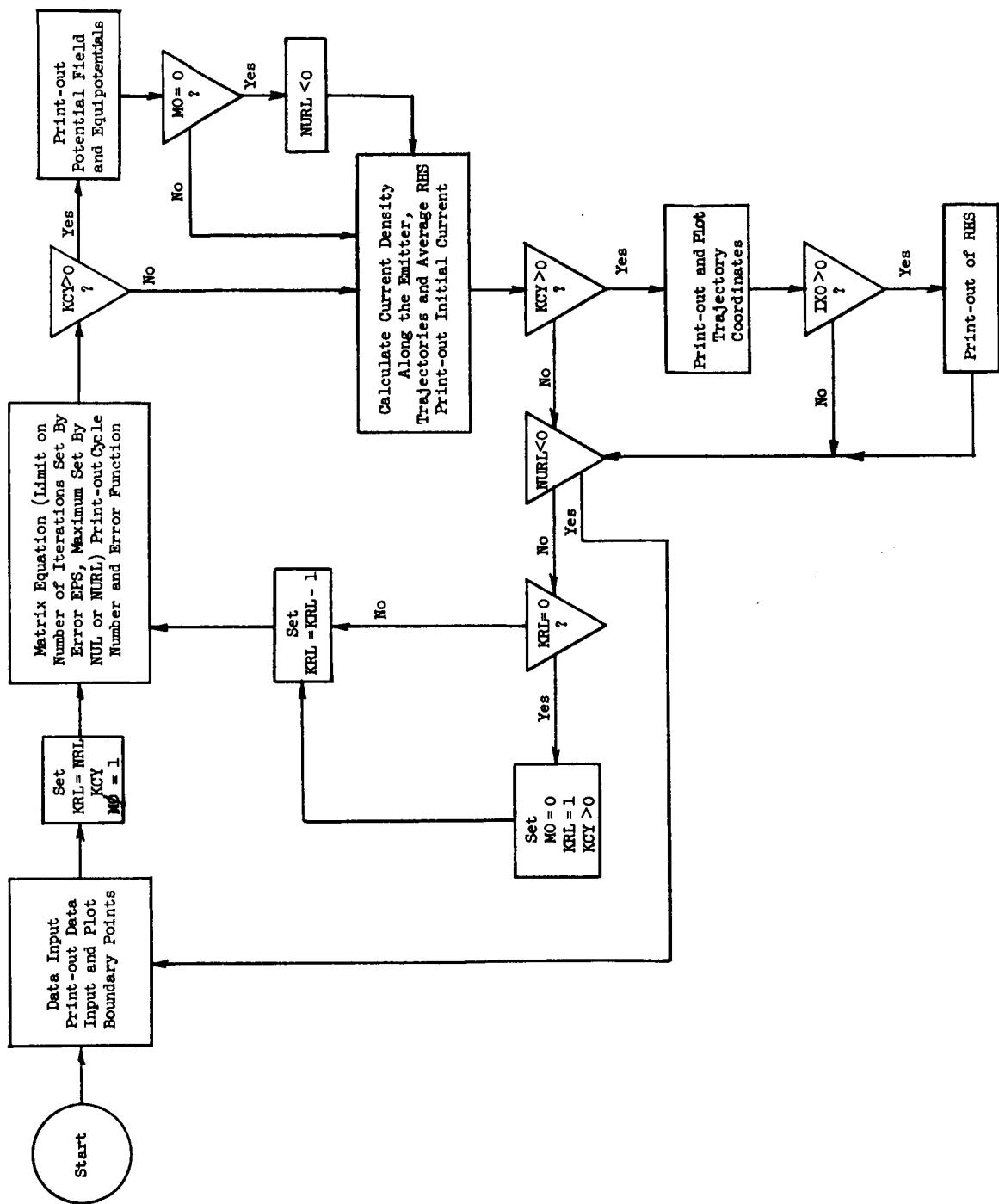
→ 100 1

LOW	HIGH	2	0.06241877	0.99999999	29	154
LOW	HIGH	4	0.53020603	0.99999996	29	188
LOW	HIGH	6	0.73457834	0.99999996	29	664
LOW	HIGH	8	0.75031348	0.99999996	392	701
LOW	HIGH	10	0.75074767	0.99999996	392	734
LOW	HIGH	12	0.75144236	0.99970973	392	731
LOW	HIGH	14	0.75244007	0.99916768	392	731
LOW	HIGH	16	0.75377956	0.99830127	392	731
LOW	HIGH	18	0.75550042	0.99719535	392	731
LOW	HIGH	20	0.75764639	0.99595493	392	731
LOW	HIGH	22	0.76026683	0.99466971	392	731
LOW	HIGH	24	0.76341622	0.99340408	392	731
LOW	HIGH	26	0.76715223	0.99219910	392	731
LOW	HIGH	28	0.77153189	0.99107761	392	731
LOW	HIGH	30	0.77660624	0.99006657	392	748
LOW	HIGH	32	0.78241381	0.98917856	392	748
LOW	HIGH	34	0.78897274	0.98837800	392	748
LOW	HIGH	36	0.79627310	0.98765965	392	748
LOW	HIGH	38	0.80426996	0.98701709	392	748
LOW	HIGH	40	0.81287961	0.98644357	392	748
LOW	HIGH	42	0.82197937	0.98593245	392	748
LOW	HIGH	44	0.83141293	0.98547738	392	748
LOW	HIGH	46	0.84100071	0.98507245	392	748
LOW	HIGH	48	0.85055389	0.98471230	392	748
LOW	HIGH	50	0.85989034	0.98439204	392	748
LOW	HIGH	52	0.86884899	0.98410731	392	748
LOW	HIGH	54	0.87730087	0.98385420	392	748
LOW	HIGH	56	0.88515513	0.98362923	392	748

LOW	HIGH	58	0.89235988	0.98342929	392	748
LOW	HIGH	60	0.89889881	0.98328237	392	782
LOW	HIGH	62	0.90478495	0.98315969	392	782
LOW	HIGH	64	0.91005322	0.98304868	392	782
LOW	HIGH	66	0.91475304	0.98294814	392	782
LOW	HIGH	68	0.91894164	0.98285712	392	782
LOW	HIGH	70	0.92267898	0.98277467	392	782
LOW	HIGH	72	0.92602389	0.98269998	392	782
LOW	HIGH	74	0.92903145	0.98263233	392	782
LOW	HIGH	76	0.93175158	0.98257105	392	782
LOW	HIGH	78	0.93422838	0.98252056	392	816
LOW	HIGH	80	0.93649992	0.98248880	392	816
LOW	HIGH	82	0.93859853	0.98245867	392	816
LOW	HIGH	84	0.94055128	0.98243012	392	816
LOW	HIGH	86	0.94238053	0.98240314	392	816
LOW	HIGH	88	0.94296780	0.98237771	323	816
LOW	HIGH	90	0.94326138	0.98236138	323	850
LOW	HIGH	92	0.94353233	0.98234868	306	850
LOW	HIGH	94	0.94372708	0.98233570	306	850
LOW	HIGH	96	0.94388814	0.98232382	289	884
LOW	HIGH	98	0.94401705	0.98231713	289	884
LOW	HIGH	100	0.94414704	0.98230983	289	918

XR=0.98144202

END OF PROBLEM



MAIN ONE -DATA INPUT

MAIN1

CSPACE-CHARGE SOLUTION.VLAQ HAMZA MICROWAVE LABORATORY.
COMMON URH,UR,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1 NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2 ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCODR,KCH,HSL,XLSL,EPN,PNOT,
3 IDEC,JUT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4 XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5 IXU,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6 VTHX,VTHY,YAXS,NFUL
DIMENSION KRT(2),JT(4000),RH(4000),
1 U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2 A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3 ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4 PTY(60)
DIMENSION ND(3),KRTX(10),KRTY(10),WOLT(28)
200 MO=1
READ INPUT TAPE 5,100,NH
DO 13 J=1,NH
READ INPUT TAPE 5,107
13 WRITE OUTPUT TAPE 6,107
READ INPUT TAPE 5,100,NXF,NYF,NEM,NTJ,NCIM,NRL,NUL,NURL,
INCOOR,IDECK,NFUL,NCO,KRHX,KRHY
JDY = NYF
WRITE OUTPUT TAPE 6,108
108 FORMAT(5HO NXF,5H NYF,5H NEM,5H NTJ,5H NDIM,5H NRL,5H NUL,
15H NURL,5HNCOOR,5H IDEC,5H NFUL,5H NCU,5H KRHX,5H KRHY)
WRITE OUTPUT TAPE 6,310,NXF,NYF,NEM,NTJ,NDIM,NRL,NUL,NURL,
1 NCOOR,IDECK,NFUL,NCU,KRHX,KRHY
READ INPUT TAPE 5,300,IXU,NSPAN,NPOTX,NPUTY,YAXS
WRITE OUTPUT TAPE 6,109
109 FORMAT(5HO IXO,5HNSPAN,5HNPUTX,5HNPUTY,8H YAXS)
WRITE OUTPUT TAPE 6,311,IXU,NSPAN,NPOTX,NPUTY,YAXS
READ INPUT TAPE 5,100,NRTN,(KRTX(K),KRTY(K),K=1,NRTN)
WRITE OUTPUT TAPE 6,110
110 FORMAT(5HOKRTN,5H KRTX,5H KRTY,5H KRTX,5H KRTY,5H KRTX,5H KRTY)
WRITE OUTPUT TAPE 6,310,NRTN,(KRTX(K),KRTY(K),K=1,NRTN)
READ INPUT TAPE 5,102,VAT,VBT,SIZE,VA,VB,VC
WRITE OUTPUT TAPE 6,111
111 FORMAT(4X3HVAT,7X3HVBT,6X4HSIZE,7X2HVA,8X2HVB,8X2HVC)
WRITE OUTPUT TAPE 6,302,VAT,VBT,SIZE,VA,VB,VC
READ INPUT TAPE 5,102,HGH,XLOW,HSL,XLSL,VD
WRITE OUTPUT TAPE 6,112
112 FORMAT(4X3HHGH,6X4HXLOW,6X3HHSL,7X4HXLSL,7X2HVD)
WRITE OUTPUT TAPE 6,302,HGH,XLOW,HSL,XLSL,VD
READ INPUT TAPE 5,102,AXX,BXX,CXX,DXX,XR
WRITE OUTPUT TAPE 6,113
113 FORMAT(4X3HAXX,7X3HBXX,7X3HCXX,7X3HDXX,7X2HXR)
WRITE OUTPUT TAPE 6,302,AXX,BXX,CXX,DXX,XR
READ INPUT TAPE 5,8,R0+EPS,XEMIT,H
WRITE OUTPUT TAPE 6,114
114 FORMAT(7X2HRO,10X7HEPSILON,9X5HXEMIT,6X13HMESH SIZE - H)
WRITE OUTPUT TAPE 6,308,R0,EPN,XEMIT,H
READ INPUT TAPE 5,105,YEP,XQM,ATOM,VTH,VTHX,VTHY
WRITE OUTPUT TAPE 6,115
115 FORMAT(12X6HFPSNUT,6X3HXQM,6X4HATOM,6X3HVTH,7X4HVTHX,6X4HVTHY)
WRITE OUTPUT TAPE 6,105,YEP,XQM,ATOM,VTH,VTHX,VTHY

MAIN ONE -DATA INPUT

MAIN1

```

      READ INPUT TAPE 5,102,(ATX(J),ATY(J),J=1,NEM)
      WRITE OUTPUT TAPE 6,119
119  FORMAT(31HO          CATHODE COORDINATES)
      WRITE OUTPUT TAPE 6,302,(ATX(J),ATY(J),J=1,NEM)
      READ INPUT TAPE 5,100,(KCY(J),J=1,10)
      WRITE OUTPUT TAPE 6,120
120  FORMAT(33HO          PRINT-OUT OF CYCLE NO.)
      WRITE OUTPUT TAPE 6,100,(KCY(J),J=1,10)
      READ INPUT TAPE 5,104,(WOLT(NN),NN=1,28)
      WRITE OUTPUT TAPE 6,116
116  FORMAT(8H0 VOLT-1,7X2H-2,8X2H-3,8X2H-4,8X2H-5,8X2H-6,8X2H-7)
      WRITE OUTPUT TAPE 6,304,(WOLT(NN),NN=1,28)                                E25
HH=H**2
HT=.5*H
H2=2.*H
XMPR=.5*(FLOATF(NXF*NYF))**2/FLOATF(NXF**2+NYF**2)
XQM=XQM/ATOM
RX = H/YEP
J=1
IF (NDIM-2) 1001,1001,2005
1001 DO 1002 I=1,NYF
      IF (I-1) 1006,1006,1007
1006   XT(J+3) = 0.0
      XT(J+5) = -0.5
      GO TO 1008
1007   IF (I-NYF) 1003,1005,1003
1005   XT(J+3) = -0.5
      XT(J+5) = 0.0
      GO TO 1008
1003   XT(J+3) = -0.25
      XT(J+5) = -0.25
1008   XT(J) = 0.25
      XT(J+1) = 0.25
      XT(J+2) = 0.25
      XT(J+4) = 1.0
1002   J = J+6
      GO TO 2011
2005 DO 2010 I=1,NYF
      RP= FLOATF(NYF-I)*H+RU
      IF (I-1) 1009,1009,1010
1009   XT(J+3) = 0.0
      XT(J+5) = -2.0*RP
      GO TO 1011
1010   IF (RP) 2009,2008,2009
2009   XT(J+5) = -(RP-HT)
      XT(J+3) = -(RP+HT)
1011   XT(J) = 1.0
      XT(J+1) = RP
      XT(J+2) = RP
      XT(J+4) = 4.0*RP
      GO TO 2010
2008 XT(J)= .125
      XT(J+1)=.125* H
      XT(J+2)=.125*H
      XT(J+3)=-.50 * H
      XT(J+4)=.75 *H

```

MAIN ONE -DATA INPUT

MAIN1

```

XT(J+5)=0.
2010   J = J + 6
2011 NOD = 1
      NSS=2
      NTRIP=0
      NPONT=NYF
      KRH=(KRHX-1)*NPONT+KRHY
      NTUP=NPONT*NXF
      KRT(1)=NRTN
      I=2
      DO 2 K=1,NRTN
      KRT(I)=(KRTX(K)-1)*NPONT+KRTY(K)
2  I=I+1
      KT(1)=-NPONT
      KT(2)=NPONT
      KT(3)=-1
      KT(4)=0
      KT(5)=+1
      WRITE OUTPUT TAPE 6,117
117    FORMAT(41HO      BOUNDARY POINTS OF ELECTRODE SHAPE )
      CALL PLOT (0.0,VC,-3)
      DO 2020 NX=1,NXF
      DO 2020 NY=1,NYF
      IF (NTRIP) 2030,2040,2030
2040 READ INPUT TAPE 5,2035,NS,(ND(I),I=1,3),NXC,NYC,HEW,HNS,NVOLT,
1     NVOLT1,NCHECK
2035  FORMAT (1H 4I1,2I4,2F6.3,2I5,I4)
      WRITE OUTPUT TAPE 6,2035,NS,(ND(I),I=1,3),NXC,NYC,HEW,HNS,NVOLT,
1     NVOLT1,NCHECK
      IF (HNS) 2031, 2032, 2031
2031  XXX=FLOATF(NXC-1)*H*VD
      YYY=-(FLOATF(NYC-1)-HNS)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
2032  IF (HEW) 2033, 2034, 2033
2033  XXX=(FLOATF(NXC-1)+HEW)*H*VD
      YYY=-FLOATF(NYC-1)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
      GO TO 2036
2034  IF (HNS) 2036, 2037, 2036
2037  XXX=FLOATF(NXC-1)*H*VD
      YYY=-FLOATF(NYC-1)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
2036  NTRIP = 1
      KC=  NPONT*(NXC-1)+NYC
2030 K=  NPONT*(NX-1)+NY
      IF (K-KC) 2060,2050,2060
2060 IF (NSS-1) 2070,2070,2080
2070 IF (NY-NYF) 2071,2072,2071
2072 NSS = 2
      JT(K) = 1 + 6*(NY-1)
      VOLT1= FLOATF((NXF-NX)/NXF)*VA
      GO TO 2310
2071 JT(K) = 1 + 6*(NY-1)
      GO TO 2020
2080 JT(K) = 9999
      IF (NX-NCO) 2081,2020,2020

```

71A

S77
S78
S79
S80
S81

MAIN ONE -DATA INPUT

MAIN1

```

2081 IF (U(K)) 2020,2084,2020
2084 U(K) = VA
GO TU 2020
2050 NTRIP = 0
NSS=NS
VOLT = WOLT(NVOLT)
VOLTI = WOLT(NVOLT1)
HEW = HEW*H
HNS=HNS*H
IF (ND(3)) 2052,2052,2053
2052 VOLTI = VOLT
2053 HN = H
HS = H
HE = H
HW = H
KE = K+NPONT
KW = K-NPONT
KN=K-1
KS=K+1
JT(K)=J
IF (HEW) 2090,2200,2100
2090 HW = - HEW
U(KW) = VOLT
GO TU 2200
2100 HE = HEW
U(KE) = VOLT
2200 IF (HNS) 2210,2230,2220
2210 HS = - HNS
U(KS) = VOLTI
GU TU 2230
2220 HN = HNS
U(KN) = VOLTI
2230 IF (NDIM-2) 1004,1004,2239
1004 XT(J) = ((HN+HS)*(HE+HW))/(16.*HH)
XT(J+1) = (HN+HS)/(8.*HW)
XT(J+2) = (HN+HS)/(8.*HE)
XT(J+3) = -(HE+HW)/(8.*HN)
XT(J+5) = -(HE+HW)/(8.*HS)
XT(J+4) = XT(J+1)+XT(J+2)-XT(J+3)-XT(J+5)
GO TO 2233
2239 RP= (FLOAT(NPONT-NY))*H+R0
IF(RP)2231,2232,2231
2231 XT(J)= (HE+HW)*(HN+HS)/(4.*HH)
XT(J+1)=((HN+HS)/(2.*HW))*(RP+((HN-HS)/4.))
XT(J+2)=HW*XT(J+1)/HE
XT(J+3)=-(HW+HE)/(2.*HN)*(RP+(HN/2.))
XT(J+5)=-(HW+HE)/(2.*HS)*(RP-(HS/2.))
XT(J+4)=XT(J+1)+XT(J+2)-XT(J+3)-XT(J+5)
GO TO 2233
134
2232 XT(J)= (HE+HW)*(HN/(16.*HH) )
XT(J+1)=(HN/(8.*HW) )*H
XT(J+2) = H* HN/(8.*HE)
XT(J+3) = - H*(HE+HW)/(4.*HN)
XT(J+4)=(HN/8.* ((HW+HE)/(HW*HE))+(HE+HW)/(4.*HN) )*H
XT(J+5)=0.
135A
2233 DO 2300 I=1,2
141A
141

```

MAIN ONE -DATA INPUT

MAIN1

```

NDA= NDA+1
GO TO 2300,2240,2250,2260,2270),NDA
2240 XT(J+1) = XT(J+1)+ XT(J+2)
XT(J+2) = 0.0
GO TO 2300
2250 XT(J+5) = XT(J+5) +XT(J+3)
XT(J+3) = 0.0
GO TO 2300
2260 XT(J+2) =XT(J+2) +XT(J+1)
XT(J+1) =0.0
GO TO 2300
2270 XT(J+3) =XT(J+3) +XT(J+5)
XT(J+5) =0.0
2300 CONTINUE
IF (ND(3)) 2310,2310,2311
2311 XT(J) = 0.25
XT(J+1) = 0.
XT(J+2) = XSL
XT(J+3) = 0.
XT(J+4) = 1.
XT(J+5) = XSL - 1.
2310 IF (NSS-1) 2320,2330,2340
2330 LINC1(NDD)=K
VUP = VOLTI
XT(J+3) =-XT(J+3)
GO TO 2320
2340 LINC2(NDD)=K
LINC (NDD)= 2*XMODF(NX,2) -1
VDOWN = VOLTI
KB=LINC1(NDD)
DO 2350 KK=KB,K
2350 U(KK)= VUP +(VDOWN-VUP)*FLOATF(KK-KB)/FLOATF(K-KB)
XT(J+5)= -XT(J+5)
NDD=NDD+1
2320 J = J + 6
2020 CONTINUE
NLIN=NDD-1
IF (NCHECK - 1) 4000,502,4000
4000 WRITE OUTPUT TAPE 6,4001
4001 FORMAT (24H0ERROR IN BOUNDARY POINT)
CALL EXIT
502 WRITE OUTPUT TAPE 6,118
118 FORMAT(20X20HTHIS ENDS DATA CARDS)
24 DO 6 J=1,NTOP
6 RH(J)=0.
NPUT=(NPOTX-1)*NPONT+NPOTY
IF(NCOORD) 10,10,11
11 DO 12 J=1,NEM
ETX(J)=ATX(J)
12 ETY(J)=ATY(J)
GO TO 15
10 DO 14 J=1,40
ETX(J)=0.
ETY(J)=0.
14 CONTINUE
15 KRL=NRL

```

MAIN ONE -DATA INPUT

```
C UCAL SOLVES THE MATRIX EQUATION
25      CALL UCAL
C MNTRI CALCULATES THE RHS AND TRAJECTORIES
26      CALL MNTRI
      GO TO 200
8 FORMAT (4F15.8)
100     FORMAT(14I5)
101     FORMAT(6I5)
102     FORMAT(6F10.4)
103     FORMAT(13I5)
104     FORMAT(7F10.4)
105     FORMAT(10X6E10.5)
106     FORMAT(3F10.5)
107     FORMAT(72H
1
300 FORMAT(4I5, F10.6)
302 FORMAT(1H 6F10.4)
304 FORMAT(1H 7F10.4)
308 FORMAT(1H 4F15.8)
310 FORMAT(1H 14I5)
311 FORMAT(1H 4I5, F10.6)
END(1,0,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

ARC CALCULATES THE BEGINNING TRAJECTORY COORDINATES

```

SUBROUTINE ARC
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1   NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2   ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPSS,NPOT,
3   IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4   XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5   IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6   VTHX,VTHY, YAXS, NFUL
DIMENSION KRT(2),JT(4000),RH(4000),
1   U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2   A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3   ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4   PTY(60)
SUM=0.
DO 1 J=2,NEM
1   SUM=SUM+SQRTF((ATX(J)-ATX(J-1))**2+(ATY(J)-ATY(J-1))**2)
IF (NFUL) 15,15,20
15 ARCL = FLOATF(NTJ) - 0.5
GO TO 30
20 ARCL = FLOATF(NTJ) - 1.0
30 ARCL=SUM/ARCL
ETX(1)=ATX(1)
ETY(1)=ATY(1)
HYP=ARCL
K=1
J=1
10 IF(K-NTJ)3,6,6
3   K=K+1
2   XDIF=ATX(J)-ATX(J+1)
   YDIF=ATY(J+1)-ATY(J)
   SA=SQRTF(XDIF**2+YDIF**2)
   IF(HYP-SA) 4,4,5
4   CSA=YDIF/SA
   SNA=XDIF/SA
   ETX(K)=ATX(J)-HYP*SNA
   ETY(K)=ATY(J)+HYP*CSA
   HYP=ARCL+HYP
   GO TO 10
5   HYP= HYP-SA
   J=J+1
   GO TO 2
6   K=K+1
   NN=NTJ + 1
   ETX(K)=ATX(NEM)
   ETY(K)=ATY(NEM)
7   WRITE OUTPUT TAPE 6,103,SUM,ARCL
   WRITE OUTPUT TAPE 6,100,(J,ATX(J),ATY(J),J=1,NEM)
   WRITE OUTPUT TAPE 6,102,(J,ETX(J),ETY(J),J=1,NN)
8   CONTINUE
100  FORMAT (12HOX,Y-EMITTER /(7(1H ,I2,2H (F5.3,1H,F5.3,2H) )))
102  FORMAT (16HOX,Y-BEGIN TRAJ. /(7(1H ,I2,2H (F5.3,1H,F5.3,2H) )))
103  FORMAT(22HOARC,DELTA ARC LENGTH 2F10.5)
      RETURN
END(1,0,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

CALR CALCULATES RHS

```

SUBROUTINE CALR(KE,KED)
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UR,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3  IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,VURL,NJOT,XEMIT,
5  IXD,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY, YAXS, NFUL
      DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
      JEX=KE
      JD=KED
      IF (NFUL) 500, 500, 60
500  XEP = FLOAT(NYF-1) * H
      GO TO 70
60  XEP = YAXS
70  DO 33 JJ=1,NAJ
      J=JJ
CIF CU(J)=0.,NO CONTRIBUTION
      IF(CU(J)) 33,33,1
1  IF(AY(J)+1.) 2,2,5
2  IF(AX(1)-BXX) 3,4,4
3  AY(J)=XLLOW
      GO TO 5
4  AY(J)=HGH
CIF CU(NAJ),LAST TUBE
5  IF(J-NAJ)9,6,33
6  IF(AY(JJ)) 7,8,8
7  AY(JJ) = - AY(JJ)
8  HT=(XEP-AY(JJ))
      RT1=HT
      XH=AY(JJ)
      RT2=0.
      YL=XH+HT
      JX=AY(JJ)/DELY
      NA=JX+JEX
      NB=JD
      TB1 = VY(JJ)/VX(JJ)
      DE = ATANF(TB1)
      DE = CUSF(DE)
      WA = VX(JJ)
      WB=WA
      GO TO 23
9  HT=AY(J+1)-AY(J)
      IF(HT)12,12,13
12  HT=-HT
      XH=AY(J+1)
      RT1=XEP-XH
CJX NORMALIZES Y-DISTANCES IN THE CELL
      JX=XH/DELY
      NB=AY(J)/DELY +1.

```

CALR CALCULATES RHS

```
    WA = VX(J+1)
    WB = VX(J)
    TB1=VY(J+1)/VX(J+1)
    TB2=VY(J)/VX(J)
    TBA = .5*(TB1+TB2)
    DE = ATANF(TBA)
    DE = COSF(DE)
    GO TO 14
13   XH=AY(J)
      RT1=XEP-XH
CJX NORMALIZES Y-DISTANCES
    JX=XH/DELY
      WA = VX(J)
      WB= VX(J+1)
    TB1=VY(J+1)/VX(J+1)
    TB2=VY(J)/VX(J)
    TBA = .5*(TB1+TB2)
    DE = ATANF(TBA)
    DE = COSF(DE)
    NB=AY(J+1)/DELY +1.
14   NA=JX*JEX
    NB=NB+JEX
    YL=XH+HT
      RT2=XEP-YL
23   DO 32 K=NA,NB
    XA=K-JEX
25   XUD=(XA-.5)*DELY
26   XX=XUD+DELY
    YU=MAX1F(XUD,XH)
    YD=MIN1F(XX,YL)
    IF(YD-YU)32,32,27
27   XA=.5*(YD+YU)
    W=WA+(XA-XH)*(WB-WA)/HT
CCALCULATION OF RHS
    IF(NDIM-2) 31,31,50
50   RH(K)=RH(K)+(YD-YU)*2.* (XEP-XA)*CU(JJ)/((HT*W*DE)*(RT1+RT2))
    GO TO 32
31   RH(K)=RH(K)+(YD-YU)*CU(JJ)/(HT*W *DE)
32   CONTINUE
33   CONTINUE
38   RETURN
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

CORRCT CONDITIONALLY ENDS TRAJECTORIES

```

SUBROUTINE CORRCT
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3  IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5  IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
XLOW1 = XLOW
XLOW2 = HGH
IF (AX(1) - AXX) 11,12,1
1  IF (AX(1) - BXX) 12,2,2
2  IF (AX(1) - CXX) 13,13,11
13 XLOW1 = XLOW2
12 DO 10 J=1,NTJ
    IF (AY(J) +1.) 10,10,5
5   IF (AY(J) - XLOW1) 6,10,10
C  CHECK ON THE NEXT TRAJECTORY
6   IF (AY(J+1) +1.) 9,9,4
4   IF (AY(J+1) - XLOW1) 9,9,3
3   AYD = AY(J+1) - AY(J)
    AYDS = AY(J+1) - XLOW1
    AYDL = AYD - AYDS
    CU(J) = CU(J) * AYDS/AYD
    VX(J) = (VX(J)*AYDL + VX(J+1)*AYDS)/AYD
    VY(J) = (VY(J)*AYDL + VY(J+1)*AYDS)/AYD
C  CHECK ON PREVIOUS TRAJECTORY (CASE 4)
14  IF (J-1) 14,14,7
7   IF (AY(J-1) - XLOW1) 14,8,8
8   AYDS = AY(J-1) - XLOW1
    AYD = XABSF (AY(J-1) - AY(J))
    AYDL = AYD - AYDS
    CU(J-1) = CU(J-1)*AYDS/AYD
14  AY(J) = XLOW1
    GO TO 10
9   CU(J) = 0.
    AY(J) = -1.
10  CONTINUE
11  RETURN
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

EQLINE SOLVES FOR THE EQUIPOENTIALS

```

SUBROUTINE EQLINE
CSpace-Charge Solution. VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH, UB, JT, RH, U, XT, KT, LINC, XR, NTOP, NUL, NLIN, ARCL, EQX, EQY,
1   NPIT, XEP, NXEP, CU, LINC1, AX, AY, VX, VY, DX, DELY, YEP, XQM, H, KISW, ETX,
2   ETY, PTY, PTX, NAJ, NTJ, VA, VB, VC, NCOOR, KCH, HSL, XSL, EPS, NPOT,
3   IDEC, JOT, NSPAN, RX, NRL, KRL, KRH, VAT, VBT, SIZE, KRT, RHUP, RDOWN,
4   XCU, NOT, MO, KCY, NSW, ATX, ATY, LINC2, NXF, NYF, NURL, NJOT, XEMIT,
5   IXO, HGH, XLOW, XMPR, NEM, A, X, JDY, AXX, BXX, CXX, DXX, NDIM, VD, VTH,
6   VTHX, VTHY
DIMENSION KRT(2), JT(4000), RH(4000),
1   U(4000), XT(4000), KT(5), LINC(150), LINC1(150), LINC2(150),
2   A(180), X(60), CU(40), VX(40), VY(40), KCH(40), AX(40), AY(40),
3   ATX(40), ATY(40), ETX(40), ETY(40), XCU(40), KCY(10), PTX(60),
4   PTY(60)
IF(SIZE) 1,27,1
1   POTEN=VAT
2   WRITE OUTPUT TAPE 6,101
2   JE= NYF + 1
3   JD = NYF - 1
3   JC= NXF-1
4   DX=1
4   DX=DX*H
4   BX=0.
4   JED=JE+JD
4   L=1
3   AX=C.
4   DO 22 JJ=1,JC
4   KS=1
5   AAY=0.
5   DO 19 K=JE,JED
6   IF(KS) 8,8,7
7   M=1
7   J=K-NYF
7   GO TO 9
8   J=K-1
9   IF ( JT(K)-9999+JT(J)-9999) 28,18,18
28  IF((U(K)-POTEN)*(U(J)-POTEN)) 10,10,18
10  DIF=ABSF(U(J)-U(K))
10  IF(DIF) 13,13,11
11  IF(M) 12,14,12
12  VX(L)=ABSF(U(J)-POTEN)/DIF*DX+AX
12  VY(L)=AAY
13  GO TO 15
13  VX(L)=AX+DX
13  VY(L)=AAY
13  GO TO 15
14  VX(L)=AX+DX
14  VY(L)= ABSF(U(J)-POTEN)/DIF*DX+AAY
15  IF(L-6) 17,16,16
16  WRITE OUTPUT TAPE 6,100,POTEN,(VX(I),VY(I),I=1,6)
16  L=0
17  L=L+1
18  AAY=AAY+DX
19  CONTINUE
19  IF(KS) 21,21,20

```

EQLINE SOLVES FOR THE EQUIPOTENTIALS

```
20      KS=C
      M=0
      JE=JE+1
      GO TO 5
21      JE=JE+JD
      JED=JE+JD
      BX=BX+DX
      AX=AX+DX
22      CONTINUE
      IF(L-2) 25,23,23
23      DO 24 J=L,6
      VX(J)=0.
24      VY(J)=0.
      WRITE OUTPUT TAPE 6,100,POTEN,(VX(I),VY(I),I=1,6)
25      POTEN=POTEN-SIZE
      IF(POTEN-VBT) 27,26,26
26      AX=AX-BX
      GO TO 2
27      RETURN
100   FORMAT(8H EQUIPOTF8.1,2H 6(1H(F8.5,1H,F8.5,1H)))
101   FORMAT(41HO X,Y-COORDINATE OF EQUIPOTENTIAL LINES. )
      END(1,1,0,0,0,1,0,0,0,0,0,0,0,0,0,0,0)
```

MATRIX IS USED FOR THE FORWARD AND BACK SUBSTITUTION

```
SUBROUTINE MATRIX(N,A,X)
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XSSL,EPS,NPOT,
3  IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XLU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5  IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY
      DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
M=3*N-2
A(M+1)=0.
A(2)=A(2)/A
X=X/A
      IF(N-1) 12,12,9
9   K=2
DO 10 J=4,M,3
A(J)=A(J)-A(J-1)*A(J-2)
A(J+1)=A(J+1)/A(J)
X(K)=(X(K)-A(J-1)*X(K-1))/A(J)
10  K=K+1
      K=K-1
DO 11 J=1,M,3
NB=M-J-1
K=K-1
11  X(K)=X(K)-A(NB)*X(K+1)
12  RETURN
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

MNTKI CALCULATES TRAJECTORIES AND RHS (FOR SOLID BEAM)

```

SUBROUTINE MNTKI
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UR,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1 NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISH,ETX,
2 ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XSL,EPS,NPOT,
3 IDEC,JDT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4 XCU,NOT,MN,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5 IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6 VTHX,VTHY, YAXS, NFUL
DIMENSION KRT(2),JT(4000),RH(4000),
1 U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2 A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3 ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4 PTY(60)
DIMENSION E1X(40),E1Y(40)
DELY=H
DX=DELY
301 IWRL=NRL-KRL+XABSF(M0)
DO 1 J=1,40
VY(J)=0.
VX(J)=.0001
AY(J)=0.
XCU(J)=0.
CU(J)=0.
CKCH=REFLECTION PARAMETER (ADDS ONE EVERYTIME TRAJECTORY REFLECTS)
1 KCH(J)=-1
DO 35 J=1,60
PTX(J)=0.
35 PTY(J)=0.
IF (KCY(IWRL)) 903,903,902
902 CALL PLOT (ATX(1)*VD,-ATY(1)*VD,3)
DO 901 J=2,NEM
901 CALL PLOT (ATX(J)*VD,-ATY(J)*VD,2)
903 NAJ=NTJ
IF (NCOOR) 2,2,3
CARC CALCULATES THE Emitter COORDINATES
2 CALL ARC
3 DO 909 J=1,NTJ
E1X(J) = ETX(J)
909 E1Y(J) = ETY(J)
NCOOR = 1
CPEQ CALCULATES THE EQUIPOTENTIAL LINE FOR CU CALCULATION
CALL PEQ
AX(1) = 0.
JCX=NXF-2
JEX=NYF+1
IF (NFUL) 50, 50, 60
50 XEP = FLOAT(NYF-1) * DX
GO TO 70
60 XEP = YAXS
70 DO 22 JN=1,JCX
400 JD=JEX+NYF-1
AX(1) = AX(1) + DX
CTRCU CALCULATES THE CURRENT IN THE TUBES AND CALLS TRAJ
CALL TRCU(JEX,JD)

```

MNTRI CALCULATES TRAJECTORIES AND RHS (FOR SOLID BEAM)

```

11    CONTINUE
      IF (KCY(IWRL)) 19,19,18
18    WRITE OUTPUT TAPE 6,101,AX(1),(K,AY(K),VX(K),VY(K),K=1,NTJ)
      XP = AX(1)
      DO 906 J=1,NTJ
      IF (AY(J)) 906,906,905
905    YP = AY(J)
      CALL PLOT (E1X(J)*VD,-E1Y(J)*VD,3)
      CALL PLOT (XP*VD,-YP*VD,2)
      E1X(J)=AX(1)
      E1Y(J) = AY(J)
906    CONTINUE
CCALR CALCULATES THE RHS
19    CALL CALR (JEX,JD)
22    JEX=JEX+NYF
      IF (KCY(IWRL)) 907,907,24
24    IF (IX0) 908,908,20
20    CALL TROUT
908    XMAX = FLOAT(NXF-1)*H*VD + 3.0
      S = XMAX - 3.0
      XMEN = ATX(NEM)*VD
      YMAX = - XEP*VD
      SDX = 1.0/VD
      CALL PLOT (XMAX, 0.0, -3)
      DO 910 J=1,NTJ
      E1X(J) = ETX(J)
910    E1Y(J) = ETY(J)
907    SUM = 0.0
      DO 10 J=1,NAJ
10    SUM=SUM+XCU(J)
305    WRITE OUTPUT TAPE 6,102,(J,XCU(J),J=1,NAJ)
      WRITE OUTPUT TAPE 6,103,SUM
304    IF(NURL)303,303,302
302    IF (NRL-KRL) 306,307,306
307    WW = SQRTF(2.*XQM*(VA-VB))
      RHM = 2.*SUM/WW
306    DO 4 J=1,NTOP
      RH(J) = .5*RH(J)
      IF (RHM-RH(J)) 5,4,4
5     RH(J) = RHM
4     CONTINUE
      IF (KRL) 8,7,8
7     MO=0
      KRL=1
      JJ=NRL
      KCY(JJ)= 777
      WRITE OUTPUT TAPE 6,100
      GO TO 9
8     WRITE OUTPUT TAPE 6,104,IWRL
9     RT=RH(KRH)*RX
      WRITE OUTPUT TAPE 6,105,RT,U(KRH)
21    KRL=KRL-1
CUCAL SOLVES THE MATRIX EQUATION
      CALL UCAL
      GO TO 301
303    RETURN

```

MNTRI CALCULATES TRAJECTORIES AND RHS (FOR SOLID BEAM)

```
100 FORMAT(25H1 L A S T C Y C L E )
101 FORMAT(3X3H X=F10.5,5H NO.,7X1HY,14X2HVX,14X2HVV/(16XI5,3E15.6))
102 FORMAT(27HOEMITTER CURRENT IN TUBES /(7(1XI2,E14.6)))
103 FORMAT(25H TOTAL EMITTER CURRENT E14.6)
104 FORMAT(18H1 C Y C L E NO. I2)
105 FORMAT(11HO RHTEST= F9.5,6X7HUTEST= F11.4)
END(1,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0)
```

PEQ CALCULATES THE EQUIPOTENTIAL LINE FOR THE CURRENT DENSITY

SUBROUTINE PEQ
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,VLTN,ARCL,EQX,EQY,
1 NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2 ETY,PTY,PTX,NAJ,NTJ,VA,VH,VC,NCOR,KCH,HSL,XLSL,EPS,NPOT,
3 IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,GBT,SIZE,KRT,RHUP,RHDOWN,
4 XCU,NOT,MD,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,VURL,NJOT,XEMIT,
5 IXD,IGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DX,NDIM,VD,VTH,
6 VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),
1 U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2 A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3 ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4 PTY(60)
C NPOT=POINT THRU WHICH THE EQUIPOTENTIAL LINE IS DETERMINED
POTEN=U(NPOT)
DX=H
L=0
24 AAX=0.
JE= NYF + 1
DO 28 JJ=1,NSPAN
AAY=0.
JED=JE+NYF-1
DO 27 K=JE,JED
J = K - NYF
IF((U(K)-POTEN)*(U(J)-POTEN)) 21,21,27
21 DIF=ABSF(U(J)-U(K))
L=L+1
PTY(L)=AAY
IF(DIF) 22,26,22
22 PTX(L)=ABSF(U(J)-POTEN)/DIF*DX+AAX
GO TO 27
26 PTX(L)=AAX+DX
27 AAY=AAY+DX
AAX=AAX+DX
28 JE = JE + NYF
DO 41 J=1,L
LL=L-J+1
TT=0.
JJ=LL
DO 40 I=1,LL
IF(TT-PTY(I)) 39,39,40
39 TT=PTY(I)
NN=1
40 CONTINUE
PP=PTY(JJ)
PTY(JJ)=TT
PTY(NN)=PP
PP=PTX(JJ)
PTX(JJ)=PTX(NN)
PTX(NN)=PP
41 CONTINUE
DO 44 J=2,L
IF(PTY(J)-PTY(J-1)) 44,42,44
42 NN=L-1

PEQ CALCULATES THE EQUIPOTENTIAL LINE FOR THE CURRENT DENSITY

```
DO 43 JJ=J,NN
PTX(JJ)=PTX(JJ+1)
43    PTY(JJ)=PTY(JJ+1)
44    CONTINUE
EQX=PTX(L-1)
EQY=PTY(L-1)
DO 210 KJ=1,L
IF (PTY(KJ)-PTY(KJ+1)) 210,211,210
211    PM = MIN1F(PTX(KJ),PTX(KJ+1))
PTX(KJ) = PM
PTX(KJ+1) = PM
210    CONTINUE
70    WRITE OUTPUT TAPE 6,100,(J,PTX(J),PTY(J),J=1,L)
60    RETURN
100   FORMAT(18HOX,Y-EQUIPOTENTIAL /,(7(1H ,I2,2H (F5.3,1H,F5.3,2H) )))
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

TRAJ CALCULATES THE TRAJECTORY COORDINATES AND VELOCITIES

```

SUBROUTINE TRAJ(M,KE,KED)
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1   NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISW,ETX,
2   ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3   IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4   XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5   IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6   VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),
1   U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2   A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3   ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4   PTY(60)
JE=KE
300019
JED=KED
300020
K=M
300021
XEP = FLOATF(NYF-1)*H
AD=AY(K)/DX
300022
JX=AD
300023
XA=JX
300024
XA=AD-XA
300025
JP=JX+JE
300026
JS = 10
JQ = JP-NYF
UL=(1.-XA)*U(JQ)+XA*U(JQ+1)
300029
UK=(1.-XA)*U(JP)+XA*U(JP+1)
300030
C CALCULATION OF LEFTHAND DERIVATIVE
300031
IF(XA-.5) 1,1,5
300032
1   IF(JX) 2,2,3
2   YLA=2.*XA*(U(JQ+1)-U(JQ))
300034
GO TO 4
300035
3   YLA=(XA+.5)*U(JQ+1)-2.*XA*U(JQ)+(XA-.5)*U(JQ-1)
4   DY=VY(K)/VX(K)
300037
JOX=JX
300038
GO TO 7
300039
5   JX=JX+1
300040
JQ=JQ+1
300041
XA=XA-1.
300042
IF (JX-NYF +1) 3,6,6
6   YLA=2.*XA*(U(JQ-1)-U(JQ))
300044
GO TO 4
300045
C CALCULATION OF RIGHTHAND DERIVATIVE
300046
7   XB=XA+DY
300047
IF(DY) 9,9,10
300048
8   JX=JX-1
300049
XB=1.+XB
300050
9   IF(XB+.5) 8,12,12
300051
11  XB=XB-1.
300052
JX=JX+1
300053
10  IF(XB-.5) 12,12,11
300054
12  IF(JX) 14,17,16
300055
13  JX=JX+2*(1-NYF)
300057
14  JX=-JX
XB=-XB
300058

```

TRAJ CALCULATES THE TRAJECTORY COORDINATES AND VELOCITIES

15	JP=JE+JX	300059
	YRA=(XB+.5)*U(JP+1)-2.*XB*U(JP) + (XB-.5)*U(JP-1)	
	IF(XB) 19,20,20	300061
16	IF (JX-NYF +1) 30,18,13	
30	IF(K-1) 32,32,15	
32	IF(AX(1)-ETX(1)-2.*H) 34,34,15	
34	XB=ABSF(XB)	
17	JP=JE + JX	
	YRA=2.*XB*(U(JP+1)-U(JP))	300064
	XB=ABSF(XB)	300065
	GO TO 20	300066
18	JP=JE+JX	300067
	YRA=2.*XB*(U(JP-1)-U(JP))	300068
19	JP=JP-1	300069
	XB=1.-ABSF(XB)	300070
20	JQ = JP-NYF	
	USN=(1.-XB)*U(JQ)+XB*U(JQ+1)	300072
	UQN=(1.-XB)*U(JP)+XB*U(JP+1)	300073
	DUX=.5*(UK-UL-USN+UQN)	300074
	DUXX = VX(K)**2-2.*XQM*DUX	
	IF (DUXX) 35,36,36	
35	VXB=- SQRTF(-DUXX)	
	GO TO 37	
36	VXB = SQRTF(DUXX)	
37	DT = ABSF(2.*DX/(VXB+VX(K)))	
	JS=JS-1	300077
C	YA=Y ACCELERATION	300078
	XD = .5*XQM/DX	
	YA=XD*(YLA+YRA)	300079
C	DY=DELTA Y INCREMENT	300080
	DY=DT*(VY(K)-.5*YA*DT)/DX	300081
	JX=JOX	300082
	IF(JS) 21,21, 7	300083
21	VX(K)=VXB	300084
	IF (VX(K)) 38,38,39	
38	CU(K) = 0.	
	AY(K) = -1.	
	GO TO 26	
39	VY(K)=VY(K)-YA*DT	300085
	AY(K)=AY(K)+DY*DX	300086
C	REFLECTION OF TRAJECTORIES IF OUTSIDE BOUNDS	300087
	IF(AY(K))22,23,23	300088
22	AY(K)=-AY(K)	300089
	GO TO 25	300090
23	IF(AY(K)-XEP) 26,26,24	300091
24	AY(K)=XEP+XEP-AY(K)	300092
	IF(VY(K))27,27,25	300093
25	VY(K)=-VY(K)	300094
27	KCH(K)=KCH(K)+1	300095
26	CONTINUE	300096
	RETURN	300097
	END(1,0,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0,0)	

TRCU INITIALIZES TRAJ. AND CALCULATES CUR.DENSITIES

```
SUBROUTINE TRCU(KE,KED)
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DX,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3  IDEC,JNT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XCU,NOT,MD,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5  IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY,YAXS,NFUL
DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
DIMENSION US(2),UR(2)
JEK=KE
JD=KED
DO 16 K=1,NTJ
IF (NFUL) 50, 50, 60
50 XEP = YAXS
50 LL=0
KK=K
CCHECK ON TERMINATED TRAJECTORIES
IF (AY(K)+1.) 16,16,18
CCHECK ON UNINITIALIZED TRAJECTORIES
18 IF (KCH(K)) 20,15,15
CCHECK IF TRAJECTORY CAN BE INITIALIZED
20 IF (AX(1)-ETX(KK)-.05*H) 16,16,2
2  KK=KK+1
IF (IDEC ) 800,801,801
801 TB=(XEP-ETY(KK-1))/(XEMIT+ETX(KK-1))
DE = ATANF(TB)
TB = - TB
XX= ETY(KK-1)-TB*ETX(KK-1)
JJ=1
GO TO 42
800 TB=(XEP-ETY(KK-1))/(XEMIT-ETX(KK-1))
DE = ATANF(TB)
XX= ETY(KK-1)-TB*ETX(KK-1)
JDY1= ETY(KK-1)/DX +1.
DO 777 JJB=1,JDY
IF (PTY(JJB)) 774,774,775
775 JJ= PTY(JJB)/DX +1.
IF (JJ=JDY1-1) 777,777,779
779 JJ=JJB
GO TO 776
774 JJ= JJB-1
776 JJB = JDY
777 CONTINUE
4  IF (PTY(JJ+1)) 42,6,42
42 PTT = PTX(JJ)-PTX(JJ+1)
PTT=ABSF(PTT)
IF(PTT-.0001) 43,43,44
43 CPX = PTX(JJ)
CPY = ETY(KK-1) + TB*CPX
```

TRCU INITIALIZES TRAJ. AND CALCULATES CUR.DENSITIES

```

      GO TO 45
44   TA = -DX/(PTX(JJ)-PTX(JJ+1))
      YY=PTY(JJ)-TA*PTX(JJ)
      CPX=(YY-XX)/(TB-TA)
      CPY=YY+TA*CPX
45   IF(IDEC) 5,7,7
5    IF ((CPY-PTY(JJ))*(CPY-PTY(JJ+1))) 8,8,6
6    JJ = JJ-1
    GO TO 4
7    IF(PTY(JJ+1)-CPY) 3,3,8
3    JJ = JJ+1
    GO TO 4
8    LL=LL+1
    IF (LL-2)9,10,10
CTRAJECTORIES INITIALIZED
9    AY(KK-1)=ETY(KK-1)+TB*(AX(1)-ETX(KK-1))
    XA=AY(KK-1)/DX
    JX=XA
    JP=JEX+JX
    AD=JX
    XA=XA-AD
    UP=(1.-XA)*U(JP)+XA*U(JP+1)
    PHI = 1.570795 - DE
    IF (VA-UP) 900,901,901
900   V = - SQRTF(2.*XQM*(UP-VA))
    VX(KK-1) = V*COSF(DE) + VTH*COSF(PHI)
    IF (VX(KK-1)) 904,904,903
904   AY(KK-1) = -1.
    CU(K) = 0.
    KCH(K) = 0
    GO TO 16
901   V=SQRTF(2.*XQM*(VA-UP))
    VX(KK-1) = V*COSF(DE) + VTH*COSF(PHI)
903   IF (IDEC) 850,851,851
851   VY(KK-1) = - V*SINF(DE) - VTH*SINF(PHI)
    GO TO 902
850   VY(KK-1)=V*SINF(DE) - VTH*SINF(PHI)
902   TB = VY(KK-1)/VX(KK-1)
    AY(K) = ETY(KK-1) + TB*(AX(1)-ETX(KK-1))
10   US(LL)=CPX
    UR(LL)=CPY
    IF(K=NTJ)12,11,12
CSPECIAL FOR LAST CURRENT DENSITY
11   LL=2
    US(2)=EQX
    UR(2)=XEP
    PPX=.5*(ETX(KK-1)+ETX(KK) )
    PX=.5 *(US(1)+US(2))
    PPY=.5*(ETY(KK-1)+ETY(KK))
    RHO = XEP - ETY(KK-1)
    PY=.5 *(UR(1)+UR(2))
    GO TO 31
12   IF(LL-2)2,14,14
14   PPX = .5*(ETX(KK-2)+ETX(KK-1))
    PX=.5*(US(1)+US(2))
    PPY = .5*(ETY(KK-2)+ETY(KK-1))

```

TRCU INITIALIZES TRAJ. AND CALCULATES CUR.DENSITIES

```
RHO=XEP-PPY
PY=.5*(UR(1)+UR(2))
31 DEX=SQRTF((PX-PPX)**2+(PY-PPY)**2)
    IF (IDEC) 603,604,604
603 RA = DEX/(XEMIT-ETX(NTJ+1))
    IF (NDIM-2) 631,631,602
602 CR= 1.+1.6*RA + 2.06*(RA**2)
    GO TO 600
631 CR= 1.+.8*RA +.66*(RA**2)
    GO TO 600
604 RA = DEX/(XEMIT+ETX(NTJ+1))
    IF (NDIM-2) 605,605,606
606 CR = 1.-1.6*RA + 2.6*(RA**2)
    GO TO 600
605 CR = 1.-.8*RA+.66*(RA**2)
600 POTEN=U(NPOT)
DELU=VA-POTEN
XK=4./9.*YEP*SQRTF(2.*XQM*DELU)*DELU
YCU=XK/(CR*DEX**2)
CCALCULATION OF CURRENT DENSITY
53 IF (NDIM-2) 54,54,55
54 IF (K-NTJ) 56,57,57
56 CU(K)= YCU*ARCL
XCU(K) = CU(K)
GO TO 52
57 CU(K)= .5*ARCL*YCU
XCU(K) = CU(K)
GO TO 52
55 IF (K-NTJ) 17,19,19
19 CU(K) = YCU*RHO**2
XCU(K) = CU(K)*3.1416
GO TO 52
17 CU(K) = ARCL*RHO*YCU
XCU(K) = CU(K) * 6.2832
52 IF (AX(1)-ETX(K)-.5*H) 51,51,58
58 KCH(K) = 0
51 WRITE OUTPUT TAPE 6,100,US(1),US(2),UR(1),UR(2),DEX,YCU,
1 KCH(K),K
GO TO 16
CTRAJ CALCULATES THE TRAJECTORIES AFTER THEY HAVE BEEN INITIALIZED
15 CALL TRAJ(K,JEX,JD)
16 CONTINUE
CALL CORRCT
RETURN
100 FORMAT(4H X1=E8.3,4H X2=E8.3,4H Y1=E8.3,4H Y2=E8.3,4H DX=E8.3,
14H CD=E10.4,2I5)
END(1,1,0,0,0,1,0,0,0,0,0,0,0,0,0,0)
```

TROUT PRINTS OUT THE RHS

SUBROUTINE TROUT
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UR,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1 NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DLY,YEP,XQM,H,KISW,ETX,
2 ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3 IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4 XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5 IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6 VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),
1 U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2 A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3 ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4 PTY(60)
DIMENSION NTY(8),NTX(150)
IF(MO) 10,3,10
10 K=1
WRITE OUTPUT TAPE 6,101
NN=1
DO 1 N=1,NXF
NTX(NN)=N
DO 4 J=1,NYF
NTY(K)=J
I=(N-1)*NYF+J
PTY(K)=RH(I)*RX
K=K+1
IF (J-NYF) 13,14,14
13 IF (K-9) 4,2,2
14 DO 7 JJ=K,8
PTY(JJ)=0.0
7 NTY(JJ)=0
2 WRITE OUTPUT TAPE 6,100,NTX(NN),(NTY(L),L=1,8),(PTY(L),L=1,8)
K=1
4 CONTINUE
NN=NN+1
1 CONTINUE
8 RETURN
3 WRITE OUTPUT TAPE 6,104
GO TO 10
100 FORMAT (1H I3,3X8I4,8F10.3)
101 FORMAT(49HO RHS OF MATRIX EQUATION - SPACE-CHARGE DENSITY)
104 FORMAT(25HORH-FIELD OF LAST CYCLE)
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0)

TWOUT PRINTS OUT THE POTENTIAL FIELD

SUBROUTINE TWOUT
CSpace-Charge Solution. Vlad Hamza Microwave Laboratory.

```
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DX,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XSL,EPS,NPOT,
3  IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XCU,NOT,M0,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5  IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
DIMENSION NYT(8),NTX(150)
IF(M0) 10,3,10
10  K=1
      WRITE OUTPUT TAPE 6,101
NN=1
DO 1 N=1,NXF
NTX(NN)=N
DO 4 J=1,NYF
NYT(K)=J
I=(N-1)*NYF+J
PTY(K)=U(I)
K=K+1
IF (J-NYF) 13,14,14
13 IF (K-9) 4,2,2
14 DO 7 JJ=K,8
PTY(JJ)=0.0
7  NYT(JJ)=0
2  WRITE OUTPUT TAPE 6,100,NTX(NN),(NYT(L),L=1,8),(PTY(L),L=1,8)
      K=1
4  CONTINUE
NN=NN+1
1  CONTINUE
8  RETURN
3  WRITE OUTPUT TAPE 6,104
NURL=-7777
GO TO 10
100 FORMAT (1H I3,3X8I4,8F10.3)
101  FORMAT(25HO  U-FIELD OF THIS CYCLE.  )
104  FORMAT(25HOU-FIELD OF LAST CYCLE.  )
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0)
```

UCAL SOLVES THE MATRIX EQUATION

```

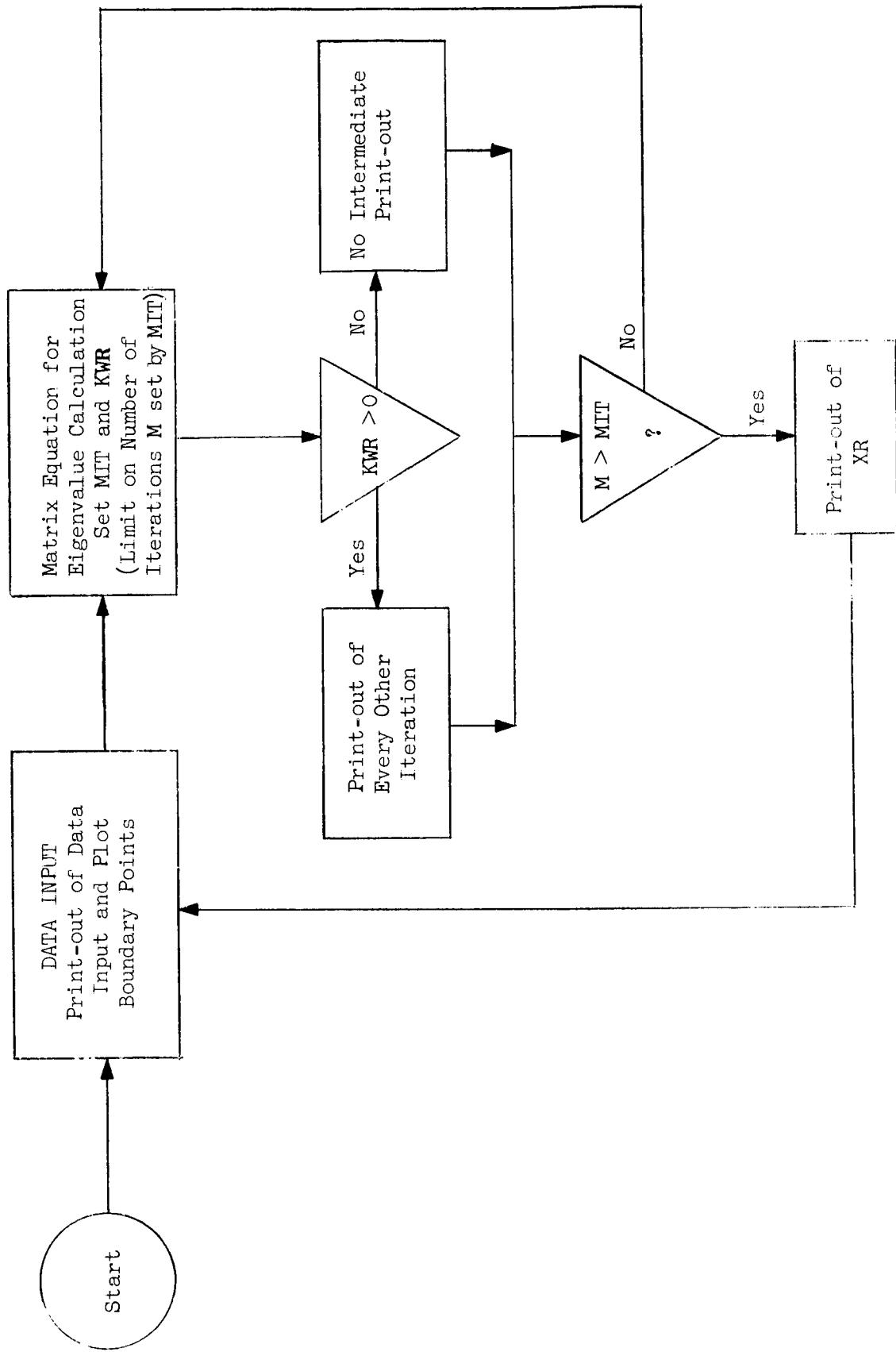
SUBROUTINE UCAL
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1   NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DY,DELY,YEP,XQM,H,KISH,ETX,
2   ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3   IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4   XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5   IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6   VTHX,VTHY
      DIMENSION KRT(2),JT(4000),RH(4000),
1   U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2   A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3   ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4   PTY(60)
      IF (NRL-KRL) 46,6,46
6   WRITE OUTPUT TAPE 6,101
46   XW=1.
      DO 30 NLU=1,NUL
      NEZ=NLU
      XEP=0.
      XM=.25*XN**2
      NOD=1
38   DO 29 NL=1,NLIN
      IF(LINC(NL))29,29,33
33   KB=LINC1(NL)
      KC=LINC2(NL)
      JV=1
      JU=1
      DO 28 K=KB,KC
      SUM=0
      JZ=JT(K)
27   DO 22 JY=3,5
      JX=JZ+JY
      A(JU)=XT(JX)
22   JU=JU+1
      DO 26 JY=1,5
      JX=JZ+JY
      IF(KT(JY))34,26,34
34   IF(XT(JX)) 26,26,25
25   JW=K+KT(JY)
      SUM=SUM+XT(JX)*U(JW)
26   CONTINUE
      X(JV)=SUM+XT(JZ)*RH(K)*RX
      JV=JV+1
28   CONTINUE
      N=KC-KB+1
C MATRIX IS USED FOR THE FORWARD AND BACK SUBSTITUTION
      CALL MATRIX (N,A(2),X)
      JV=1
      DO 24 K=KB,KC
23   DIF=X(JV)-U(K)
      JV=JV+1
C MATRIX EQUATION
      U(K)=XW*DIF+U(K)
      DIF=ABSF(DIF)

```

UCAL SOLVES THE MATRIX EQUATION

```
      IF(DIF-XEP) 24,24,21
21      XEP=DIF
      NXEP=K
24      CONTINUE
29      LINC(NL)=-LINC(NL)
      IF(XW-1.) 40,31,40
40      XW=1./(1.-XM*XW)
      GO TO 41
31      XW=1./(1.-2.*XM)
41      IF(NOD) 37,37,36
36      NOD=0
      GO TO 38
37      XCON=XEP*XMPR
      IF(XCON -EPS) 42,42,30
30      CONTINUE
42      KNUT=KRT(1)
      J=2
      DO 43 K=1,KNUT
      JN=KRT(J)
      IF(U(JN)-VA) 43,49,49
43      J=J+1
      GO TO 47
49      WRITE OUTPUT TAPE 6,102
      WRITE OUTPUT TAPE 6,100,JN,U(JN)
      CALL EXIT
47      IF(NRL-KRL) 2,1,2
1      NUL=NURL
2      IWRL=NRL-KRL+XABSF(M0)
      WRITE OUTPUT TAPE 6,104,NEZ,NXEP,XCON,EPS
      IF(KCY(IWRL)) 4,4,3
C TWOUT PRINTS OUT THE POTENTIAL FIELD
3      CALL TWOUT
C EQLINE CALCULATES THE EQUIPOTENTIALS
      CALL EQLINE
4      RETURN
100     FORMAT(16H0    POINT NO.= I5,5X10HVOLTAGE = F15.5)
101     FORMAT(39H1    NO SPACE-CHARGE - LAPLACE SOLUTION )
102     FORMAT(31H0I CANNOT GET OUT OF THE LOOP   )
104     FORMAT(34H0ITERATION NO./POINT/ERROR/EPSILON  13,I5,2F15.6)
END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0)
```

APPENDIX B



Flow Chart for XR-Calculations

MAIN ONE -DATA INPUT

MAIN1

```
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
C      THIS SUBROUTINE IS GOOD FOR XR-CALCULATION ONLY
C      XR IS THE LARGEST EIGENVALUE OF THE MATRIX
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1  NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DX,DELY,YEP,XQM,H,KISW,ETX,
2  ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3  IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4  XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,NURL,NJOT,XEMIT,
5  IXO,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6  VTHX,VTHY, YAXS, NFUL
      DIMENSION KRT(2),JT(4000),RH(4000),
1  U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2  A(180),X(6C),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3  ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4  PTY(60)
      DIMENSION ND(3),KRTX(10),KRTY(10),WOLT(28)
200  MO=1
      READ INPUT TAPE 5,100,NH
      DO 13 J=1,NH
      READ INPUT TAPE 5,107
13    WRITE OUTPUT TAPE 6,107
      READ INPUT TAPE 5,100,NXF,NYF,NEM,NTJ,NDIM,NRL,NUL,NURL,
      INCOOR, IDEC, NFUL, NCO, KRHX, KRHY
      JDY = NYF
      WRITE OUTPUT TAPE 6,108
108   FORMAT(5H0 NXF,5H NYF,5H NEM,5H NTJ,5H NDIM,5H NRL,5H NUL,
      15H NURL,5HNCOOR,5H IDEC,5H NFUL,5H NCO,5H KRHX,5H KRHY)
      WRITE OUTPUT TAPE 6,310,NXF,NYF,NEM,NTJ,NDIM,NRL,NUL,NURL,
      1  NCOOR,IDECK,NFUL, NCO, KRHX, KRHY
      READ INPUT TAPE 5,300,IXO,NSPAN,NPOTX,NPOTY, YAXS
      WRITE OUTPUT TAPE 6,109
109   FORMAT(5H0 IXO,5HNSPAN,5HN POTX,5HN POTY, 8H YAXS)
      WRITE OUTPUT TAPE 6,311,IXO,NSPAN,NPOTX,NPOTY, YAXS
      READ INPUT TAPE 5,100,NRTN,(KRTX(K),KRTY(K),K=1,NRTN)
      WRITE OUTPUT TAPE 6,110
110   FORMAT(5HOKRTN,5H KRTX,5H KRTY,5H KRTX,5H KRTY,5H KRTX,5H KRTY)
      WRITE OUTPUT TAPE 6,310,NRTN,(KRTX(K),KRTY(K),K=1,NRTN)
      READ INPUT TAPE 5,102,VAT,VBT,SIZE,VA,VB,VC
      WRITE OUTPUT TAPE 6,111
111   FORMAT(4X3HVAT,7X3HVBT,6X4HSIZE,7X2HVA,8X2HVB,8X2HVC)
      WRITE OUTPUT TAPE 6,302,VAT,VBT,SIZE,VA,VB,VC
      READ INPUT TAPE 5,102,HGH,XLOW,HSL,XLSL,VD
      WRITE OUTPUT TAPE 6,112
112   FORMAT(4X3HHGH,6X4HXLOW,6X3HHSL,7X4HXLSL,7X2HVD)
      WRITE OUTPUT TAPE 6,302,HGH,XLOW,HSL,XLSL,VD
      READ INPUT TAPE 5,102,AXX,BXX,CXX,DXX,XR
      WRITE OUTPUT TAPE 6,113
113   FORMAT(4X3HAXX,7X3HBXX,7X3HCXX,7X3HDXX,7X2HXR)
      WRITE OUTPUT TAPE 6,302,AXX,BXX,CXX,DXX,XR
      READ INPUT TAPE 5,8,RO,EPS,XEMIT,H
      WRITE OUTPUT TAPE 6,114
114   FORMAT(7X2HRO,10X7HEPSILON,9X5HXEMIT,6X13HMESH SIZE - H)
      WRITE OUTPUT TAPE 6, 308, RO, EPS, XEMIT,H
      READ INPUT TAPE 5,105,YEP,XQM,ATOM,VTH,VTHX,VTHY
      WRITE OUTPUT TAPE 6,115
```

MAIN ONE -DATA INPUT

MAIN1

```

115 FORMAT(12X6HEPSNOT,6X3HXQM,6X4HATOM,6X3HVTH,7X4HVTHX,6X4HVTHY)
  WRITE OUTPUT TAPE 6,105,YEP,XQM,ATOM,VTH,VTHX,VTHY
  READ INPUT TAPE 5,102,(ATX(J),ATY(J),J=1,NEM)
    WRITE OUTPUT TAPE 6,119
119 FORMAT(31HO      CATHODE COORDINATES)
  WRITE OUTPUT TAPE 6,302,(ATX(J),ATY(J),J=1,NEM)
  READ INPUT TAPE 5,100,(KCY(J),J=1,10)
    WRITE OUTPUT TAPE 6,120
120 FORMAT(33HC      PRINT-OUT OF CYCLE NO.)
  WRITE OUTPUT TAPE 6,100,(KCY(J),J=1,10)
  READ INPUT TAPE 5,104,(WOLT(NN),NN=1,28)
    WRITE OUTPUT TAPE 6,116
116 FORMAT(8HO VOLT-1,7X2H-2,8X2H-3,8X2H-4,8X2H-5,8X2H-6,8X2H-7)
  WRITE OUTPUT TAPE 6,304,(WOLT(NN),NN=1,28)

HH=H**2
HT=.5*H
H2=2.*H
XMPR=.5*(FLOAT(NXF*NYF))**2/FLOAT(NXF**2+NYF**2)
XQM=XQM/ATOM
  RX = H/YEP
  J=1
  IF (NDIM-2) 1001,1001,2005
1001 DO 1002 I=1,NYF
    IF (I-1) 1006,1006,1007
1006  XT(J+3) = 0.0
    XT(J+5) = -0.5
    GO TO 1008
1007  IF (I-NYF) 1003,1005,1003
1005  XT(J+3) = -0.5
    XT(J+5) = 0.0
    GO TO 1008
1003  XT(J+3) = -0.25
    XT(J+5) = -0.25
1008  XT(J)   = 0.25
    XT(J+1) = 0.25
    XT(J+2) = 0.25
    XT(J+4) = 1.0
1002  J = J+6
    GO TO 2011
2005 DO 2010 I=1,NYF
  RP= FLOAT(NYF-I)*H+R0
  IF (I-1) 1009,1009,1010
1009  XT(J+3) = 0.0
  XT(J+5) = -2.0*RP
  GO TO 1011
1010  IF (RP) 2009,2008,2009
2009  XT(J+5) = -(RP-HT)
  XT(J+3) = -(RP+HT)
1011  XT(J)   = 1.0
  XT(J+1) = RP
  XT(J+2) = RP
  XT(J+4) = 4.0*RP
  GO TO 2010
2008 XT(J)= .125
  XT(J+1)=.125* H
  XT(J+2)=.125*H

```

E25

65A

MAIN ONE -DATA INPUT

MAIN1

```

XT(J+3)=-.50 * H
XT(J+4)=.75 *H
XT(J+5)=0.
2010   J = J + 6
2011 NDD = 1
      NSS=2
      NTRIP=0
      NPONT=NYF
      KRH=(KRHX-1)*NPONT+KRHY
      NTOP=NPONT*NXF
      KRT(1)=NRTN
      I=2
      DO 2 K=1,NRTN
      KRT(I)=(KRTX(K)-1)*NPONT+KRTY(K)
2 I=I+1
      KT(1)=-NPONT
      KT(2)=NPONT
      KT(3)=-1
      KT(4)=0
      KT(5)=+1
      WRITE OUTPUT TAPE 6,117
117    FORMAT(41HO      BOUNDARY POINTS OF ELECTRODE SHAPE )
      CALL PLOT (0.0,VC,-3)
      DO 2020 NX=1,NXF
      DO 2020 NY=1,NYF
      IF (NTRIP) 2030,2040,2030
2040 READ INPUT TAPE 5,2035,NS,(ND(I),I=1,3),NXC,NYC,HEW,HNS,NVOLT,
1     NVOLT1,NCHECK
2035  FORMAT (1H 4I1,2I4,2F6.3,2I5,I4)
      WRITE OUTPUT TAPE 6,2035,NS,(ND(I),I=1,3),NXC,NYC,HEW,HNS,NVOLT,
1     NVOLT1,NCHECK
      IF (HNS) 2031, 2032, 2031
2031  XXX=FLOATF(NXC-1)*H*VD
      YYY=-(FLOATF(NYC-1)-HNS)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
2032  IF (HEW) 2033, 2034, 2033
2033  XXX=(FLOATF(NXC-1)+HEW)*H*VD
      YYY=-FLOATF(NYC-1)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
      GO TO 2036
2034  IF (HNS) 2036, 2037, 2036
2037  XXX=FLOATF(NXC-1)*H*VD
      YYY=-FLOATF(NYC-1)*H*VD
      CALL SYMBOL (XXX,YYY,0.07, 12,0.0,1)
2036  NTRIP = 1
      KC=  NPONT*(NXC-1)+NYC
2030 K=  NPONT*(NX-1)+NY
      IF (K-KC) 2060,2050,2060
2060 IF (NSS-1) 2070,2070,2080
2070  IF (NY-NYF) 2071,2072,2071
2072  NSS = 2
      JT(K) = 1 + 6*(NY-1)
      VOLT1= FLOATF((NXF-NX)/NXF)*VA
      GO TO 2310
2071  JT(K) = 1 + 6*(NY-1)
      GO TO 2020

```

71A

S77
S78
S79
S80
S81

MAIN ONE -DATA INPUT

```

2080   JT(K) = 9999
      IF (NX-NCO) 2081,2020,2020
2081   IF (U(K)) 2020,2084,2020
2084   U(K) = VA
      GO TO 2020
2050 NTRIP = C
      NSS=NS
      VOLT = WOLT(NVOLT)
      VOLT1 = WOLT(NVOLT1)
      HEW = HEW*H
      HNS=HNS*H
      IF (ND(3)) 2052,2052,2053
2052   VOLT1 = VOLT
2053   HN = H
      HS = H
      HE = H
      HW = H
      KE = K+NPONT
      KW = K-NPONT
      KN=K-1
      KS=K+1
      JT(K)=J
      IF (HEW) 2090,2200,2100
2090   HW = - HEW
      U(KW) = VOLT
      GO TO 2200
2100   HE = HEW
      U(KE) = VOLT
2200 IF (HNS) 2210,2230,2220
2210   HS = - HNS
      U(KS) = VOLT1
      GO TO 2230
2220   HN = HNS
      U(KN) = VOLT1
2230 IF (NDIM-2) 1004,1004,2239
1004 XT(J) = ((HN+HS)*(HE+HW))/(16.*HH)
      XT(J+1) = (HN+HS)/(8.*HW)
      XT(J+2) = (HN+HS)/(8.*HE)
      XT(J+3) = -(HE+HW)/(8.*HN)
      XT(J+5) = -(HE+HW)/(8.*HS)
      XT(J+4) = XT(J+1)+XT(J+2)-XT(J+3)-XT(J+5)
      GO TO 2233
2239 RP= (FLOATF(NPONT-NY))*H+R0
      IF(RP)2231,2232,2231
2231 XT(J)= (HE+HW)*(HN+HS)/(4.*HH)
      XT(J+1)=((HN+HS)/(2.*HW))*(RP+((HN-HS)/4.))
      XT(J+2)=HW*XT(J+1)/HE
      XT(J+3)=-(HW+HE)/(2.*HN)*(RP+(HN/2.))
      XT(J+5)=-(HW+HE)/(2.*HS)*(RP-(HS/2.))
      XT(J+4)=XT(J+1)+XT(J+2)-XT(J+3)-XT(J+5)
      GO TO 2233
134
2232 XT(J)= (HE+HW)*(HN/(16.*HH) )
      XT(J+1)=(HN/(8.*HW ))*H
      XT(J+2) = H* HN/(8.*HE)
      XT(J+3) = - H*(HE+HW)/(4.*HN)
      XT(J+4)=(HN/8.* ((HW+HE)/(HW*HE))+(HE+HW)/(4.*HN) )*H
      135A
      141A

```

MAIN1

MAIN ONE -DATA INPUT

MAIN1

141

```

XT(J+5)=-0.
2233 DO 2300 I=1,2
NDA= ND(I)+1
GO TO (2300,2240,2250,2260,2270),NDA
2240 XT(J+1) = XT(J+1)+ XT(J+2)
XT(J+2) = 0.0
GO TO 2300
2250 XT(J+5) = XT(J+5) +XT(J+3)
XT(J+3) = 0.0
GO TO 2300
2260 XT(J+2) =XT(J+2) +XT(J+1)
XT(J+1) =0.0
GO TO 2300
2270 XT(J+3) =XT(J+3) +XT(J+5)
XT(J+5) =0.0
2300 CONTINUE
IF (ND(3)) 2310,2310,2311
2311   XT(J) = 0.25
XT(J+1) = 0.
XT(J+2) = XSL
XT(J+3) = 0.
XT(J+4) = 1.
XT(J+5) = XSL - 1.
2310 IF (NSS-1) 2320,2330,2340
2330 LINC1(NDD)=K
VUP      = VOLT1
XT(J+3)  =-XT(J+3)
GO TO 2320
2340 LINC2(NDD)=K
LINC (NDD)= 2*XMODF(NX,2) -1
VDOWN    = VOLT1
KB=LINC1(NDD)
DO 2350 KK=KB,K
2350 U(KK)= VUP +(VDOWN-VUP)*FLOATF(KK-KB)/FLOATF(K-KB)
XT(J+5)= -XT(J+5)
NDD=NDD+1
2320   J = J + 6
2020 CONTINUE
NLIN=NDD-1
IF (NCHECK - 1) 4000,502,4000
4000 WRITE OUTPUT TAPE 6,4001
4001 FORMAT (24HOERROR IN BOUNDARY POINT)
CALL EXIT
502   CALL MATIN
XMAX = FLOATF(NXF-1)*H*VD + 3.0
CALL PLOT (XMAX, -VC, -3)
GO TO 200
8 FORMAT (4F15.8)
100   FORMAT(14I5)
101   FORMAT(6I5)
102   FORMAT(6F10.4)
103   FORMAT(13I5)
104   FORMAT(7F10.4)
105   FORMAT(10X6E10.5)
106   FORMAT(3F10.5)
107   FORMAT(72H

```

MAIN ONE -DATA INPUT

```
1  
300 FORMAT(4I5, F10.6)  
302 FORMAT(1H 6F10.4)  
304 FORMAT(1H 7F10.4)  
308 FORMAT(1H 4F15.8)  
310 FORMAT(1H 14I5)  
311 FORMAT(1H 4I5, F10.6)  
END(1,0,0,0,0,0,1,0,0,0,0,0,0,0,0)
```

MAIN1

MATIN CALCULATES THE EIGENVALUE

SUBROUTINE MATIN
CSPACE-CHARGE SOLUTION.VLAD HAMZA MICROWAVE LABORATORY.
COMMON URH,UB,JT,RH,U,XT,KT,LINC,XR,NTOP,NUL,NLIN,ARCL,EQX,EQY,
1 NPIT,XEP,NXEP,CU,LINC1,AX,AY,VX,VY,DX,DELY,YEP,XQM,H,KISW,ETX,
2 ETY,PTY,PTX,NAJ,NTJ,VA,VB,VC,NCOOR,KCH,HSL,XLSL,EPS,NPOT,
3 IDEC,JOT,NSPAN,RX,NRL,KRL,KRH,VAT,VBT,SIZE,KRT,RHUP,RHDOWN,
4 XCU,NOT,MO,KCY,NSWP,ATX,ATY,LINC2,NXF,NYF,VURL,NJOT,XEMIT,
5 IXU,HGH,XLOW,XMPR,NEM,A,X,JDY,AXX,BXX,CXX,DXX,NDIM,VD,VTH,
6 VTHX,VTHY
DIMENSION KRT(2),JT(4000),RH(4000),URH(4000),
1 U(4000),XT(4000),KT(5),LINC(150),LINC1(150),LINC2(150),
2 A(180),X(60),CU(40),VX(40),VY(40),KCH(40),AX(40),AY(40),
3 ATX(40),ATY(40),ETX(40),ETY(40),XCU(40),KCY(10),PTX(60),
4 PTY(60)
READ INPUT TAPE 5,102,MIT,KWR
WRITE OUTPUT TAPE 6,102,MIT,KWR
C MIT=NUMBER OF ITERATIONS ON EIGENVALUE CALCULATION
C KWR=- OR 0,NO INTERMEDIATE OUTPUT
C KWR=+,PRINT INTERMEDIATE ITERATIONS ON EIGENVALUE CALCULATION
C COLUMN VECTOR INITIALIZED
50 DO 45 J=1,NTOP
IF(JT(J)-9999)44,43,43
43 URH(J)=0.
U(J) = 0.0
GO TO 46
44 URH(J)=1.
U(J) = 0.0
46 CONTINUE
JS=-1
C ITERATIVE LOOP
DO 41 M=1,MIT
C LOOP ON NUMBER OF LINES
DO 31 NL=1,NLIN
IF(LINC(NL)) 23,31,23
23 KB=LINC1(NL)
KC=LINC2(NL)
JV=1
JU=1
DO 13 K=KB,KC
SUM=0.
JZ=JT(K)
14 DO 15 JY=3,5
JX=JZ+JY
A(JU)=XT(JX)
15 JU=JU+1
DO 16 JY=1,2
JX=JZ+JY
JW=K+KT(JY)
16 SUM=SUM+XT(JX)*URH(JW)
X(JV)=SUM
JV=JV+1
13 CONTINUE
N=KC-KB+1
CALL MATRIX(N,A(2),X)
C MATRIX IS USED FOR THE FORWARD AND BACK SUBSTITUTION

MATIN CALCULATES THE EIGENVALUE

```
        JV=1
        DO 17 J=KB,KC
        RH(J)=X(JV)
17      JV=JV+1
31      CONTINUE
C SWITCH ALLOWING MATRIX TO BE APPLIED TWICE
        IF(JS) 32,34,34
32      DO 33 J=1,NTOP
        U(J) = URH(J)
33      URH(J)=RH(J)
        GO TO 41
C DETERMINATION OF SMALLEST AND LARGEST RATIOS FOR EIGENVALUE
34      XL=0.
        XS=1.
        DO 39 JD=1,NTOP
        IF(URH(JD))39,39,35
35      X = RH(JD)/U(JD)
        IF(XL-X)36,37,37
36      XL=X
        NNL=JD
37      IF(XS-X)39,39,38
38      XS=X
        NS=JD
39      CONTINUE
        IF(KWR) 51,51,52
52      WRITE OUTPUT TAPE 6,101,M,XS,XL,NS,NNL
51      YL=RH(NNL)
        DO 40 JD=1,NTOP
40      URH(JD)=RH(JD)/YL
        IF(XL-XS-5.0E-03)42,42,41
41      JS=-JS
42      XR=SQRTF(.5*(XL+XS))
        WRITE OUTPUT TAPE 6,103,XR
47      RETURN
101     FORMAT(20H      LOW      HIGH      15,2F13.8,5H      2I6)
102     FORMAT(14I5)
103     FORMAT(4H0XR= F10.8)
        END(1,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0)
```


ARC

$$SUM = \sum_{J=2}^{NEM} [(ATX_J - ATX_{J-1})^2 + (ATY_J - ATY_{J-1})^2]^{1/2}$$

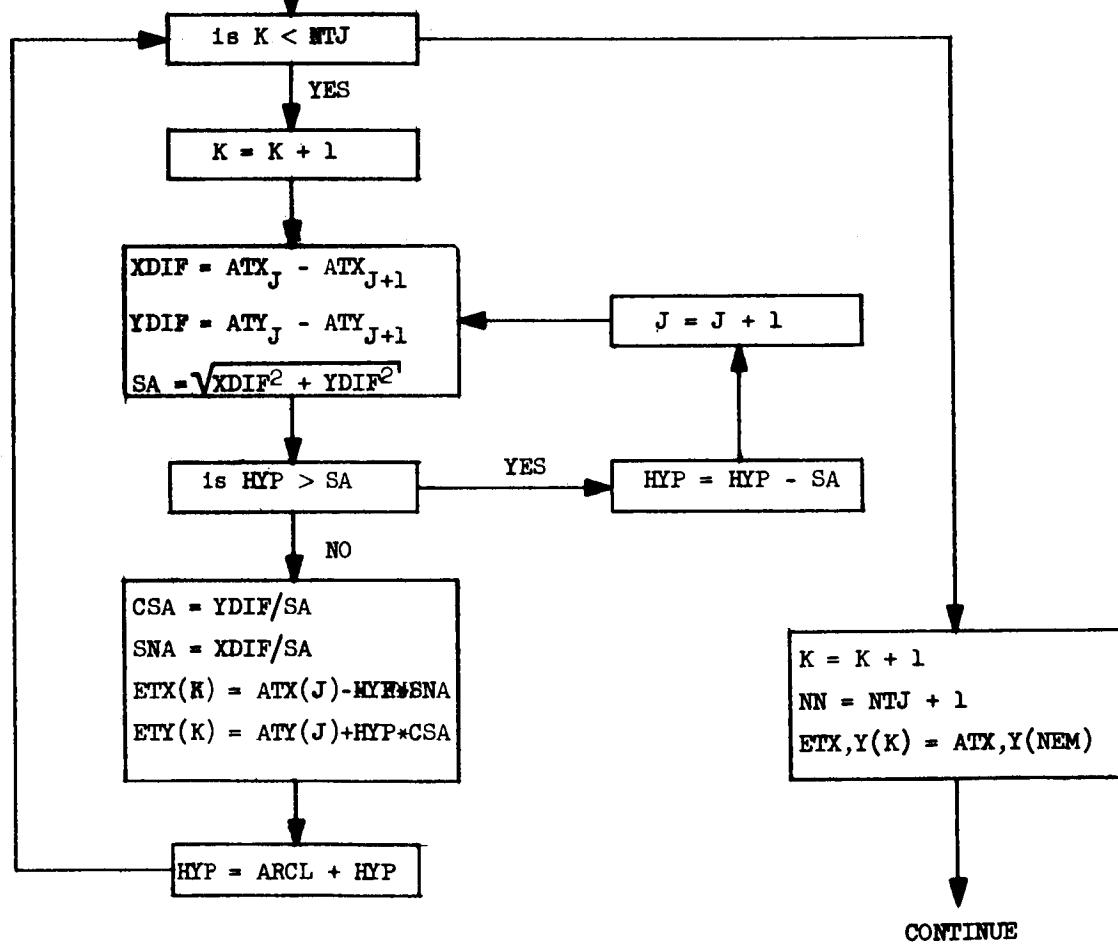
$$ARCL = \frac{SUM}{N + J + 0.5}$$

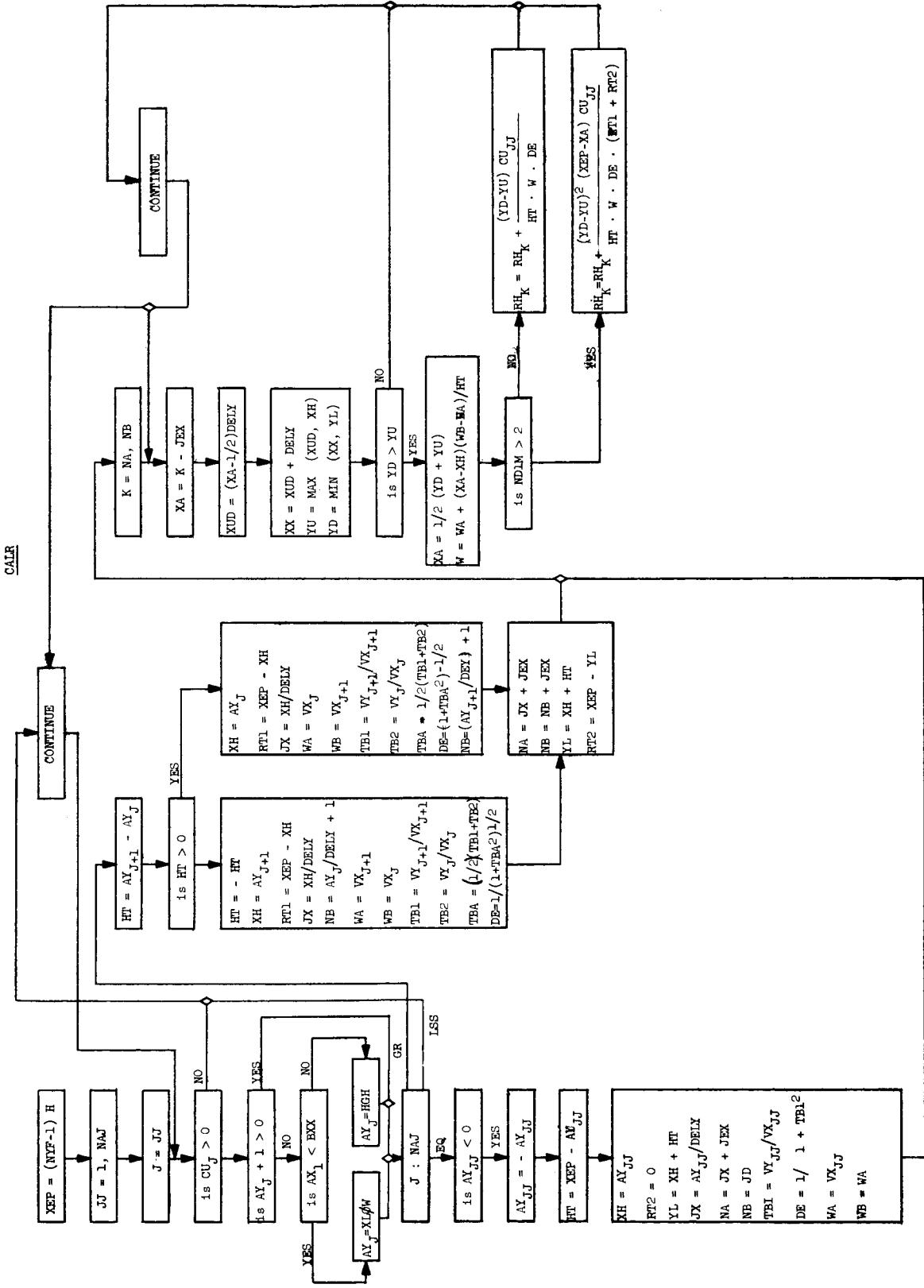
ETX,Y(1) = ATX,Y(1)

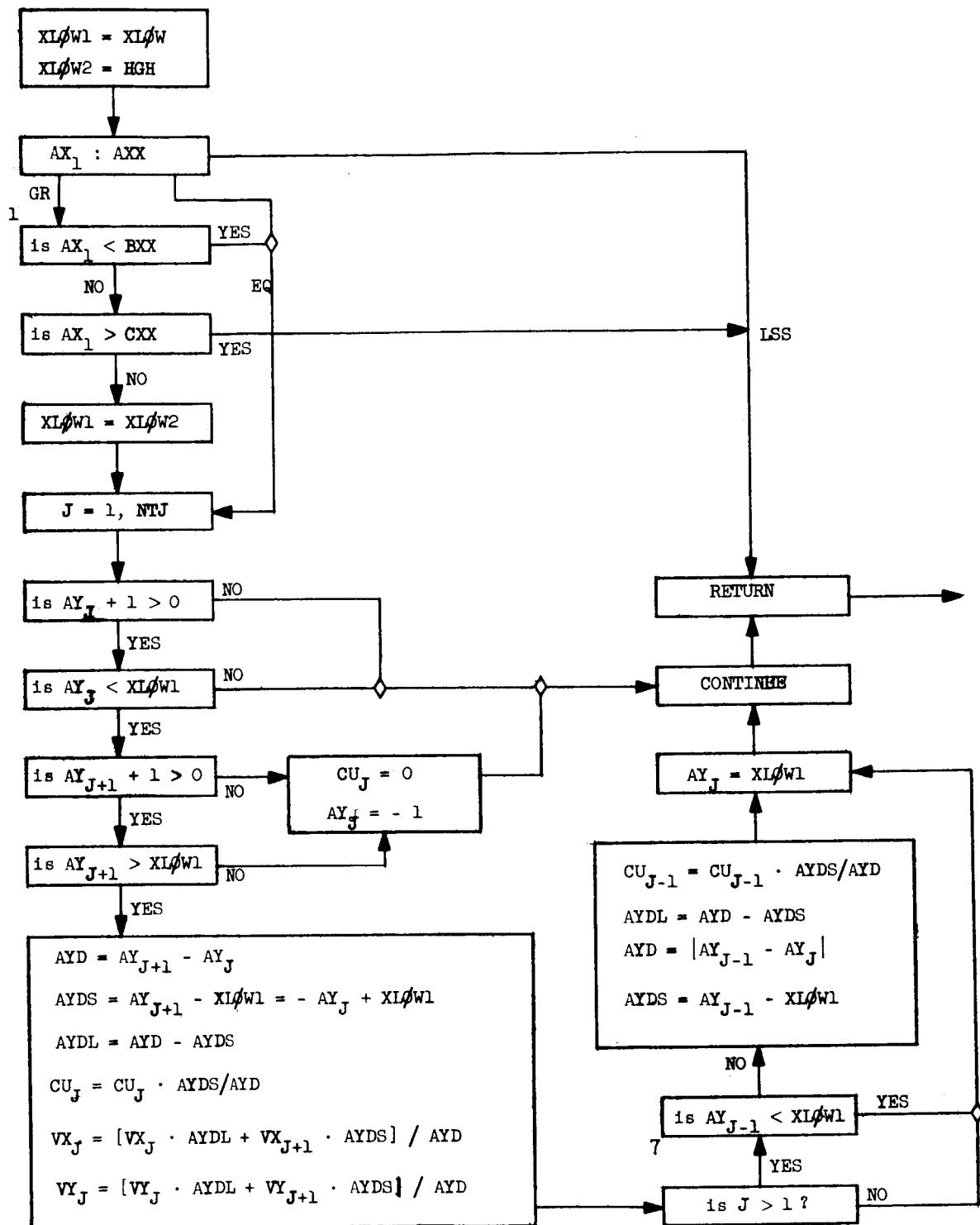
HYP = ARCL

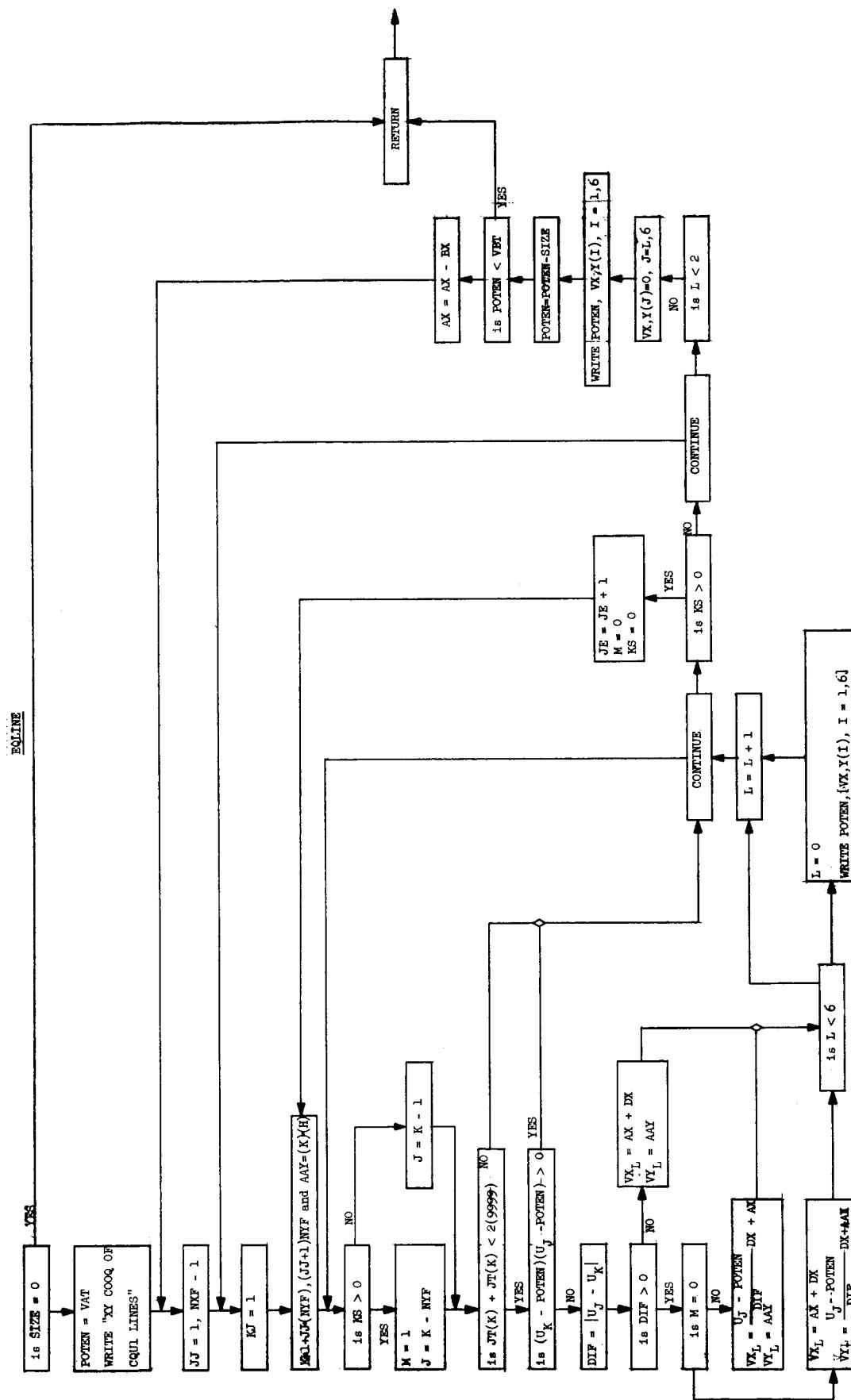
K = 1

I = 1

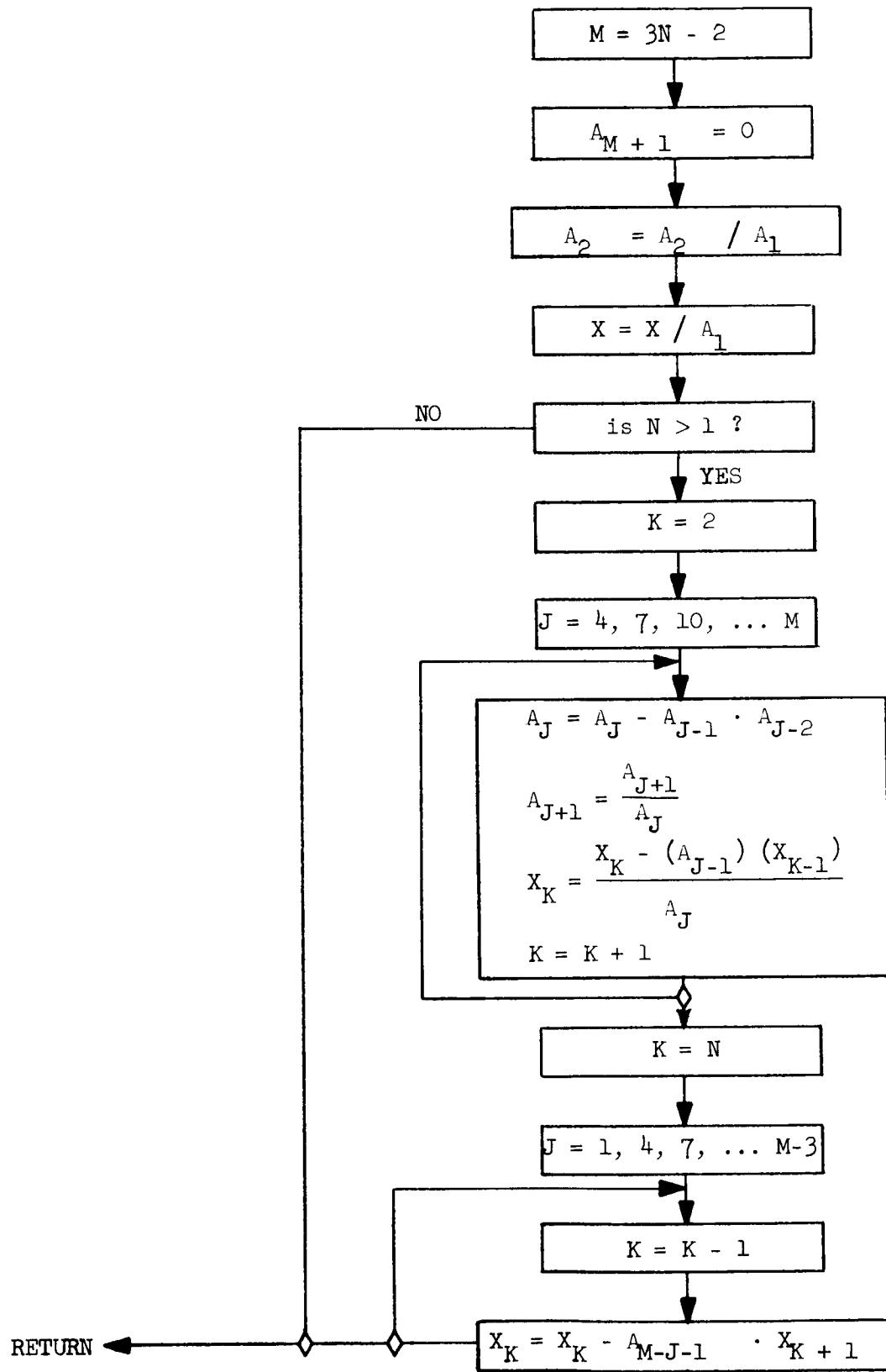


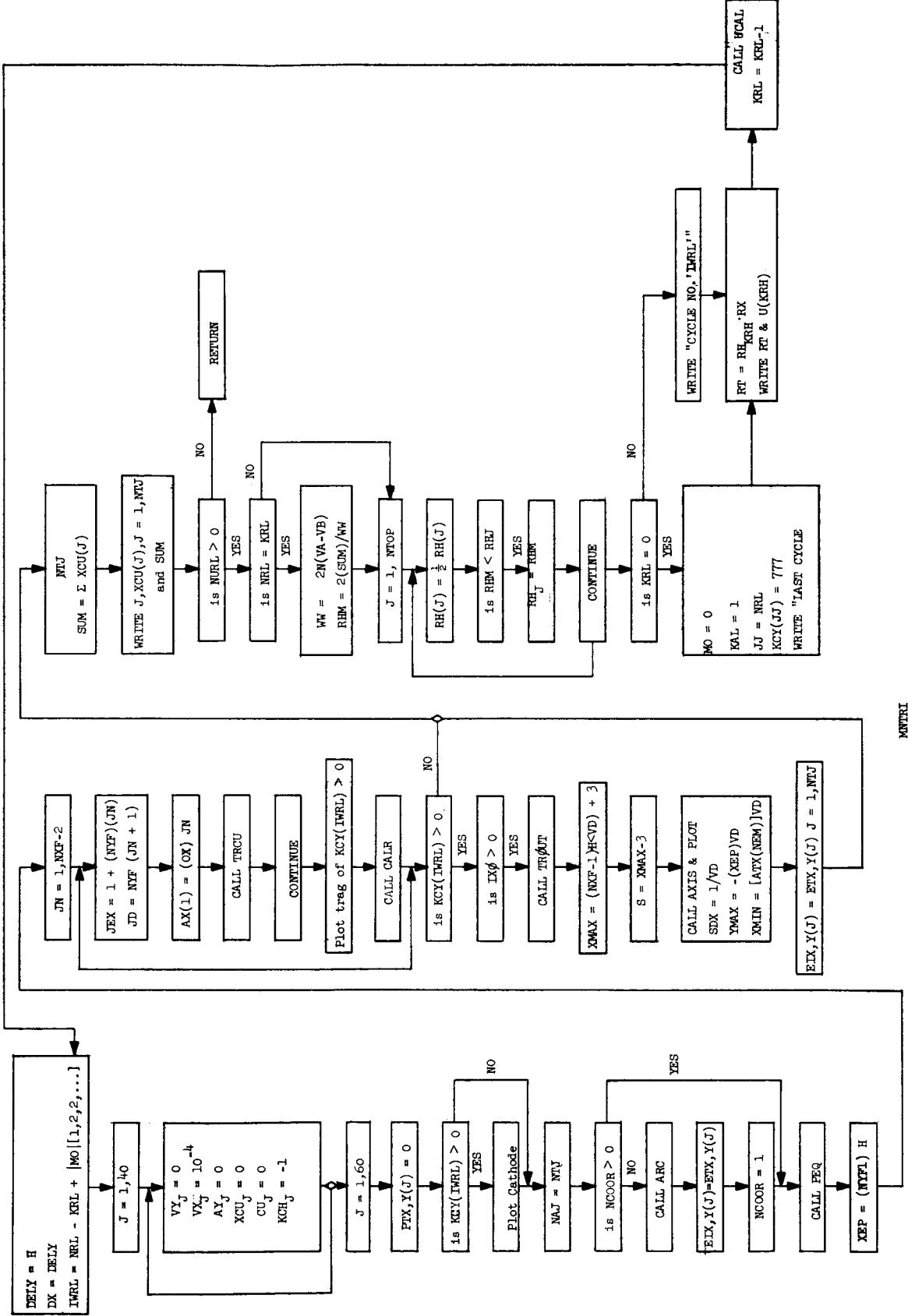


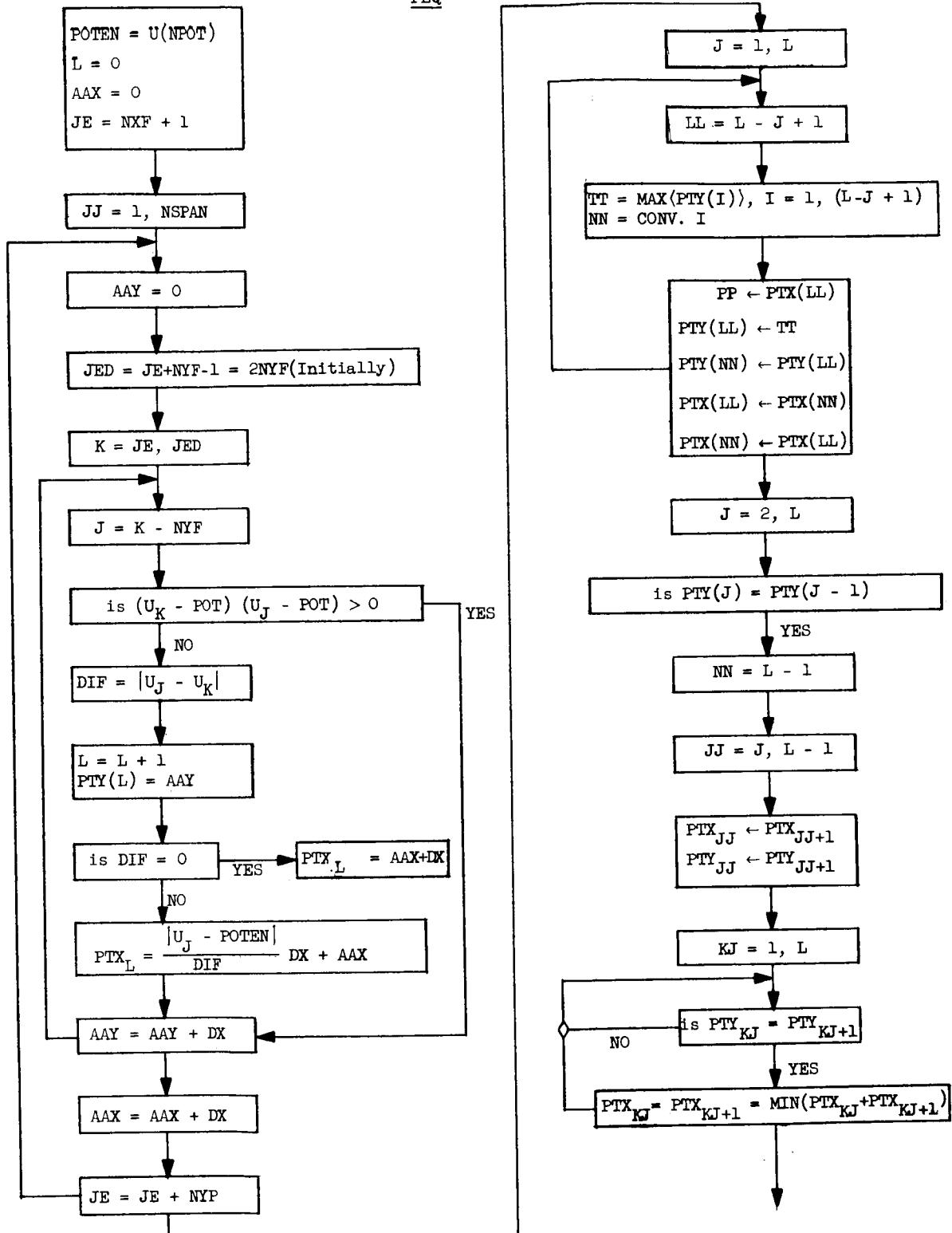


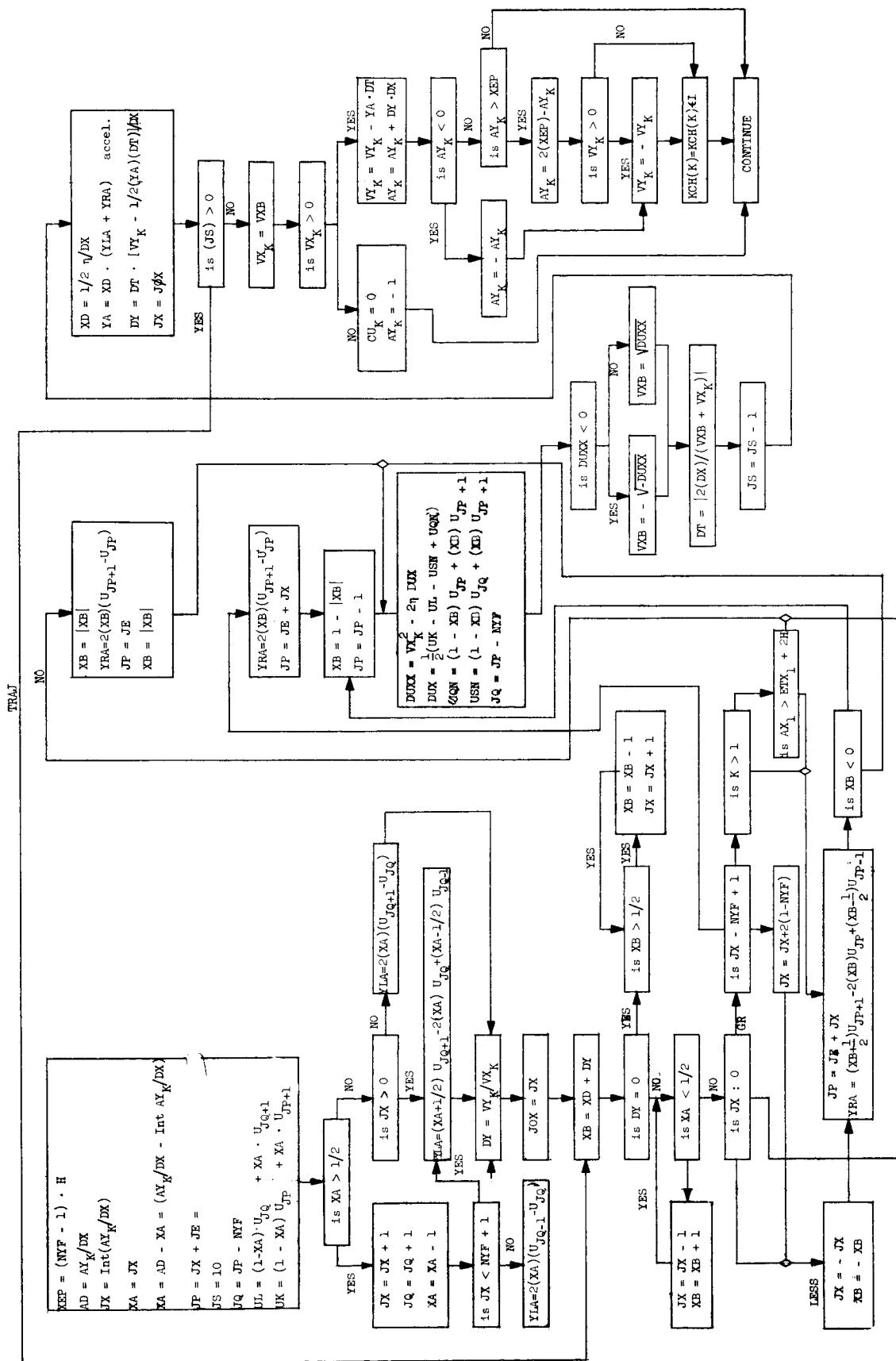


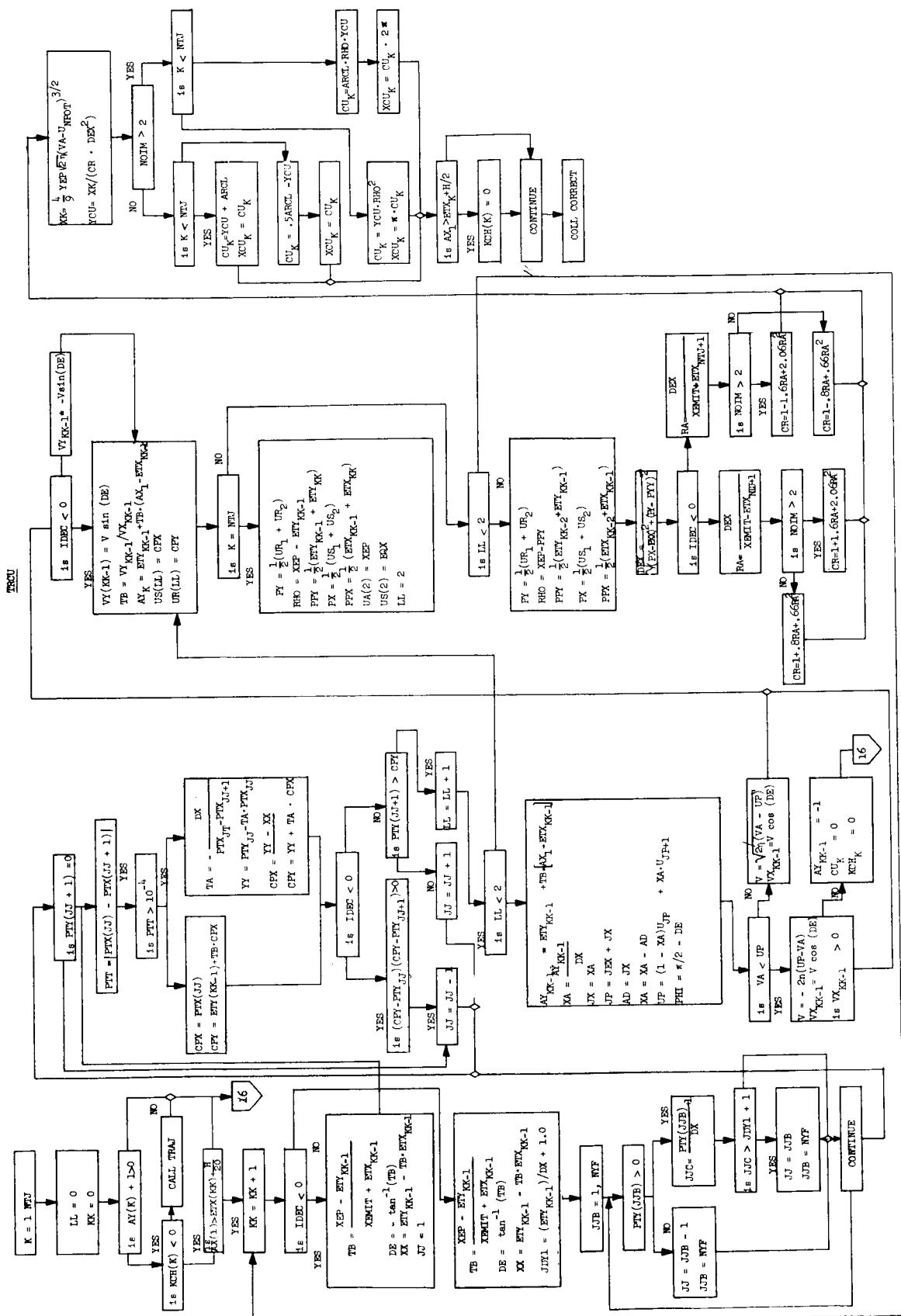
MATRIX

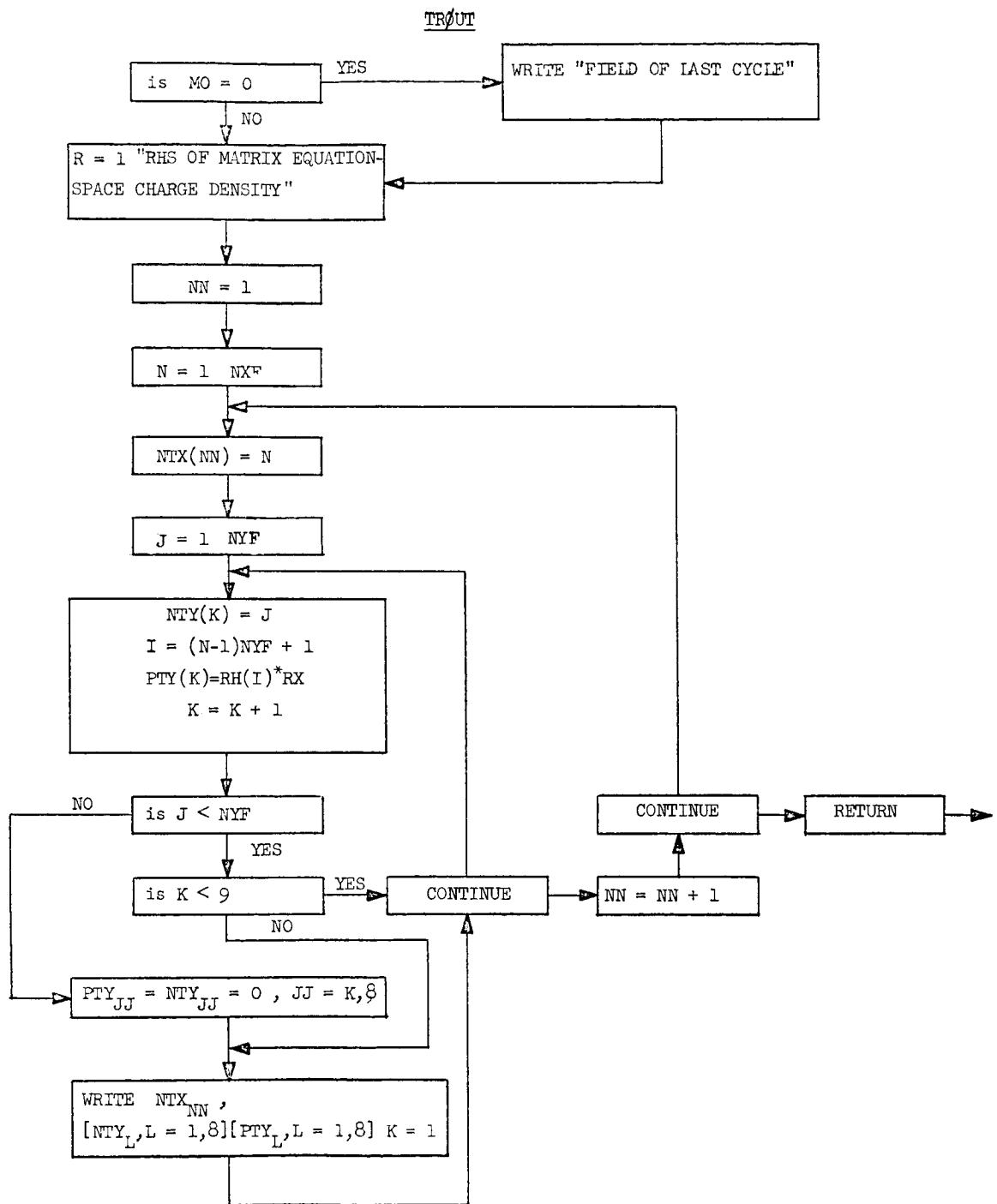


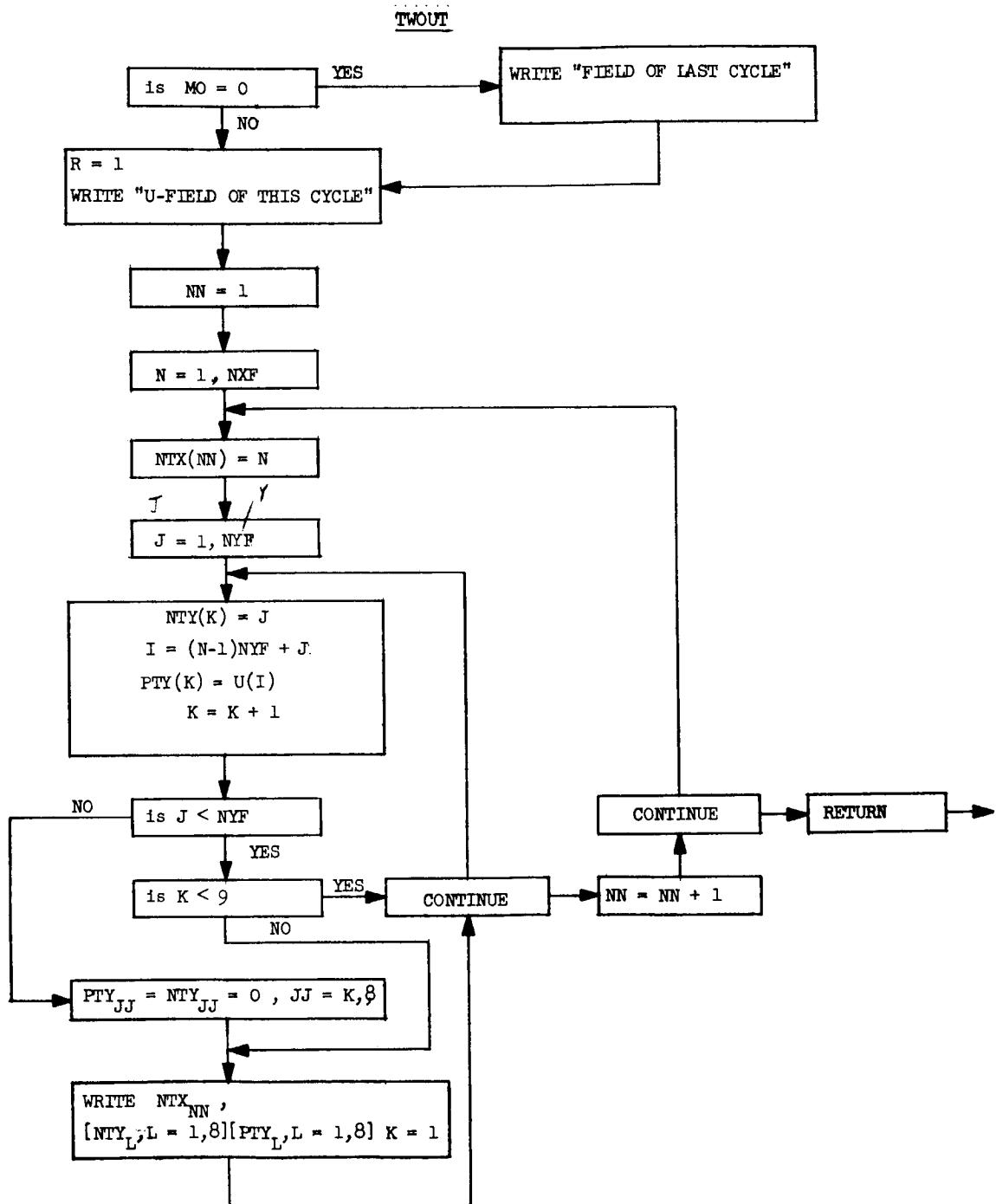


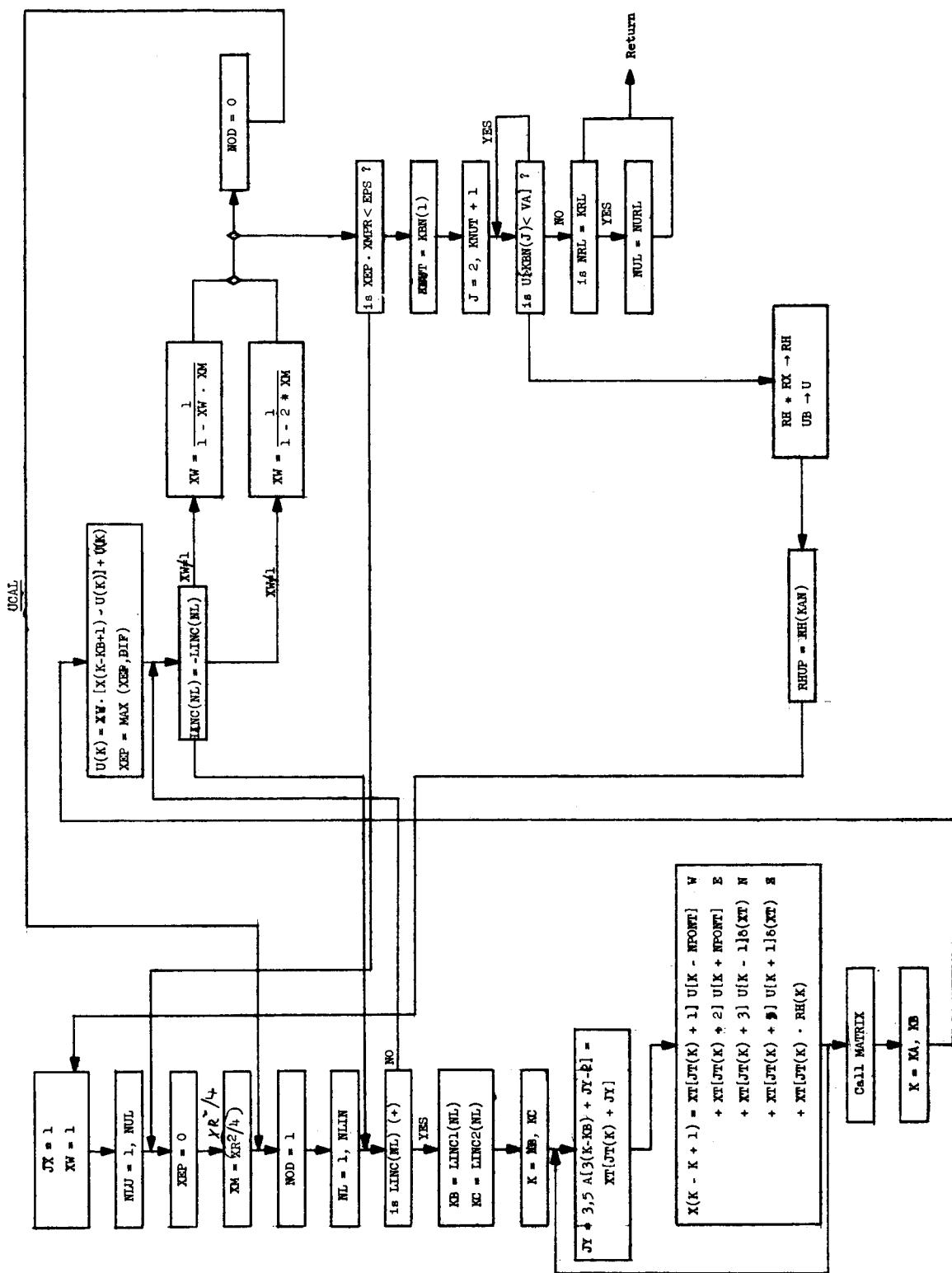












REFERENCES

1. V. Hamza, "Design Analysis of Electrostatic Thrustors by a Computer Technique," Microwave Laboratory Report No. 1327, Stanford University (May 1965).
2. V. Hamza and G. S. Kino, "Error Analysis of a Numerical Solution to Space-charge-flow Problems," Microwave Laboratory Report No. 1335, Stanford University; submitted for publication to Quarterly of Applied Mathematics, June 1965.
3. V. Hamza, "Convergence and Accuracy Criteria of Iteration Methods for the Analysis of Axially Symmetric and Sheet Beam Electrode Shapes with an Emitting Surface," Microwave Laboratory Report No. 1332 Stanford University; Submitted for publication to IEEE Trans. on Electron Devices, May 1965.

ERRATUM to AFCRL-TDR-65-816

In DD Form 1473, last page of above report, initial date of period covered by the report, given as 23 Mar '63 should read 21 Mar '63.

Distribution: one copy of ERRATUM sheet to all recipients of report listed in Distribution List in report.

MCDONNELL